



14 **Abstract**

15 Sexual selection and sexual antagonism are important drivers of eco-evolutionary processes. The  
16 evolution of traits shaped by these processes depends on their genetic architecture, which remain  
17 poorly studied. Here, implementing a quantitative genetics approach using diallel crosses of the bulb  
18 mite, *Rhizoglyphus robini*, we investigated the genetic variance that underlies a sexually-selected  
19 weapon that is dimorphic among males and female fecundity. Previous studies indicated that a negative  
20 genetic correlation between these two traits likely exists. We found male morph showed considerable  
21 additive genetic variance, which is unlikely to be explained solely by mutation-selection balance,  
22 indicating the likely presence of large-effect loci. However, a significant magnitude of inbreeding  
23 depression also indicates that morph expression is likely to be condition-dependent to some degree and  
24 that deleterious recessives can simultaneously contribute to morph expression. Female fecundity also  
25 showed a high degree of inbreeding depression, but variance in female fecundity was mostly explained  
26 by epistatic effects, with very little contribution from additive effects. We found no significant genetic  
27 correlation, nor any evidence for dominance reversal, between male morph and female fecundity. The  
28 complex genetic architecture underlying male morph and female fecundity in this system has important  
29 implications for our understanding of the evolutionary interplay between purifying selection and  
30 sexually antagonistic selection.

31

32 **Keywords:** quantitative genetics, diallel, dimorphism, genetic architecture, dominance reversal,  
33 condition-dependence, large-effect loci

## 34 **Introduction**

35 The nature of genetic variation segregating in natural populations is of considerable interest in  
36 evolutionary genetics as standing genetic variance constitutes a major source of a population's short-  
37 term evolutionary potential (Barton and Keightley 2002; Barrett and Schluter 2008). Understanding the  
38 nature of genetic variation has also been of particular importance in the development of sexual  
39 selection theory, as it forms the basis of hypotheses explaining indirect genetic benefits of female  
40 mating preferences for costly and exaggerated male signalling structures (Andersson 1986; Rowe and  
41 Houle 1996), and the phenotypic variation that exists in traits which are used during male contest  
42 competition (Berglund et al. 1996). This phenotypic variation may take the shape of the discontinuous or  
43 discrete expression of the traits that mediate sexual competition and the evolution of alternative  
44 reproductive phenotypes adopting different reproductive strategies (Gross 1996; Sinervo and Lively  
45 1996; Gross and Repka 1998; Brockmann 2001; Shuster and Wade 2003; Tomkins and Hazel 2007). Such  
46 alternative reproductive phenotypes are found in a wide diversity of taxa (Oliveira et al. 2008) and are  
47 hypothesised to exist due to the costliness of these traits where only males of high 'quality' (Zahavi  
48 1975) or 'status' (Gross 1996) can pay the costs of expression.

49 One of most likely sources of variation in male genetic quality stems from the continuous influx of  
50 deleterious mutations that will segregate in populations at low frequency under mutation-selection  
51 balance (Haldane 1937; Lande 1975; Lynch et al. 1999). Such deleterious mutations will be spread across  
52 the genome (Andersson 1986), reducing the amount of resources available for an individual to allocate  
53 toward fitness related traits, commonly referred to as an individuals' 'condition' (Rowe and Houle 1996).  
54 Condition-dependence of exaggerated sexually selected trait (SST) expression can become an  
55 evolutionary stable strategy (Maynard Smith and Price 1973), when the survival costs of expressing SSTs  
56 in poor-condition individuals exceeds their reproductive benefits (Grafen 1990; Gross and Repka 1998).

57 The evolution of this condition-dependence thus causes SST expression to be informative of male  
58 genetic quality. Furthermore, in at least some taxa it underlies the evolution and expression of  
59 alternative reproductive phenotypes, where high-condition males develop into aggressive morphs that  
60 engage in contest competition over access to females and express disproportionately large and costly  
61 SSTs. In contrast, poor-condition males express disproportionately small or have complete absence of  
62 SSTs and adopt non-aggressive, often 'sneaky' mating tactics (Gross 1996). Implicating loci underlying  
63 the genetic variance of condition-dependent SSTs has been challenging due to the nature of this  
64 variance, i.e. a large number of loci each with individually small effect sizes (Rowe and Houle 1996).  
65 Despite challenges, a number of recent examples appear consistent with this scenario and include the  
66 polygenic determination of antlers in red deer, *Cervus elaphus* (Peters et al. 2022), mating success in  
67 *Drosophila melanogaster* (Dugand et al. 2019) and the discontinuous expression of a sexually selected  
68 weapon in the bulb mite, *Rhizoglyphus robini* (Parrett et al. 2022).

69 However, some systems do not conform to this polygenic condition-dependence model, with SST  
70 expression determined by relatively few genes or even a single gene (or supergene) of large effect  
71 (Shuster and Wade 1991; Sinervo and Lively 1996; Johnston et al. 2013; Küpper et al. 2016; Lamichhaney  
72 et al. 2016; Hendrickx et al. 2022). The maintenance of variation in such systems with large-effect  
73 quantitative trait loci (QTLs) is likely a consequence of balancing selection, for example negative  
74 frequency-dependence (Gross 1991) or Rock-Paper-Scissor games (Sinervo and Lively 1996) predicted by  
75 evolutionary game theory (Maynard Smith 1982), or antagonistic pleiotropy and life-history trade-offs  
76 (Johnston et al. 2013; Mérot et al. 2020). One other possible widespread form of balancing selection  
77 may stem from sexual antagonism, which could have both large-effect QTLs or polygenic underpinnings,  
78 and sexually antagonistic polymorphisms maintained due to alternative alleles having opposite fitness  
79 consequences in each of the sexes (Connallon and Clark 2012, 2014). A potentially major source of  
80 sexual antagonism may stem from the expression of SSTs, where high-fitness males expressing

81 elaborated SSTs sire low-fitness daughters (Harano et al. 2010; Plesnar-Bielak et al. 2014; Okada et al.  
82 2021). The likelihood of such polymorphisms being maintained by sexually antagonistic selection  
83 increases with epistasis between antagonistic loci (Arnqvist et al. 2014), as well as beneficial reversals of  
84 dominance between the antagonistic alleles within a given locus (Barson et al. 2015; Grieshop and  
85 Arnqvist 2018; Connallon and Chenoweth 2019) – both of which reduce the fitness costs of carrying any  
86 of the ‘wrong’ alleles for one’s sex. Thus, studying the genetic architecture of SSTs and associated  
87 sexually antagonistic effects to female fitness (i.e. partitioning total trait variance into that stemming  
88 from additivity, dominance and epistasis) will help to clarify whether variation in such traits is  
89 maintained by balancing selection, mutation-selection balance, or some combination of the two.

90 The relative contributions of balancing selection and mutation-selection balance to the genetic variance  
91 in SST expression has important implications for sexual selection theory and beyond, but remains largely  
92 unresolved. For example, rapid adaptation to altered environments may be facilitated if genetic  
93 variation is maintained under balancing selection (Barrett and Schluter 2008), possibly stemming from  
94 sexual antagonistic selection (Connallon and Clark 2014). Moreover, sexual selection against deleterious  
95 mutations can also improve adaptation rates and/or reduce extinction risk (Lorch et al. 2003; Fricke and  
96 Arnqvist 2007; Jarzebowska and Radwan 2010; Plesnar-Bielak et al. 2012; Lumley et al. 2015; Martínez-  
97 Ruiz and Knell 2016; Parrett and Knell 2018; Cally et al. 2019; Parrett et al. 2019; Godwin et al. 2020) if  
98 condition-dependent expression of SSTs reveals individuals’ relative share of the population’s mutation  
99 load (Grieshop et al. 2021b). On the other hand, by favouring alleles that harm female/population  
100 offspring production (Holland 2002; Kokko and Brooks 2003; Rundle et al. 2006; Berger et al. 2016;  
101 Grieshop et al. 2017), increasing costs associated with SST expression (Doherty et al. 2003; Bro-  
102 Jørgensen 2014; Martins et al. 2018) or by reducing effective population size (Kokko and Brooks 2003;  
103 Parrett et al. 2022) adaptation rates may be hindered and extinction risks increased by sexual selection  
104 and sexual conflict.

