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# Greenhouse Warming Reduces Global Energy Conversion Into Oceanic Lee Waves

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### Key Points:

- The response of energy conversion into lee waves to greenhouse warming is investigated with a high-resolution coupled global climate model
- Lee wave conversion rate is projected to decrease by ~20% by the end of 21st century under the high carbon emission scenario
- This decrease is attributed to the weakened bottom large-scale flows, mesoscale eddies and stratification

### Supporting Information:

Supporting Information may be found in the online version of this article.

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**Abstract** Oceanic lee waves play an important role in dissipating wind-driven ocean circulations and powering turbulent diapycnal mixing. Here we investigate impacts of the greenhouse warming on global energy conversion into lee waves using a linear theory of lee wave generation and output from a high-resolution (0.1° for the ocean) coupled global climate model. The global energy conversion rate into lee waves under the historical (1930s) climate condition is estimated to be  $193.0 \pm 3.0$  GW. Under the high carbon emission scenario, this conversion rate is projected to decrease by about 20% by the end of 21st century, due to weakened bottom large-scale mean flows, mesoscale eddies and stratification. The decrease of the conversion rate is widespread and particularly pronounced in the Gulf Stream and Drake Passage.

**Plain Language Summary** Oceanic lee waves, a kind of stationary internal gravity waves, are generated when bottom flows impinge on small-scale uneven topography. They provide an energy pathway from wind-driven large-scale circulations to microscale turbulent mixing. Theories predict that the energy conversion into lee waves depends on the stratification and flow speed near the sea floor, both of which are likely to weaken under the greenhouse warming. In this study, we use a high-resolution coupled global climate model to estimate the response of global energy conversion into lee waves to the greenhouse warming. Our results show that, under the high carbon emission scenario, the global energy conversion into lee waves at the end of the 21st century will decrease by 20% compared to its level in the 1930s.

## 1. Introduction

Oceanic lee waves are generated via the interactions of bottom geostrophic flows with small-scale topography characterized by wavelengths typically ranging from 0.1 to 10.0 km (Bell, 1975a, 1975b). These waves can extract energy from the geostrophic flows and radiate upward into the ocean interior. The generation of lee waves results in a drag force on the background flow, acting as an energy sink for the flow (Naveira Garabato et al., 2013; L. Yang et al., 2021; L. Yang et al., 2023). When lee waves break due to the wave-wave interactions or shear instability, the energy extracted from the geostrophic flows is dissipated and a fraction of it is converted into ocean turbulent diapycnal mixing (e.g., Nikurashin et al., 2013).

The global energy conversion rate from geostrophic flows into lee waves is estimated to range from 0.2 to 0.75 TW, depending on the datasets and methods for estimation (Nikurashin & Ferrari, 2011; Scott et al., 2011; Wright et al., 2014). Despite the large difference of overall magnitude of the energy conversion rate, its geographical distribution is consistent across these studies, with the Southern Ocean (SO) playing a dominant role. In view that the global wind work into the surface geostrophic currents is estimated to be around 1 TW (Wunsch, 1999), the generation of lee waves could be an important energy sink for wind-driven ocean circulations and a source for deep-ocean turbulent diapycnal mixing (Munk & Wunsch, 1998; Wunsch & Ferrari, 2004). Several studies based on observations (Brearley et al., 2013; Clément et al., 2016; Cusack et al., 2017; Evans et al., 2020; Hu et al., 2020; Meyer et al., 2016) and numerical models (Trossman et al., 2013; Trossman et al., 2016; Melet et al., 2014; Nikurashin et al., 2013; Z. Yang et al., 2021, 2022, 2023b) have highlighted the important role of lee waves in regulating the ocean energetics, powering turbulent diapycnal mixing, which in turn impacts the global climate system. Understanding the response of lee wave generation to the greenhouse warming is thus important for accurately predicting future climate changes.

Melet et al. (2015) investigated the changes of global energy conversion rate into lee waves under different warming scenarios using the linear theory (Bell, 1975a, 1975b) and a coarse-resolution coupled global climate model

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(CGCM). They reported that the global energy conversion rate into lee waves is projected to decrease by about 20% by the end of the 22nd century under a high carbon emission scenario mainly due to the weakening of the model-resolved large-scale mean flows near the sea floor. However, the oceanic resolution of their CGCM, that is, 1°, is insufficient to resolve the ocean mesoscale eddies that make dominant contribution to the total kinetic energy of the geostrophic flows (Ferrari & Wunsch, 2009).