105 Here, we implemented a quantitative genetic approach using diallel crosses in the bulb mite, *R. robini*, in  
106 order to partition genetic variance and investigate dominance relationships of a sexually selected  
107 weapon, which earlier work implied has sexually antagonistic effects on female fitness (Plesnar-Bielak et  
108 al. 2014; Łukasiewicz et al. 2020). Male *R. robini* comprise of two male morphs distinct in the expression  
109 of sexually selected weaponry (Parrett et al. 2022), the aggressive fighters have a thickened third pair of  
110 legs and use them while engaging in contest competition, which can be lethal. In contrast, the non-  
111 aggressive scramblers have legs with all approximately equal thickness and avoid direct competition  
112 (Radwan 1995; Radwan et al. 2000). Previous work has shown that males in poor phenotypic condition  
113 tend to express the scambler phenotype (Radwan 1995; Smallegange 2011), but male morph is  
114 nevertheless significantly heritable (Radwan 1995; Smallegange and Coulson 2011), with some previous  
115 data suggesting the existence of a large-effect QTL (Radwan 1995). Yet, other evidence suggests that  
116 fighters may be associated with a lower load of deleterious mutations (Łukasiewicz et al. 2020; Parrett  
117 et al. 2022), such that heritability of morph may result from polygenic condition-dependence. Fighter  
118 morphs tend to outcompete scramblers, which incur high mortality in inter-morph competition (Radwan  
119 et al. 2000; Radwan and Klimas 2001), yet the scambler morph persists. It is plausible that sexual  
120 antagonism may also contribute to the maintenance of genetic variance in male morph. Previous work  
121 showed that selection for morph results in correlated response in female fecundity, such that females  
122 from fighter-selected treatments have lower fecundity than females from scambler-selected  
123 treatments (Plesnar-Bielak et al. 2014; Łukasiewicz et al. 2020). The relative contribution of each of  
124 these candidate mechanisms remains unknown.

125 If indeed most of the genetic variance underlying morph is due to deleterious mutations, we can expect  
126 additive genetic variance to be moderate and comparable to other life history traits (Mousseau and Roff  
127 1987). Female fecundity is likely a useful benchmark as it is known to be a highly polygenic and  
128 therefore a large target for deleterious mutations to act upon (Houle 1992). Furthermore, if additive

129 genetic variance is determined by deleterious mutations it should also be accompanied by a comparable  
130 portion of dominance variation (Crnokrak and Roff 1995; Roff and Emerson 2006), and substantial  
131 inbreeding depression (DeRose and Roff 1999), because deleterious mutations segregating in natural  
132 populations are typically recessive (Charlesworth and Willis 2009). The potential for sexual antagonism  
133 to maintain male morph variation would be much enhanced if there were beneficial dominance reversal,  
134 that is, if dominant fighter morph (recessive scambler morph) allele(s) had recessive (dominant) effects  
135 on female fecundity. Under such dominance reversal, heterozygous fighter/scambler genotypes would  
136 express the male fighter morph and have high female fecundity, stabilising the underlying sexually  
137 antagonistic polymorphisms (Kidwell et al. 1977; Fry 2010). Therefore, we investigated dominance  
138 relationships for male morph and female fecundity. The relative dominance of each inbred lines' genetic  
139 variation over the other lines in the diallel was estimated as the covariance between their mean  
140 outcrossed values and the 'self-cross' means of the inbred lines they are crossed with (Grieshop and  
141 Arnqvist 2018). If these array covariances are positively correlated between male morph and female  
142 fecundity it would indicate that the underlying alleles are either dominant or recessive for both traits,  
143 whereas a negative correlation indicates that alleles are dominant for one trait but recessive for the  
144 other.

## 145 **Methods**

### 146 *General husbandry*

147 All mites were reared under standard laboratory conditions. Stock cultures were housed in plastic  
148 containers (~7 × 10 cm), large colonies (>10 mites) were reared in small plastic containers (~2.2 cm  
149 diameter), and small colonies (10 or less) or individual mites were housed in glass vials (~1 cm diameter).  
150 All containers and vials had a base of plaster-of-Paris (~1 cm) which was soaked in water prior to  
151 transferring any mites. In order to maintain humidity (> 90%), all mite housing was placed on damp

152 tissue paper and placed within a plastic box containing a ball of soaked tissue paper. Mites were stored  
153 in incubators kept at a constant 23°C. Powdered yeast was provided *ad libitum* for feeding. All housing  
154 was checked regularly, to ensure mites had access to yeast and humidity remained high.

#### 155 *Establishing inbred lines*

156 In brief, 41 inbred lines of *R. robini*, each founded by a single virgin female and male, were established  
157 from mites collected from onions in fields close to Mosina, Poland. The morph of each founding male  
158 was recorded and in subsequent generations of inbreeding males of the same morph as the founder  
159 male were used to propagate each inbred line (for full details see Łukasiewicz et al. 2020). Inbred lines  
160 were developed by full sib × sib mating for ten generations, inbreeding was then relaxed due to logistical  
161 constraints and inbred lines allowed to expand for approximately three months (~six generations). Full  
162 sib × sib inbreeding was then resumed for a further four generations, thus giving a total of fourteen  
163 generations of full sib × sib inbreeding. Inbred lines were again allowed to expand for approximately  
164 three months (~six generations) prior to the onset of the current experiment in order to have inbred  
165 lines of adequate and stable sizes that could be used for this experiment. During inbreeding protocols,  
166 after their initial establishment each inbred line was maintained with back-ups. Each generation we  
167 reared 20 larvae (or less if not available) to adulthood for each inbred line and mated each male of the  
168 appropriate morph with a randomly selected virgin female. One to five such pairs were formed, giving  
169 up to four backups per inbred line per generation. One of these families was randomly selected to found  
170 the next generation, but if this family failed to produce offspring, a random backup was selected to  
171 replace it. Before the first expansion (i.e. generation 10) we recorded 233 such cases (counts based on  
172 two families, per line, each generation), of which 199 were due to infertility, and 34 due to embryonic or  
173 larval mortality. Although non-significant ( $\chi^2 = 2.89$ , *d.f.* = 1, *p* = 0.089) there was a trend that  
174 reproductive failures were observed more often in fighter founded lines compared to those founded by

175 scamblers, with the average number of observed reproductive failures, per line, in each treatment  
176 being 6.42 and 4.40, respectively (Supplementary Figure 1).

### 177 *Diallel crosses and assays*

178 From those that survived the inbreeding programme we randomly selected 20 inbred lines, 10 founded  
179 by a fighter male and 10 from a scambler male. From each of these inbred lines we transferred 50  
180 females to a new container for egg-laying for five days, after which females were removed from  
181 containers. Three inbred lines, one founded by a fighter and two founded by a scambler, did not have  
182 enough females available, and only 20-30 were therefore placed in egg-laying containers. After a further  
183 six days we attempted to isolate approximately 200 F<sub>0</sub> larvae and proto-nymphs from each inbred line  
184 into individual vials. If on the first day of isolation we did not achieve adequate numbers, we continued  
185 isolating individuals on the next two consecutive days. The three inbred lines with low numbers of  
186 female parents (from above) were discarded at this stage due to low offspring numbers. In addition,  
187 another inbred line (founded by a fighter male) was discarded due to experimenter error. This left us  
188 with 16 inbred lines, eight founded by fighter males and eight founded by scambler males.

189 From these 16 inbred lines we created a partial diallel in a 'chess-board' design with reciprocal outbred  
190 crosses, and all possible inbred crosses. In total, this led to 144 cross combinations: 16 inbred self-  
191 crosses (i.e. sires and dams from the same inbred line), and 128 outbred crosses (i.e. sires and dams  
192 from different inbred lines) consisting of each inbred line crossed reciprocally with four fighter-founded  
193 and four scambler-founded inbred lines (see Figure 1). For each outbred cross we set up five replicate  
194 virgin pairs (P-generation) and for each inbred self-cross we increased this number to ten replicate virgin  
195 pairs (for two self-crosses: IN7 and IN14, it was only possible to establish seven and eight pairs,  
196 respectively). The mated pairs were left in vials together and females allowed to lay eggs for six days,  
197 after which the adults were removed from vials. After a further two days each vial was then checked for

198 larvae. We collected  $F_1$  larvae for two purposes: 1) to gain virgin females for fecundity assays and 2) to  
199 estimate male morph proportion. As it was not logistically feasible to isolate every single larva, and in  
200 order to spread our efforts as evenly as possible across the entire diallel, we stopped isolating larvae  
201 from an outbred cross when we had isolated our target number of larvae from three out of five replicate  
202 pairs (or six out of ten for self-crosses). We aimed to collect 70 larvae per replicate pair, with 10 larvae  
203 reared individually to obtain virgin females for fecundity assays, and the remaining reared in groups of  
204 10 individuals per vial (or less if not available) and used to determine morph proportion. These numbers  
205 of mites (10 or less) per vial represent low density rearing conditions. During larvae collection we  
206 prioritised fecundity assays and isolated larvae individually first. Until we reached these targets, we  
207 continued isolating larvae throughout the following ten days from all replicates of a cross combination.  
208 In some cases, we were not able to find enough larvae and on occasions a low level of opportunistic  
209 sampling was also performed. Data collected from all replicate pairs were included in our analyses. The  
210 number of males used to estimate morph proportion of each replicate is therefore varied, but any  
211 analysis (see below) takes this into account.

212 Morph proportion of  $F_1$  adults that eclosed from each group of larvae was determined eight days after  
213 larvae were isolated.  $F_1$  adults were sexed and male morph recorded before being removed from vials;  
214 any nymphs remaining were left in the vials for future morph scoring. Vials were then checked every  
215 other day for any remaining mites to mature, with the morph of any males being recorded. Housing  
216 mites in groups for morph proportion assays allowed us to sustainably increase sample size compared to  
217 if isolating individual larvae; the method choice is justified as it was previously shown that colony  
218 density does not influence morph determination in this species (Radwan 1995). Moreover, this better  
219 reflects housing conditions of mites within their pre-experiment conditions compared to individually  
220 housed mites. Although in some cases this led to deaths of males, most likely as a consequence of lethal  
221 combat, if vials are checked regularly dead mites can be sexed and male morph determined with relative

222 ease: only six dead mites across the entire experiment were unidentifiable. Splitting mites into vials with  
223 low density rearing conditions, rather than rearing all larvae in one pool, allowed us to have similar  
224 rearing densities when we did not obtain 60 larvae (the mites were then simply split among fewer  
225 groups) or if more offspring were produced and not separated. The numbers of fighters and scramblers  
226 were then pooled from these groups of mites for each replicate pair.

227 For female fecundity, vials containing individually housed  $F_1$  mites were checked every other day and  
228 adults sexed. Only females < 3 days post adult-eclosion were used in fecundity assays. From each cross  
229 combination we aimed to assay the fecundity of three  $F_1$  females from outbred crosses or six from  
230 inbred self-crosses – each from a unique P-generation pair when possible. Isolated  $F_1$  females were  
231 paired with a random < 3-day-old (post adult-eclosion) male of either morph from a large outbred stock  
232 population, as previous work has shown that male morph does not have direct effects on female  
233 fecundity in *R. robini* (Plesnar-Bielak et al. 2014; Parrett et al. 2022). Females were allowed to oviposit  
234 for 10 days, transferring the pair to a new vial on day 5 (replacing any dead males; in both first and  
235 second vials  $n = 19$  dead males were observed), and removing the pair on day 10. The intermittent  
236 removal of a male during fecundity assays does not lead to detectably lower female fecundity for at  
237 least two days (Kołodziejczyk and Radwan 2003), so these rare cases of male death were unlikely to  
238 affect our results. The eggs from both vials were counted the same day adults were removed from vials.  
239 On occasions some eggs had hatched and therefore larvae were also present in the vials, these were  
240 included in these counts as eggs. As these were relatively rare and an excess of food remained in tightly  
241 plugged vials we do not believe errors were introduced due to some eggs hatching. As female egg-laying  
242 rate remains relatively consistent over the first three weeks of their lives, after which females have  
243 declining fecundity (Tilszer et al. 2006), and because three weeks make up a significant proportion of an  
244 average females lifespan (3-5 weeks depending on study: Kołodziejczyk and Radwan 2003; Parrett et al.  
245 2022), such a measure is likely a good estimate of lifetime fitness. In an attempt to exclude the

246 possibility that females did not lay eggs due to a male effect (for example, male sterility or lack of  
247 mating), we provided a new male if there were zero eggs in the first vial. If in the second vial also there  
248 were zero eggs, we assumed this to be a consequence of the female, but if females produced eggs in the  
249 second vial (i.e. with a new male) we assumed the zero-count in the first vial to be an effect of the first  
250 male. We removed those later situations from our dataset ( $n = 25$ ), but retained the former as zero eggs  
251 laid.

252 We performed a partial second block specifically targeting cross combinations in which sample sizes  
253 were low or completely missing ( $n = 48$ ). Sample sizes for each cross combination were considered low if  
254 we did not have fecundity data for three females from outbred crosses or six females from inbred-self  
255 crosses and/or if we had determined the morph from less than 30 males from each outbred cross  
256 combination or 60 males from inbred-self crosses. Although unbalanced sampling effort exists between  
257 blocks 1 and 2, by repeating a partial block it allowed us to have estimates from cross combinations with  
258 completely missing data or improve estimates of those with low sample size, and it also allowed us to  
259 partition some variance due to environment factors (i.e. block). It should be noted that our statistical  
260 method for variance partitioning is specifically intended to accommodate imbalanced sampling in the  
261 diallel (Lenarcic et al. 2012).