In this study, we evaluate the response of the global energy conversion into lee waves to the greenhouse warming using an eddy-resolving (0.1° for the ocean) Community Earth System Model (hereinafter CESM-HR for short; Chang et al., 2020). Note that even at this high spatial resolution, the model is still unable to resolve lee waves and hence does not include feedbacks associated with them. The paper is organized as follows. Section 2 describes the linear theory of lee wave generation and the configurations of the CESM-HR. In Section 3, we compare the energy conversion rates into lee waves in the historical period (1930–1934) and in the end of the 21st century under the high carbon emission scenario, and analyze the factors responsible for the changes of the energy conversion rate. Sensitivity to the choice of Froude number (a nondimensional measure of topographic steepness) at which energy conversion saturates is also discussed. A summary is provided in Section 4.

## 2. Methodology

### 2.1. Linear Theory of Lee Wave Generation

In the case of sub-critical topography where slope of ocean topography is smaller than slope of radiating lee waves, the energy conversion rate from geostrophic flows into lee waves  $E$  can be derived from the linear theory (Bell, 1975a, 1975b):

$$E = \frac{\rho_0}{4\pi^2} \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} P(k, l) \frac{(\mathbf{U}_b \cdot \mathbf{k})}{|\mathbf{k}|} \sqrt{N_b^2 - (\mathbf{U}_b \cdot \mathbf{k})^2} \cdot \sqrt{(\mathbf{U}_b \cdot \mathbf{k})^2 - f^2} dk dl, \quad (1)$$

where  $\rho_0$  is the reference density,  $k = (k, l)$  is the horizontal wavenumber,  $P(k, l)$  is the two-dimensional topographic spectrum,  $N_b$  and  $\mathbf{U}_b$  are the bottom stratification (buoyancy frequency) and bottom velocity, and  $f$  is the Coriolis frequency.

Equation 1 is applicable only to the sub-critical topography. To account for the saturation of  $E$  over the super-critical topography (Nikurashin & Ferrari, 2010), the value of  $E$  in Equation 1 is multiplied by a factor of  $(Fr_c/Fr)^2$  for  $Fr > Fr_c$ , where  $Fr = N_b h / U_b$  is the Froude number with  $h$  the root-mean-squared height of the small-scale topography and  $Fr_c$  is the critical Froude number. In this study,  $Fr_c$  is set as 0.5 following Aguilar and Sutherland (2006), but other values of  $Fr_c$  (0.4 and 0.75) are also adopted to test the influences of  $Fr_c$  on the future change of  $E$ .

### 2.2. Topographic Spectrum

The topographic spectrum model proposed by Goff and Jordan (1988) is used to represent the small-scale topographic features:

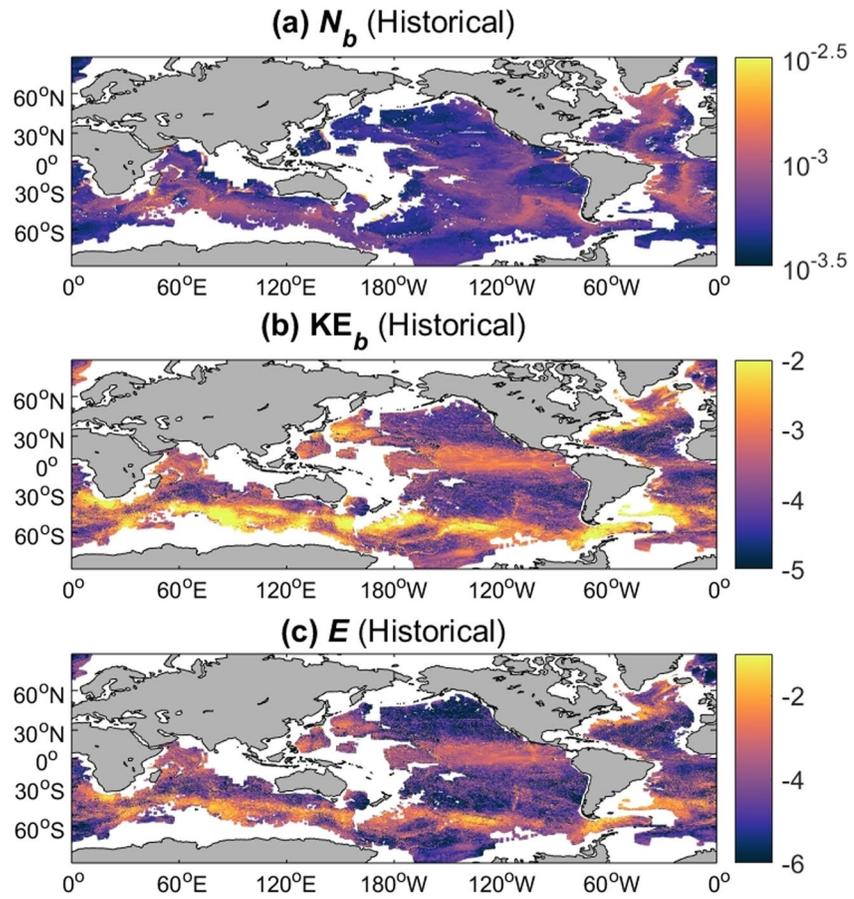
$$P(k, l) = \frac{2\pi H^2 (\mu - 2)}{k_0 l_0} \left[ 1 + \frac{k^2}{k_0^2} \cos^2(\phi - \phi_0) + \frac{l^2}{l_0^2} \sin^2(\phi - \phi_0) \right]^{-\frac{\mu}{2}}, \quad (2)$$