## 262 *Statistical analysis*

263 We performed diallel analysis for sex-specific data separately. In each case we partitioned the genetic  
264 variance of each trait by fitting models using the package *litterDiallel* (Shorter et al. 2019). This package  
265 adapted the *BayesDiallel* (Lenarcic et al. 2012) Gibbs sampler to also allow generalised linear mixed  
266 models to be fitted using *MCMCglmm* (Hadfield 2010). Using this Bayesian modelling approach we were  
267 able to partition the phenotypic variation of male morph and female fecundity (separately) in the  $F_1$   
268 offspring of crosses between maternal strain  $j$  and paternal strain  $k$  into additive effects ( $a_j + a_k$ ),

269 parental-sex effects ( $m_j - m_k$ ), dominance effects ( $\beta_{\text{inbred.overall}} + \beta_j$ ), symmetric and asymmetric  
270 epistatic effects ( $v_{jk} + w_{jk}$ , respectively), and unexplained variance (noise;  $\varepsilon_i$ ), as follows:

$$271 \quad \mathbf{d}^T \boldsymbol{\beta} = \{a_j + a_k\} + \{m_j - m_k\} + I_{\text{inbreds}}(\beta_{\text{inbred.overall}} + \beta_j) + I_{\text{hybrids}}(v_{jk} + w_{jk})$$

272 Male morph proportion is formulated as a binomial GLMM, with the observed proportion of each male  
273 phenotype  $i$  ( $y_i$ ) modelled as:  $y_i \sim \text{Binomial}(n_i, \pi_i)$ . Here,  $n_i$  is the total number of males and  $\pi_i$  is the  
274 proportion of fighters. In MCMCglmm, this is specified as a two-outcome “multinomial2” model with  
275  $n.\text{fighters}_i = n_i \cdot \pi_i$  and  $n.\text{scramblers}_i = n_i \cdot (1 - \pi_i)$ . The GLMM uses the inverse logit link to the  
276 standard BayesDiallel model, while controlling for overall fixed effects of mean ( $\mu$ ) and block, i.e.  $\pi_i =$   
277  $\text{logit}^{-1}(\mu + \text{block}_i \cdot \beta_{\text{block}} + \mathbf{d}^T \boldsymbol{\beta} + \varepsilon_i)$ . Female fecundity is formulated as a Gaussian linear model,  
278 with the  $Z$ -scores (see below) for each individual  $i$  modelled as:  $y_i = \mu + \text{block}_i \cdot \beta_{\text{block}} + \mathbf{d}^T \boldsymbol{\beta} + \varepsilon_i$ .  
279 Models were iterated 1,000,000 times, with a thinning interval of 1,000 and a burn-in of 50,000.  
280 Minimally informative priors ( $V = 1$ ,  $\text{nu} = 0.002$ ) were used during modelling. The variance components  
281 from the diallel random effects are modelled as in Shorter et al., (2019). Block was included as a fixed  
282 effect in both models.

283 Counts of male morph from all vials of a given replicate pair were combined and used to determine male  
284 morph proportion. In our experience humans may systematically differ in their counts of large numbers  
285 of small eggs, therefore for female fecundity data, in order to account for any such observer effects ( $n =$   
286 4 observers) we scaled egg counts for each observer individually and took the sum of  $Z$ -scores from both  
287 egg laying vials. In a number of cases the female died in the first vial ( $n = 14$ ) and therefore no second vial  
288 existed for these females. As we wanted to take this into account in our analysis, we scored the ‘second  
289 vial’ as having a count of zero. As a consequence, there was no second observer, so we assigned a  $Z$ -  
290 score equivalent to the mean  $Z$ -score of all observations with counts of zero. In addition, we ran the  
291 same fecundity model but took observer effects into account by taking the residuals from a simple

292 generalised model fit to fecundity count data with 'observer' as an explanatory variable. Comparison of  
293 DIC scores indicate that the model using *Z-scores* (DIC = 1898.2) had a substantially better fit compared  
294 to modelling residuals (DIC = 3942.4). We therefore only report the model using *Z-scores*.

295 To confirm all chains had good mixing we ran Gelman-Rubin analyses for each model: both had  
296 acceptable multivariate psrf scores below 1.1 (morph proportion = 1.07, fecundity = 1.06). In addition,  
297 we generated null posterior distributions for both models by randomising the unique cross identifier  
298 (within inbred and outbred crosses, separately) and repeating the above analyses, with the assumption  
299 that true signals of non-zero variance should be absent/zero in the randomized null distributions.

300 Diallel crosses also allow for the ordination of strains from those carrying the most dominant alleles to  
301 those carrying the most recessive alleles at the loci underlying the trait/s in question (Grieshop and  
302 Arnqvist 2018). The relative amount of dominant/recessive alleles in a given inbred line is estimated by  
303 the covariance of its mean outbred values ( $r$ ; averaged over all outbred combinations of a particular  
304 inbred strain) and the mean of the self-cross values of inbred lines to which it was crossed ( $P$ ). This was  
305 done separately for all strains, and separately for both male morph ( $\sigma_{PM,IM}$ ) and female fecundity  
306 ( $\sigma_{PF,IF}$ ). Positive covariance implies that the alleles a line carries are mostly recessive to alleles carried  
307 by the lines it was crossed with (i.e. their outbred values are dependent on the genetic makeup of the  
308 inbred line they are crossed with). Contrastingly, if an inbred line's outbred values do not covary with  
309 the self-cross values of inbred lines they are crossed with (i.e. values of or close to 0), this is an  
310 indication that they harbour more dominant alleles than the inbred lines they were crossed with (i.e.  
311 their outbred values are independent of the genetic makeup of the inbred line they are crossed with).  
312 This interpretation holds in absence of environmental and epistatic variation (Grieshop and Arnqvist  
313 2018). To fulfil that assumption, we first fit simple general and generalised linear models to fecundity (*Z-*  
314 *score*) and morph data, respectively, which modelled environmental effects by fitting block as a fixed

315 effect and modelled epistatic effects by fitting the sire x dam combination as a random effect, using the  
316 *lme4* package for R (Bates et al. 2015). The residuals from these models were then used to tabulate the  
317 mean values for each cross combination, which were used to calculate the array covariances described  
318 above (see supplementary S1 of Grieshop et al. 2021a for details). Inbred lines are ordinated according  
319 to their array covariances – their relative dominance/recessive relationships to one another. The array  
320 covariances were also used to test for dominance reversal between male morph and female fecundity: a  
321 negative genetic correlation between the traits would indicate that dominant alleles for one trait tend to  
322 be recessive for the other, whereas a positive genetic correlation would indicate that alleles tend to be  
323 either dominant or recessive for both traits alike – evidence for and against dominance reversals,  
324 respectively.

325 All statistical analysis was performed in R version 3.6 (R Development Core Team 2020).

## 326 **Results**

327 In total we recorded the morph of 8905 F<sub>1</sub> males across all diallel crosses: 1550 were from inbred crosses  
328 and 7355 were from outbred crosses, and 6572 were scambler and 2333 were fighter males. We also  
329 assayed the fecundity of 548 females, 138 from inbred crosses and 410 from outbred crosses. Across  
330 both blocks, morph proportion and female fecundity data was collected from 143 and 144 cross  
331 combinations, respectively (Figure 1).