where  $H^2$  is the variance of the full topographic height,  $\mu$  is the roll-off slope at high wavenumber,  $\phi_0$  is the azimuthal angle and  $(k_0, l_0)$  are the characteristic wavenumbers. Goff (2010) (hereinafter G2010 for short) derived the values of these topographic parameters from satellite observations. In this study, we adopt the G2010's estimates that have been widely used in estimating  $E$  (e.g., Baker & Mashayek, 2022; Scott et al., 2011; L. Yang et al., 2018). It should be noted that  $P(k, l)$  of G2010 is not available everywhere due to the limitation associated with the algorithm employed (Figure 1). We remind readers that the “global ocean” in this study actually refers to the region where  $P(k, l)$  of G2010 is available.

### 2.3. Eddy-Mean Flow Decomposition

The geostrophic flows consist of the large-scale mean flows and mesoscale eddies. Correspondingly,  $E$  can be decomposed into contributions by large-scale mean flows ( $E_{LM}$ ) and mesoscale eddies ( $E_{ME}$ ) defined as (L. Yang et al., 2018):

$$E_{LM} = -\bar{\tau} \cdot \bar{\mathbf{U}}_b, \quad (3)$$



**Figure 1.** Time-mean (a) bottom stratification  $N_b$  ( $s^{-1}$ ), (b) bottom kinetic energy  $KE_b$  ( $m^2/s^2$ ) and (c) energy conversion rate into lee waves  $E$  ( $W/m^2$ ) during 1930–1934 simulated by the CESM-HR. Regions where the topographic spectrum of G2010 is unavailable are masked by white.

$$E_{ME} = -\overline{\tau' \cdot \mathbf{U}'_b}, \quad (4)$$

where  $\tau = -\frac{\rho_0}{4\pi^2} \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} P(k, l) \frac{k}{|k|} \sqrt{N_b^2 - (\mathbf{U}_b \cdot \mathbf{k})^2} \cdot \sqrt{(\mathbf{U}_b \cdot \mathbf{k})^2 - f^2} dk dl$  is the wave drag vector, the overbar denotes the annual average (large-scale mean flows) and the prime denotes the anomaly (mesoscale eddies). Note that, as the lee wave drag is a nonlinear function of the total bottom velocity, the presence of the eddy field also contributes to lee wave generation due to the mean flow, that is,  $E_{LM}$ . Following L. Yang et al. (2018), the contribution of mesoscale eddies to  $E_{LM}$  is quantified as:

$$C = \left[ 1 - \frac{\tau(\bar{\mathbf{u}}) \cdot \bar{\mathbf{u}}}{\tau(\mathbf{u}) \cdot \bar{\mathbf{u}}} \right] \times 100\%. \quad (5)$$

#### 2.4. CESM-HR

The CESM-HR is used to simulate the long-term changes of  $N_b$  and  $\mathbf{U}_b$  under the greenhouse warming. The CESM-HR has a nominal resolution of  $0.1^\circ$  ( $0.25^\circ$ ) for its oceanic (atmospheric) component. There are 62 vertical levels in the ocean with a maximum grid size of 250 m at the 6000-m depth. The simulation is branched off from a 500-year-long pre-industrial control simulation (PI-CTRL) at the 250th model year and integrated to 2100 with a historical run spanning from 1850 to 2005, followed by a future transient climate run from 2006 to 2100 under the representative concentration pathway 8.5 (RCP8.5) scenario. The monthly mean temperature, salinity and three-dimensional velocity are saved during the simulation. In addition, there are daily output for these variables during 1930–1934 (historical period) and 2086–2090 (future period).

**Table 1**

The Globally Integrated Time-Mean Energy Conversion Rate Into Lee Waves  $E$  Under Different Conditions of  $N_b$  and  $U_b$  and Using Different Values of  $Fr_c$

$N_b$ (s <sup>-1</sup> )	$U_b$ (m/s)	$Fr_c$	$E$ (GW)
Historical	Historical	0.5	193.0 ± 3.0
Historical	Historical	0.4	179.4 ± 2.8
Historical	Historical	0.75	218.3 ± 3.4
Future	Future	0.5	155.5 ± 4.8
Future	Future	0.4	142.4 ± 4.2
Future	Future	0.75	169.3 ± 5.6
Historical	Future	0.5	166.9 ± 4.5
Future	Historical	0.5	176.5 ± 3.2

Note. The errorbar corresponds to the 95% confidence interval.

In this study,  $N_b$  is computed as the value of  $N$  at the vertical level just over the sea floor, while  $U_b$  is computed as the vertically averaged  $U$  within 0–500 m over the sea floor (L. Yang et al., 2018). The model drift after 250 year's spin-up is negligible for  $U_b$  but less so for  $N_b$  (Figure S1 in Supporting Information S1). This may bias the simulated long-term change of  $E$  under the greenhouse warming. To minimize such bias, we subtract the linear trend of  $N_b$  during the model years 250–500 in PI-CTRL from  $N_b$  during 1850–2100. Then the daily  $U_b$  and the time-mean  $N_b$  during 1930–1934 (2086–2090) are substituted into Equation 1 to estimate  $E$  in the historical (future) period. The inter-annual variability of  $E$  within each five-year period is found to be much smaller than the difference of  $E$  between these two periods (Table 1), lending support that the five-year period is sufficiently long to get statistically robust results. Using different  $N_b$  definitions (e.g., the bottom-most  $N_b$  or daily  $N_b$ ) is found to have a minor influence on the energy flux calculation.

### 3. Results

#### 3.1. Energy Conversion Into Lee Waves in the Historical Period Simulated by CESM-HR

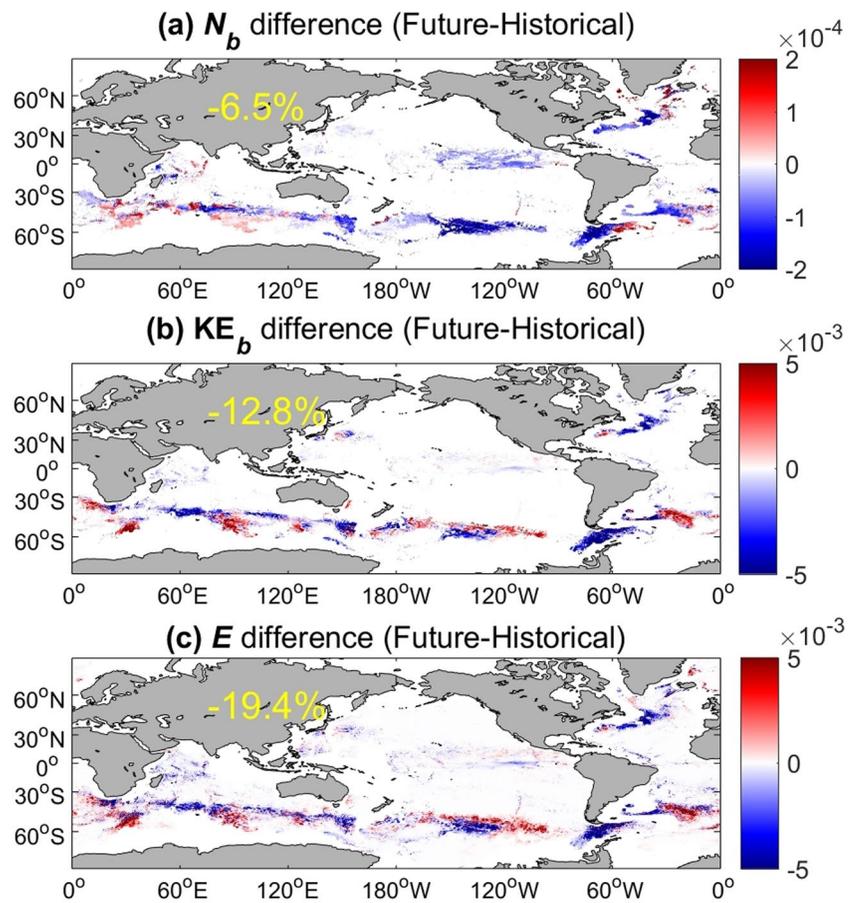
The time-mean  $N_b$  during the historical period in the CESM-HR is spatially inhomogeneous and generally consistent with that derived from observations (Teague et al., 1990; Figure 1a; Figure S2a in Supporting Information S1). Weak bottom stratification with  $N_b \sim O(10^{-4} \text{ s}^{-1})$  is found in most parts of the ocean, whereas large  $N_b \sim O(10^{-3} \text{ s}^{-1})$  is mainly concentrated along shallow mid-ocean ridges. Consistent with other eddy-resolving ocean model simulations (von Storch et al., 2012; Figure S2b in Supporting Information S1), the spatial variability of time-mean  $KE_b = (U_b \cdot U_b)/2$  is even more pronounced, varying by three orders of magnitude (Figure 1b). Large  $KE_b \sim O(10^{-2} \text{ m}^2/\text{s}^2)$  occurs along the western boundaries of ocean basins, the SO and the eastern tropical Pacific, whereas small  $KE_b \sim O(10^{-5} \text{ m}^2/\text{s}^2)$  is mainly distributed in the gyre interior. Furthermore, over most part of the global ocean,  $KE_b$  is dominated by kinetic energy associated with mesoscale eddies (Figure S7 in Supporting Information S1).