332 A considerable percentage (86.38%) of the variance in morph proportion was explained by diallel  
333 effects, whereas a low percentage (13.62%) of that variance was noise (Figure 2). The majority of  
334 variance in morph proportion (62.77%) was explained by additive genetic variance, with symmetric  
335 epistatic effects (18.08%) explaining most of the remaining variance. Dominance variance, estimated by  
336 strain-specific inbreeding variance, explained only 4.94% of variance, an order of magnitude lower  
337 compared to additive variance. Reciprocal crosses that are autosomally identical but have inherited their

338 cytoplasm and sex-chromosomes from opposite inbred lines revealed almost no influence of parental  
339 effects or asymmetric epistasis (0.13% and 0.45% of total variance explained, respectively) on the  
340 probability of offspring being a fighter or scrambler. Looking at the highest posterior density (HPD)  
341 means and 95% credibility intervals (CIs) of the diallel effects and estimates of inbred line-specific effects  
342 provides more detail (Figure 3). The HPD mean for the fixed effect of inbreeding was negative and CIs,  
343 close to, but not overlapping zero – indicating effects of inbreeding depression on the expression of the  
344 fighter morph. The probability of offspring being either a fighter or scrambler was largely associated  
345 with founder morph treatment as seen in their individual additive effects. Seven of the eight fighter-  
346 founded inbred lines have positive additive effects (i.e. increased probability of male offspring being  
347 fighter) where the HPD interval does not overlap with 0, whereas, five of the eight scrambler-founded  
348 inbred lines had negative additive effects (i.e. increased probability of male offspring being a scrambler).  
349 A number of specific cross combinations showed symmetric epistatic effects on the probability of male  
350 offspring morph beyond their predictive additive effects alone, most notably IN9:IN5, IW1:IN9,  
351 IW23:IN8, IW23:IW1 and IW25:IW19 (Figure 3).

352 In contrast, considerably more of the variance (68.52%) for fecundity was attributed to noise and a  
353 lower percentage (31.48%) explained by diallel effects (Figure 4). The majority of this variance was  
354 explained by epistatic effects (symmetric = 12.37%, asymmetric = 10.36%), with the remaining explained  
355 by dominance variance (6.94%) and additive genetic variance (1.13%). As with the male morph data,  
356 there was next to no variance explained by parental effects (0.68%). Again, a detailed look at inbred line-  
357 specific HPD means and CIs provides further insight (Figure 5). There was a very pronounced fixed effect  
358 of inbreeding, with HPD mean being negative with no overlap with zero – indicating substantial effects  
359 of inbreeding depression on female fecundity. Additionally, inspection of how variance in fecundity was  
360 explained by symmetric and asymmetric epistatic effects shows three strain-pair specific estimates

361 where the 95% CIs do not overlap zero (v:IW16:IN3, v:IW24:IW17 and w:IW19:IN9) and many others  
362 whose HPD means are far from zero but whose 95% CIs nevertheless do overlap zero (Figure 5).

363 In both cases, randomisation of data structure showed that the above patterns are unlikely to be a  
364 consequence of random chance (random data structure; morph proportion: total explained variance =  
365 5.52%, noise = 94.48%; female fecundity: total explained variance = 4.75%, noise = 95.25%).

366 The cross-trait/cross-sex additive genetic correlation between female fecundity and morph proportion  
367 was negative but non-significant ( $r = -0.18$ ,  $p = 0.493$ ; Supplementary Figure 2). For morph proportion,  
368 dominance ordination revealed that fighter-founded inbred lines had significantly higher mean array  
369 covariances ( $\sigma_{PM,IM}$ ) than scrambler-founded inbred lines ( $t = 6.56$ ,  $df = 14$ ,  $p < 0.001$ ; Figure 6a),  
370 indicating that the fighter morph is recessive to the scrambler morph (Figure 1a). In contrast, no  
371 dominance effects were observed for female fecundity with covariance ( $\sigma_{PF,IF}$ ) not differing between  
372 founder morph treatments ( $t = 1.60$ ,  $df = 14$ ,  $p = 0.131$ ; Figure 6b). Finally, there was no significant  
373 genetic correlation between the array covariances for male morph ( $\sigma_{PM,IM}$ ) and female fecundity ( $\sigma_{PF,IF}$ )  
374 among inbred lines (Pearson's  $r = 0.23$ ,  $p = 0.393$ , Spearman's  $r = 0.23$ ,  $p = 0.391$ , Supplementary Figure  
375 3).

## 376 Discussion

377 Here, using diallel crosses of *R. robini* inbred lines, we investigated the genetic variance components  
378 underlying both female fecundity and the expression of a sexually selected weapon that is dimorphic  
379 among males. Furthermore, we explored the additive genetic correlation between the two traits, as well  
380 as the genetic correlation for the dominance ordinations between the two traits. Our results provide  
381 evidence for the inheritance of the weapon being largely explained by additive genetic variation, with  
382 contributions from symmetric epistatic effects. We detected a significant inbreeding effect on morph  
383 expression, indicating that expression of the fighter phenotype is sensitive to the quantity of exposed

384 deleterious recessives. We also found that fighter-morph alleles tend to be recessive to the scrambler-  
385 morph alleles. Female fecundity, by contrast, only had a very small percentage of variance explained by  
386 additive genetic effects, with much of variance explained by symmetric and asymmetric epistatic effects.  
387 Fecundity also showed very high inbreeding depression, indicating that fecundity is determined by the  
388 quantity of exposed deleterious mutations. Aside from this (likely) polygenic deleterious recessive basis  
389 to both traits, as well as some degree of epistasis underlying both traits, there were no direct  
390 associations between male morph and female fecundity, including no additive genetic correlation and  
391 no evidence of dominance reversal.

392 The considerable additive genetic variation for morph expression detected here supports earlier work  
393 that morph is heritable in *R. robini* (Radwan 1995). Building on this work and, by using inbred lines,  
394 knowing the genotype of both males and females in the current study, we provide evidence that both  
395 sexes appear to contribute equally to the probability of offspring being a fighter or scrambler.  
396 Suggesting that the additive genetic basis to male morph in this species is predominantly due to  
397 autosomal genetic variation. This contrasts a previous study of a con-generic, *R. echinopus*, which found  
398 evidence for paternal morph effects, but overall weaker evidence for additive genetic effects. It was  
399 argued that the former is likely linked to variation on the Y-chromosome or an indirect genetic effect  
400 (Buzatto et al. 2012). While seemingly at odds, the lack of parental effect in the current study can be  
401 explained by differences in sex determination between these two species. *R. echinopus* has been  
402 reported to have XY (Grondziel 1975), whereas *R. robini* has XO (Parrett et al. 2022) sex determination,  
403 the latter obviously eliminating the scope for any Y-linked paternal effects. Furthermore, the two  
404 species show clear differences in their morph determination mode. In *R. echinopus*, as well as another  
405 acarid, *Sancassania berlesei* (Radwan 1993; Michalczyk et al. 2018), fighter morph is suppressed by  
406 pheromones emanating from dense colonies (Radwan 2001), whereas no such type of polyphenism is  
407 observed in *R. robini* (Radwan 1995). Clearly, there is much variation within acarid mites in genetic and

408 environmental contributions to male morph determination, even within the genus *Rhizoglyphus*. The  
409 significant contribution of additive variance found here for *R. robini* is also in line with some earlier work  
410 on this species showing that the proportion of male morph in a population responds to directional  
411 selection (Radwan 2003a; Smallegange and Coulson 2011; Plesnar-Bielak et al. 2014; Parrett et al. 2022).  
412 Our estimate for additive genetic variance of male morph is over an order of magnitude greater than  
413 that for female fecundity – a trait that is often considered an exemplification of a polygenic fitness-  
414 related trait in other taxa, with additive variance maintained predominantly via mutation-selection  
415 balance (Houle 1992, also see below). The very high proportion of additive variance for male morph,  
416 much exceeding dominance variance, suggests that mutation-selection balance is unlikely to be the  
417 main contributing mechanism. Accordingly, some estimates of heritability obtained in earlier work were  
418 close to or exceeded unity (Radwan 1995), which could be due to segregation of a large effect QTL,  
419 although segregation patterns excluded simple Mendelian segregation.