Consistent with the existing literature (Nikurashin & Ferrari, 2011; Scott et al., 2011), the spatial distribution of time-mean  $E$  during the historical period shows large values in the SO, the western boundaries of ocean basins and the eastern tropical Pacific (Figure 1c). The globally integrated time-mean  $E$  during 1930–1934 is  $193 \pm 3.0$  GW (hereinafter the errorbar represents the 95% confidence interval), close to the lower bound of the previous estimates (Nikurashin & Ferrari, 2011).

#### 3.2. Response of Energy Conversion Into Lee Waves to Greenhouse Warming

Consistent with previous studies (e.g., Caesar et al., 2018; Swart & Fyfe, 2012), we find an increase in the strength of the westerly winds in the Southern Ocean (Figure S3 in Supporting Information S1) and a weakening of the Atlantic Meridional Overturning Circulation (AMOC; Figure S4 in Supporting Information S1) in response to future climate change. These atmospheric and oceanic changes could further affect the ocean bottom environment. As suggested by Equation 1,  $N_b$  and  $KE_b$  are the two important factors determining the magnitude of  $E$ . To understand the change of  $E$  under the greenhouse warming, the differences of time-mean  $N_b$  and  $KE_b$  between 1930–1934 and 2086–2090 are examined. Because the geographical distribution of  $E$  is highly inhomogeneous (Figure 1c), we focus on the differences in regions where historical  $E > 0.52 \text{ mW/m}^2$  (indicated by color shading in Figures 2a and 2b). Although these regions only cover a quarter of the ocean area, they contribute to ~90% of the total  $E$ . These regions are referred to as the active- $E$  ocean hereinafter. Note that the mask for the active- $E$  ocean is designed to be broad enough to encompass the strong lee wave generation regions under future climate conditions.

Figure 2a shows the difference of time-mean  $N_b$  between 1930–1934 and 2086–2090 over the active- $E$  ocean (see Figure S5 in Supporting Information S1 for differences in the whole ocean). There is a decrease of  $N_b$  under the greenhouse warming in most parts of the active- $E$  ocean. Patches of enhanced  $N_b$  are mainly confined to the SO (e.g., 60°W–120°E) and the high-latitude regions of the North Atlantic. The changes in the deep ocean stratification depend on processes leading to ventilation of deep water. For example, warming of the Antarctic



**Figure 2.** Change of time-mean (a) bottom stratification  $N_b$  ( $s^{-1}$ ), (b) bottom kinetic energy  $KE_b$  ( $m^2/s^2$ ) and (c) energy conversion rate into lee waves  $E$  ( $W/m^2$ ) during 2086–2090 relative to their counterparts during 1930–1934 simulated by the CESM-HR. (a) and (b) only show the results in the active- $E$  ocean. Yellow numbers indicate the percentage changes of  $N_b$  and  $KE_b$  averaged over the active- $E$  ocean in (a) and (b), but the percentage change of  $E$  averaged over the global ocean in (c).

Bottom Water and cooling of the North Atlantic Deep Water would decrease the deep ocean stratification (Zhao & Thurnherr, 2018). The time-mean  $N_b$  averaged over the active- $E$  ocean decreases by 6.5% in response to the greenhouse warming. This appears contrary to the findings of Melet et al. (2015) who reported an overall increase of  $N_b$  in a warming climate but is qualitatively consistent with the projections from the high-resolution CGCMs in the Coupled Model Intercomparison Project Phase 6 (CMIP6) archive (Eyring et al., 2016; Table S1 and Figure S6 in Supporting Information S1). Furthermore, it should be noted that the calculation made by Melet et al. (2015) covers the entire ocean and includes regions with small  $E$  values, which can lead to misleading conclusions about the effects of  $N_b$  change on  $E$  change. For example,  $N_b$  along the shallow mid-ocean ridges increases significantly under the greenhouse warming (not shown). But the increase of  $N_b$  there should contribute little to the change of globally integrated  $E$ .

The value of  $KE_b$  decreases under the greenhouse warming over most parts of the active- $E$  ocean, with patches of increased  $KE_b$  in the SO. The most notable decrease of  $KE_b$  is located in the Gulf Stream, the Drake Passage and the Kerguelen Plateau, where the time-mean  $KE_b$  during 2086–2090 is less than 50% of that during 1930–1934. Such regional strong response of  $KE_b$  to the greenhouse warming may be related to multiple dynamical processes. For example, the decrease of  $KE_b$  in the Gulf Stream region may be related to the weakening of the deep western boundary current in response to the slowdown of the North Atlantic Deep Water formation rate (Dickson et al., 2002), while the decrease of  $KE_b$  in the South Atlantic may be related to the slowdown of the Antarctic Bottom Water formation rate (Zhou et al., 2023) or the shift of the Antarctic Circumpolar Current (Beech et al., 2022). The weakened eddy field plays a more important role in the reduction of  $KE_b$ , although the weakened mean flow also contributes (Figure S7 in Supporting Information S1).

The globally integrated time-mean  $E$  during 2086–2090 decreases to  $155.5 \pm 4.8$  GW, a  $\sim 20\%$  reduction compared to  $193.0 \pm 3.0$  GW during 1930–1934 (Table 1). The change of  $E$  under the greenhouse warming is spatially inhomogeneous and generally resembles that of  $KE_b$  (Figures 2b and 2c). Significant decreases in energy conversion can be found in the Gulf stream and Drake passage, whereas other regions of the Southern ocean show a meridional shift more than a simple decrease. To quantify the respective contribution of the changes of  $N_b$  and  $KE_b$  to the change of  $E$ , we recompute  $E$  during 2086–2090 by either fixing  $N_b$  or  $KE_b$  as their historical values, denoted as  $E_{N\text{-fix}}$  and  $E_{U\text{-fix}}$  respectively (Table 1). The globally integrated time-mean  $E_{N\text{-fix}}$  ( $166.9 \pm 4.5$  GW) and  $E_{U\text{-fix}}$  ( $176.5 \pm 3.2$  GW) during 2086–2090 are close to each other and significantly smaller than the globally integrated time-mean  $E$  ( $193.0 \pm 3.0$  GW) during 1930–1934. Therefore, both the weakened  $N_b$  and  $KE_b$  contribute importantly to the reduction of  $E$  under the greenhouse warming. Nevertheless, the relative importance of  $N_b$  and  $KE_b$  changes in determining the change of  $E$  is region-dependent (Figure 2). For instance, the reduced  $E$  under the greenhouse warming in the Gulf stream and the Drake Passage is primarily explained by the decreased  $KE_b$ , whereas the reduced  $E$  in the Pacific section of SO (e.g.,  $120^\circ\text{W}$ – $150^\circ\text{W}$ ) is largely attributed to the reduced  $N_b$  there.

### 3.3. Role of Mesoscale Eddies in the Change of Energy Conversion Into Lee Waves Under Greenhouse Warming

Both the interactions of large-scale mean flows and mesoscale eddies with topography generate lee waves. The time-mean  $E_{ME}$  and  $E_{LM}$  during 1930–1934 share similar spatial distributions (Figures 3a and 3b). However,  $E_{ME}$  is systematically larger in magnitude than  $E_{LM}$  and accounts for two-thirds of the globally integrated time-mean  $E$ , consistent with the dominant contribution of mesoscale eddies to the total kinetic energy of geostrophic flows (Wunsch & Ferrari, 2004; Figure S7 in Supporting Information S1). Under the greenhouse warming, the values of  $E_{ME}$  and  $E_{LM}$  are reduced over most parts of the global ocean (Figures 3c and 3d). The globally integrated time-mean  $E_{ME}$  during 2086–2090 is 20.5% smaller than that during 1930–1934, close to the 17.1% reduction for  $E_{LM}$ . However, as  $E_{ME}$  has larger magnitude in the historical period than  $E_{LM}$ , the change of globally integrated time-mean  $E$  under the greenhouse warming is primarily attributed to that of  $E_{ME}$ .