420 Our estimates of dominance relationships are also inconsistent with morph heritability being mostly due  
421 to mutation-selection balance maintaining genetic variance in condition, in turn determining morph  
422 expression (Radwan 1995; Smallegange 2011). This is because the majority of segregating deleterious  
423 mutations, which reduce condition, are expected to be recessive (Charlesworth and Willis 2009). Thus,  
424 the mutation-selection balance hypothesis would not only predict a relatively high proportion of  
425 dominance variance that we did not observe, but would also predict the scrambler associated alleles to  
426 be recessive – whereas the reverse was observed. Outbred values for fighter-founded inbred lines had  
427 considerably higher estimates of covariance with the self-cross value of inbred lines they were  
428 outcrossed to, compared to scrambler-founded inbred lines, suggesting that alleles underlying the  
429 fighter-morph are recessive. This dominance relationship is consistent with the response to divergent  
430 artificial selection of male morph, which led to earlier near-fixation of the fighter-morphs compared to  
431 scrambler-morphs (Parrett et al. 2022). This does not exclude the possibility that exposed deleterious

432 alleles could increase the likelihood of expressing the scrambler phenotype, and indeed, we observed a  
433 negative overall general inbreeding effect for fighter expression, suggesting morph expression is in some  
434 part sensitive to exposed mutational load. Concordantly, Parrett et al. 2022 observed that populations  
435 selected for scramblers males have accumulated a large load of putatively recessive mutations spread  
436 across the genome. Yet, Parrett et al. 2022 also found a few genomic regions that contained particularly  
437 high density of SNPs that differentiated between fighter and scrambler selected populations, and these  
438 regions map to the same linkage group (Chmielewski et al. unpublished data), suggesting the existence  
439 of a supergene or inversion associated with male morph determination. Thus, it appears that male  
440 morph is determined by two overlying mechanisms: (i) the existence of one or more scrambler-  
441 dominant QTL(s) directly influencing the probability (or individuals' 'liability') of morph expression,  
442 possibly residing within a supergene or inversion polymorphism (Parrett et al. 2022), and (ii) male  
443 condition and condition-dependent weapon expression, where fighter phenotype expression is inversely  
444 associated with polygenic deleterious mutation load (Łukasiewicz et al. 2020; Parrett et al. 2022; present  
445 study). Consistent with the latter, manipulating phenotypic condition via food availability and  
446 temperature have been shown to influence weapon expression (Radwan 1995; Smallegange 2011;  
447 Plesnar-Bielak et al. 2018).

448 In contrast to the estimate for male morph, we found very small additive genetic variance in female  
449 fecundity. Earlier work based on daughter-on-mother regression estimated heritability at 27%, but also  
450 showed that it is subject to significant inbreeding depression which is not easily purged and leads to  
451 inbred line extinction (Radwan 2003b). This was interpreted as evidence that heritability of fecundity is  
452 due to a large number of small-effect loci, where it would be hard to purge the deleterious mutation  
453 load on fecundity. Here, we also found a large and significant negative general effect of inbreeding, but  
454 our estimate of additive genetic variance was considerably lower. It should be noted, however, that  
455 additive genetic variance inferred from daughter-on-mother regression ignores epistatic effects (Roff

456 1997), which we found to have a pronounced effect on fecundity variance (22.73% in total). Thus, our  
457 data are consistent with female fecundity being affected by deleterious recessives (with only minor  
458 contribution to additive effects) that interact epistatically. Our data do not provide further insight to the  
459 basis of this epistatic variance in female fecundity, but we note that significant inbreeding depression as  
460 well as large contributions of dominance and epistasis are common features of genetic variance in  
461 fitness-related traits (DeRose and Roff 1999; Roff and Emerson 2006). Our results highlight that epistasis  
462 may considerably inflate the heritability of life-history traits when they are estimated using methods  
463 that ignore it.

464 Finally, we found little to no support for sexual antagonism contributing to the maintenance of  
465 alternative male morphs. We did not find a significant negative additive genetic correlation between  
466 male morph and female fecundity, though the estimate was negative ( $r = -0.18$ ), as predicted under  
467 sexual antagonism. One possibility that could explain why we have not detected that correlation here  
468 despite it being evident in the same inbred lines after four generations of inbreeding (Łukasiewicz et al.  
469 2020) could be that the ten additional generations of inbreeding (see Methods) may have caused the  
470 loss of fighter-founded inbred lines with particularly strong fighter-benefit female-detrimental genetic  
471 variation (analogous to Grieshop et al. 2017). That is, if sexually antagonistic alleles that decrease female  
472 fecundity interacted with recessive deleterious mutations upon inbreeding to cause female infertility  
473 and subsequent loss of inbred lines (see Methods), this may have disproportionately purged fighter-  
474 benefit/female-detriment sexually antagonistic alleles from our panel of inbred lines. Thus affecting our  
475 estimates of sexually antagonistic genetic variance. Indeed, in another system (*Callosobruchus*  
476 *maculatus*), inbred lineage extinction associated with male-benefit/female-detriment sexually  
477 antagonistic allelic variation (Grieshop et al. 2017) was likewise accompanied by a reduced additive  
478 genetic signal of sexual antagonism in the diallel cross among the extant inbred lines (Grieshop and

479 Arnqvist 2018) relative the much stronger additive genetic signal of sexual antagonism seen in that  
480 population prior to the inbreeding regime (Berger et al. 2014).

481 Another possibility is that the 16 inbred lines used here simply did not capture a significant proportion  
482 of segregating morph-specific sexually antagonistic variation present within an outbred population. How  
483 much it is possible extrapolate beyond these 16 inbred lines is therefore in its nature limited, however,  
484 we note that the number of inbred lines used in the current study is equal or greater than many  
485 comparable experiments using diallel crosses (e.g. Buzatto et al. 2012; Lüpold et al. 2016; Grieshop and  
486 Arnqvist 2018; Maurizio et al. 2018; Shorter et al. 2019; Grieshop et al. 2021b), and such limitation did  
487 not prevent Grieshop and Arnqvist (2018) from detecting significant sexual antagonism. In the case of  
488 our experiment, if sexual antagonism was associated with genetic variants underlying male dimorphism  
489 as previously hypothesised (Plesnar-Bielak et al. 2014; Łukasiewicz et al. 2020), these variants should be  
490 present in our sample representing equal numbers of inbred lines derived from fighter and scambler  
491 males. We therefore consider the loss of sexually antagonistic variation during inbreeding as a more  
492 likely explanation of why we have not observed similar morph-specific sexual antagonism reported by  
493 earlier studies.

494 While we might have underestimated the additive signal of sexual antagonism, we still did not find any  
495 evidence for dominance reversal either between male morph and female fecundity, which would help  
496 maintain polymorphisms underlying the two traits under sexually antagonistic balancing selection (see  
497 Reid 2022 for a common mechanism by which dominance reversal could ensue for both major-effect  
498 QTLs and polygenic underpinnings). A presumably polygenic signal of dominance reversal was previously  
499 reported for male and female fitness in seed beetles using a similar quantitative genetic approach as  
500 that used here (Grieshop and Arnqvist 2018), but other methods have revealed dominance reversals for  
501 cases of major-effect QTLs and supergenes (Barson et al. 2015; Pearse et al. 2019). In *R. robini* however,

502 dominance reversals between male morph and female fecundity do not seem to be contributing to the  
503 stable maintenance of polymorphisms underlying genetic variance in male morph.