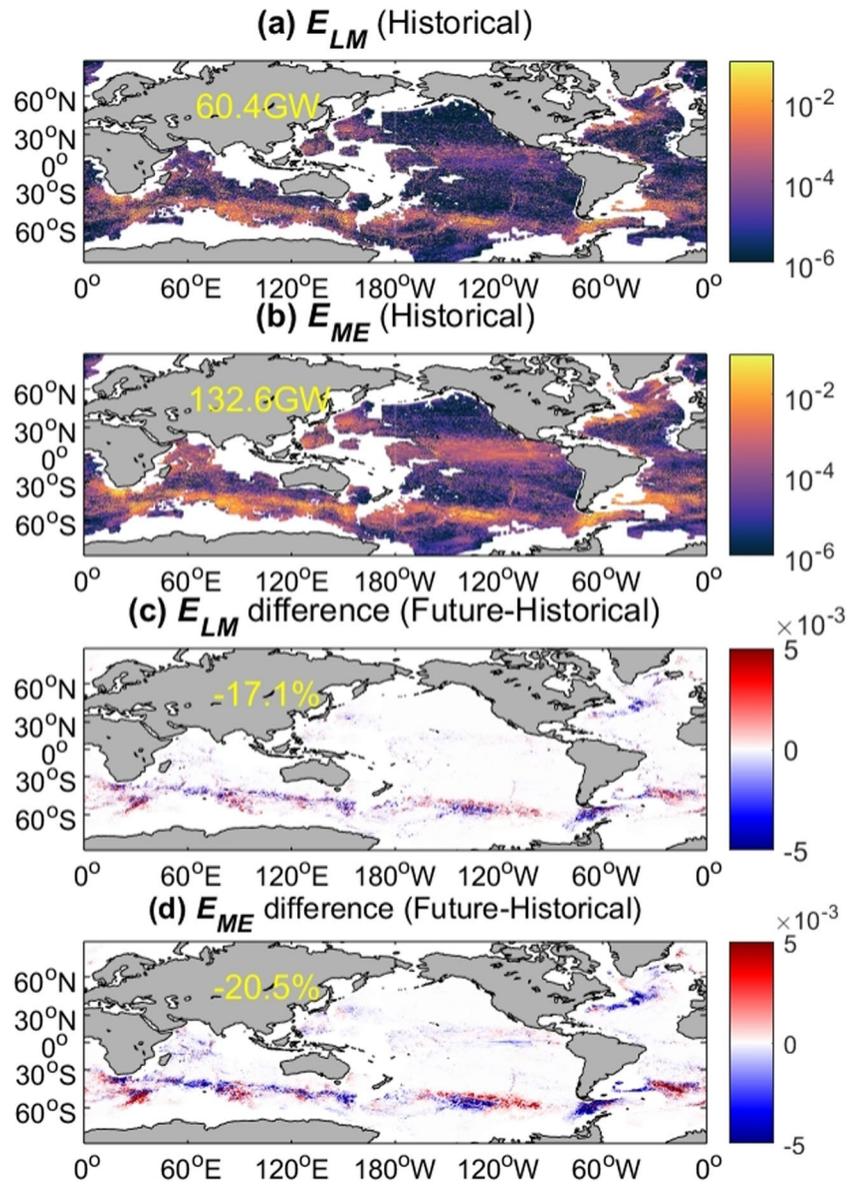
Due to the nonlinear dependence of the lee wave drag on bottom velocity, the eddy velocity contributes to  $E_{LM}$ , which is evaluated here using Equation 5. Our result shows that the presence of the eddy field significantly enhances the energy conversion into lee waves due to the mean flow (48.7% and 45.7% for the historical and future periods), highlighting the important role of eddies in shaping the time-mean wave drag.

### 3.4. Sensitivity to Critical Froude Number

One tuning parameter in the computation of Equation 1 is  $Fr_c$  that accounts for the saturation of  $E$  over the super-critical topography (Nikurashin & Ferrari, 2010). Although  $Fr_c$  is set as 0.5 in this study, it is worth pointing out that other values like 0.4 and 0.75 are also adopted in the existing literature (Nikurashin et al., 2014; Scott et al., 2011). To evaluate to what extent the uncertainties in  $Fr_c$  affect the change of  $E$  under the greenhouse warming, we perform sensitivity tests by varying the value of  $Fr_c$  from 0.4 to 0.75. The globally integrated time-mean  $E$  during 1930–1934 increases sublinearly with the increase in  $Fr_c$ , ranging from  $179.4 \pm 2.8$  GW for  $Fr_c = 0.4$  to  $218.3 \pm 3.4$  GW for  $Fr_c = 0.75$  (Table 1). This sublinear dependence of the globally integrated time-mean  $E$  on  $Fr_c$  is attributed to the fact that a significant portion of  $E$  originates from the SO where  $Fr$  is generally less than 0.4 (Figure S8 in Supporting Information S1). As a result, the value of  $E$  in the SO does not change as  $Fr_c$  varies from 0.4 to 0.75. Although  $Fr_c$  has some noticeable influence on the globally integrated time-mean  $E$ , the reduction of the globally integrated time-mean  $E$  is robust regardless of the value of  $Fr_c$ . The globally integrated time-mean  $E$  during 2086–2090 decreases by 20.6%, 19.4% and 22.4% compared to their counterparts during 1930–1934 for  $Fr_c = 0.4, 0.5$  and  $0.75$ , respectively. We conclude that the uncertainties in  $Fr_c$  do not have a substantial impact on the percentage change of  $E$  under the greenhouse warming.

## 4. Summary

In this study, we investigated the response of energy conversion into lee waves to the greenhouse warming by applying the linear theory of lee wave generation to the climate simulation of the CESM-HR resolving mesoscale eddies. The globally integrated time-mean  $E$  during the historical period (1930–1934) is estimated to be



**Figure 3.** Time-mean energy conversion rate into lee waves contributed by (a) large-scale mean flows  $E_{LM}$  and (b) mesoscale eddies  $E_{ME}$  ( $\text{W}/\text{m}^2$ ) during 1930–1934 simulated by the CESM-HR. Regions where the topographic spectrum of G2010 is unavailable are masked by white. (c) and (d) Same as (a) and (b) but for the change of time-mean  $E_{LM}$  and  $E_{ME}$  during 2086–2090 relative to their counterparts during 1930–1934. Yellow numbers indicate the globally integrated time-mean  $E_{LM}$  and  $E_{ME}$  in (a), (b) and their percentage changes under the greenhouse warming in (c), (d).