504 Overall, our study shows high additive genetic variance for the dimorphic expression of a weapon, which  
505 when taken with dominance and inbreeding results strongly suggest two overlaying mechanisms for  
506 morph determination exist. We propose that one (or more) large effect scrambler-dominant QTL(s)  
507 directly influences male morph expression which is simultaneously affected by polygenic condition.  
508 Contrastingly, we did not detect much additive genetic variance for female fecundity, although  
509 considerable epistatic effects were found highlighting models not accounting for epistasis may inflate  
510 estimates of heritability. Our study revealed that the genetic architecture of male morph is very distinct  
511 from that underlying female fecundity, with beneficial dominance reversal unlikely to be contributing to  
512 maintaining polymorphisms for male morph. The maintenance of male polyphenism in *R. robini* remains  
513 to be fully resolved, with complex genetic and environmental effects yet to be fully teased apart.

514

515 **Author contributions:** JR and KG conceived the idea. JR, JMP, AŁ and SC designed experiment. JMP, AŁ,  
516 SC, AS-K and JR performed data collection. JMP, PLM and KG carried out analysis. JMP and JR wrote the  
517 manuscript with input from PLM and KG. All authors read and approved the manuscript.

518 **Acknowledgements:** We would like to thank Mateusz Konczal for useful discussion. We are also grateful  
519 for laboratory assistance from Małgorzata Niškiewicz, Karolina Przesmycka, Issy Bolitho and Martyna  
520 Wilczek. Work from this project was funded by National Science Centre (2017/27/B/NZ8/00077 to JR &  
521 2020/39/D/NZ8/00069 to JMP), Swedish Research Council (2018-06775 to KG) and National Institutes of  
522 Health (F32-AG064883 to PLM).

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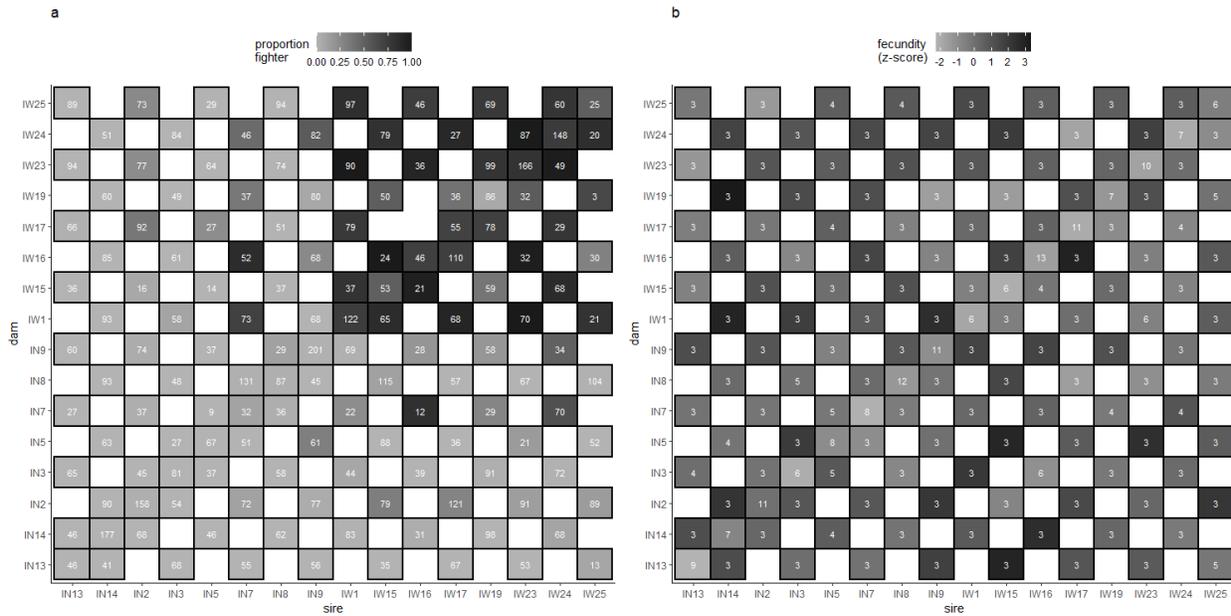
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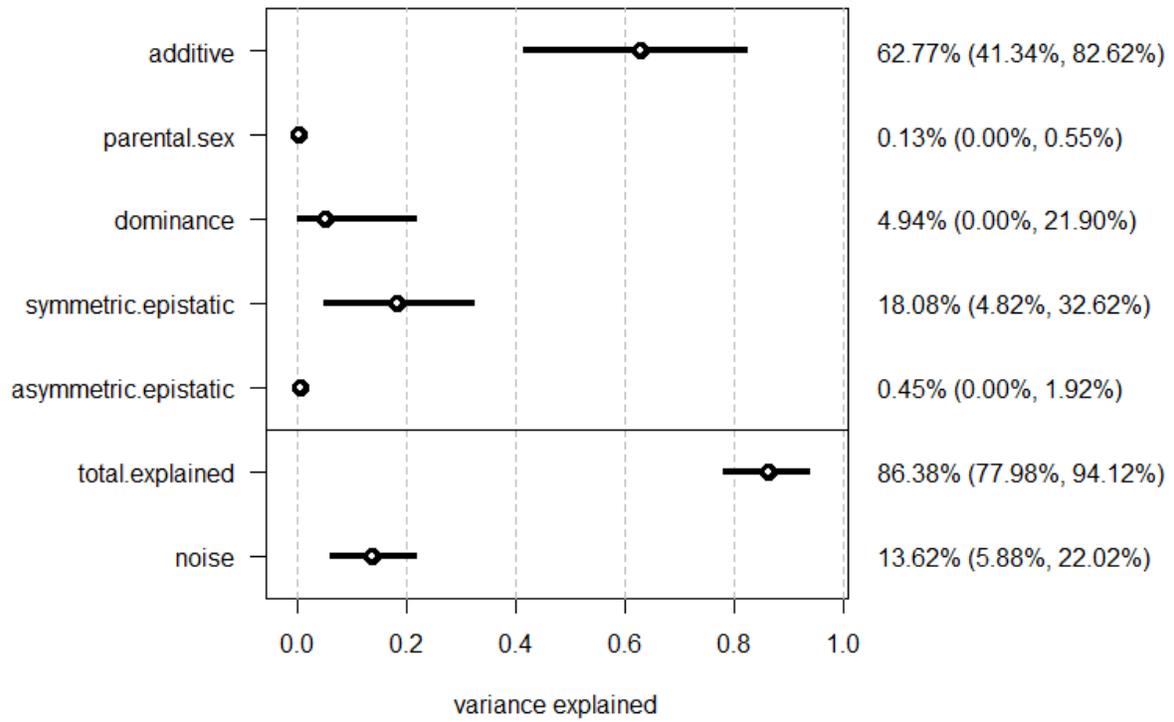
724 **Figures**



725

726 **Figure 1.** Heatmaps of a) morph proportion and b) female fecundity across the diallel with each sire and  
 727 dam cross combination. a) Morph proportion (averaged across replicates), where darker grey indicates  
 728 higher proportion of fighter males in that cross combination. Numbers within each square indicate the  
 729 total number of males from which morph was recorded, with white squares with no numbers indicating  
 730 no data was collected. b) Female fecundity (averaged summed z-scores across replicates) for each cross  
 731 combination, where darker grey indicates higher summed z-score (i.e. fecundity controlled by observer).  
 732 Numbers within each square indicate the total number of females which fecundity was recorded, with  
 733 white squares with no numbers indicating no data was collected. Sire and dam names: IN or IW followed  
 734 by a number provides inbred lines ID and indicate lines founded by a scrambler or fighter male,  
 735 respectively (i.e. IN# = scrambler founded inbred line and IW# = fighter founded inbred line).