$193.0 \pm 3.0$  GW, with the lee wave generation over the SO making dominant contribution. Under the high carbon emission scenario, the globally integrated time-mean  $E$  during 2086–2090 decreases by  $\sim 20\%$  compared to that during 1930–1934. This decrease is attributed to the weakened bottom large-scale mean flows, mesoscale eddies and stratification under the greenhouse warming.

Our findings are qualitatively consistent with those reported by Melet et al. (2015). However, the projected reduction of  $E$  by the CESM-HR is quantitatively more evident than that (a 20% decrease by the end of the 22nd century) projected by the coarse-resolution CGCM used by Melet et al. (2015). This difference may result from two aspects. First, although Melet et al. (2015) found that the change of  $N_b$  has little effect on the change of  $E$  under the greenhouse warming,  $N_b$  is projected by the CESM-HR to be reduced (Figure 2a) and contributes importantly to the reduced  $E$  (Table 1). We note that the projected reduction of  $N_b$  by the CESM-HR is

consistent with the projections by the high-resolution CMIP6 CGCMs (Figure S6 in Supporting Information S1), lending support to its reliability. Second, the weakened mesoscale eddy flows near the sea floor projected by the CESM-HR make important contribution to the reduction of  $E$  under the greenhouse warming, whereas such effects are not directly resolved in the coarse-resolution CGCM of Melet et al. (2015).

The globally integrated time-mean wind power on the surface geostrophic flows remains nearly unchanged between 1930–1934 ( $0.69 \pm 0.01$  TW) and 2086–2090 ( $0.75 \pm 0.01$  TW). The significant reduction of  $E$  under the greenhouse warming thus suggests that the lee wave generation becomes less efficient in dissipating the wind-driven ocean circulations. Furthermore, the reduced  $E$  implies weakened energy source of turbulent diapycnal mixing. Changes of these processes have not been parameterized in the current generation of CGCMs but are likely to play an important role in regulating the ocean's heat uptake and carbon sequestration under the greenhouse warming.

The lee waves can alter  $N_b$  (through lee wave-driven mixing) and  $KE_b$  (through the generation, propagation and dissipation of lee waves in a vertically sheared mean flow). For example, Trossman et al. (2013) found that both  $N_b$  and  $KE_b$  are reduced when a lee wave parameterization is included in an ocean model. Furthermore, recent studies suggest significant changes in the sensitivity of the Antarctic Circumpolar Current and ocean stratification to wind when lee waves are included (L. Yang et al., 2021; L. Yang et al., 2023). The coupled climate model employed in this study, despite running at an eddy-resolving resolution, does not resolve lee waves and therefore does not include these feedbacks associated with lee waves. Considering the projected reduction of  $E$  in response to greenhouse warming, including the feedback of lee waves could potentially lead to smaller reductions in future  $N_b$  and  $KE_b$ , which consequently results in a lesser overall reduction in future  $E$ . This suggests that our projected reduction of  $E$  may have been overestimated due to the lack of lee wave feedback.

Finally, this study does not take into account the impact of the greenhouse warming on the lee wave-geostrophic flow interactions during the upward radiation of lee waves. In addition to  $Fr$ , the lee wave energy flux is also regulated by the vertical structure of the bottom flow. Recent studies (e.g., Baker & Mashayek, 2021; Kunze & Lien, 2019; Sun et al., 2022; Wu et al., 2022; Z. Yang et al., 2023a) suggest that lee wave-geostrophic flow interactions can either transfer energy from lee waves to geostrophic flows or the opposite. The greenhouse warming does not only affect  $N_b$  and  $U_b$  but also the vertical structure of geostrophic flows in the ocean interior (Peng et al., 2022), with the later playing a key role in the energy exchange between geostrophic flows and lee waves (Kunze & Lien, 2019). The impact of the greenhouse warming on the lee wave-geostrophic flow interactions is left for a future study.

## Data Availability Statement

The CESM-HR output can be downloaded from the website [https://ihesp.github.io/archive/products/ds\\_archive/Sunway\\_Runs.html](https://ihesp.github.io/archive/products/ds_archive/Sunway_Runs.html) by selecting the tab “500-YEAR 1850 PRE-INDUSTRIAL CONTROL” and “250-YEAR 1850 TRANSIENT SIMULATIONS”. The CMIP6 model data can be downloaded from <https://esgf-node.lnl.gov/search/cmip6/>. The CMIP6 CGCMs used in this study are listed in Table S1 in Supporting Information S1. Code for calculating energy conversion rate into lee waves is available at <https://doi.org/10.7910/DVN/WDRLG5>.

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