736

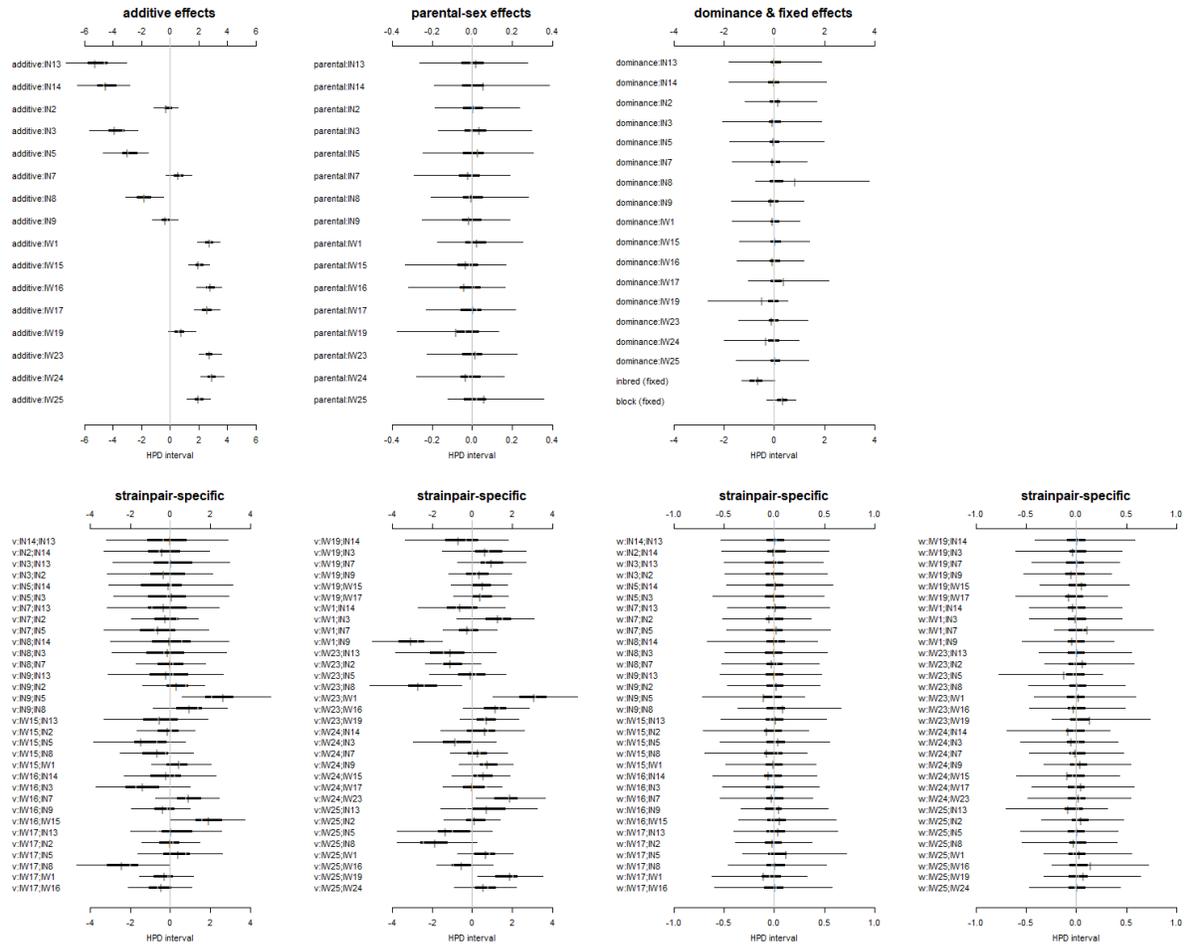


737

738 **Figure 2.** Variance contributions of distinct class effects on morph proportion. Reporting posterior

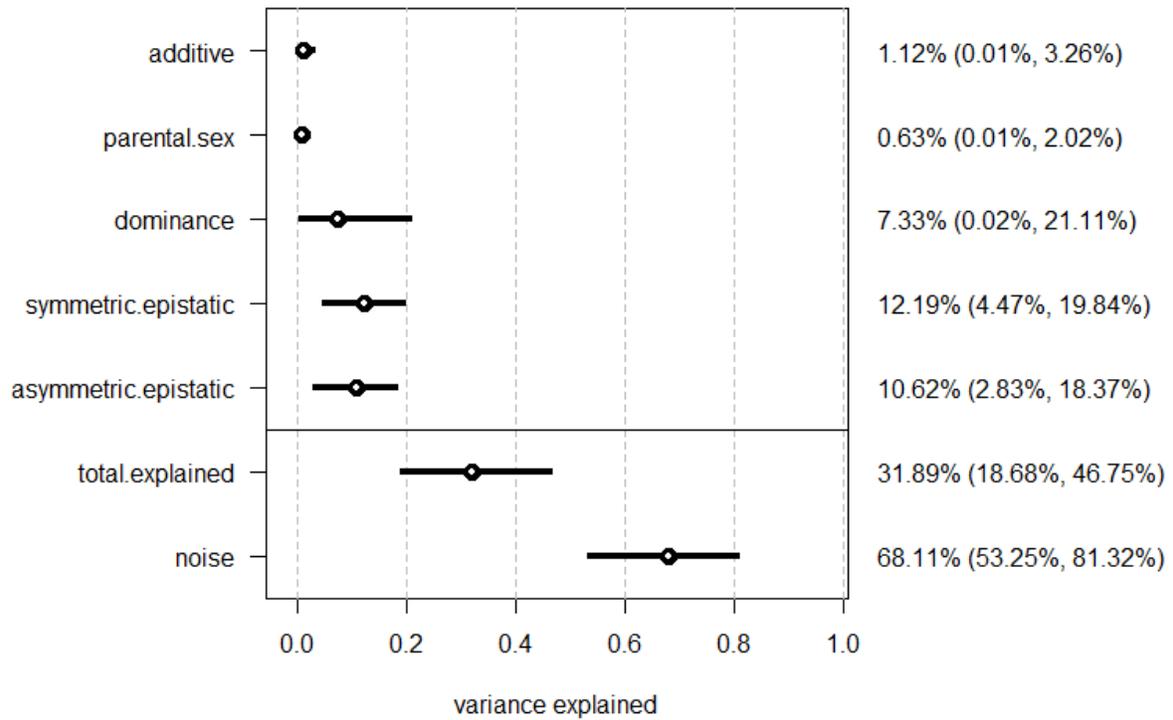
739 means and 95% HPDs of variance projections.

740



741

742 **Figure 3.** Diallele effects on morph proportion of (top row) strain-specific additive, parental sex, and  
 743 dominance effects, also fixed effects of block and main effect of inbreeding, and (bottom row) epistatic  
 744 strainpair-specific effects (labels “v” and “w” respectively refer to symmetric and non-symmetric  
 745 epistatic effects) on morph proportion. Represented for each parameter: thin line: 95% HPD; thick line:  
 746 50% HPD; vertical break: median HPD; dash: mean HPD. The grey vertical line indicate 0, where intervals  
 747 that exclude 0 have non-negligible effects on male morph. Positive values indicate increasing  
 748 contribution to offspring being fighters and negative values there is decreasing contribution of offspring  
 749 being fighter. IN or IW followed by a number provides inbred lines ID and indicate lines founded by a  
 750 scrambler or fighter male, respectively (i.e. IN# = scrambler founded inbred line and IW# = fighter  
 751 founded inbred line).

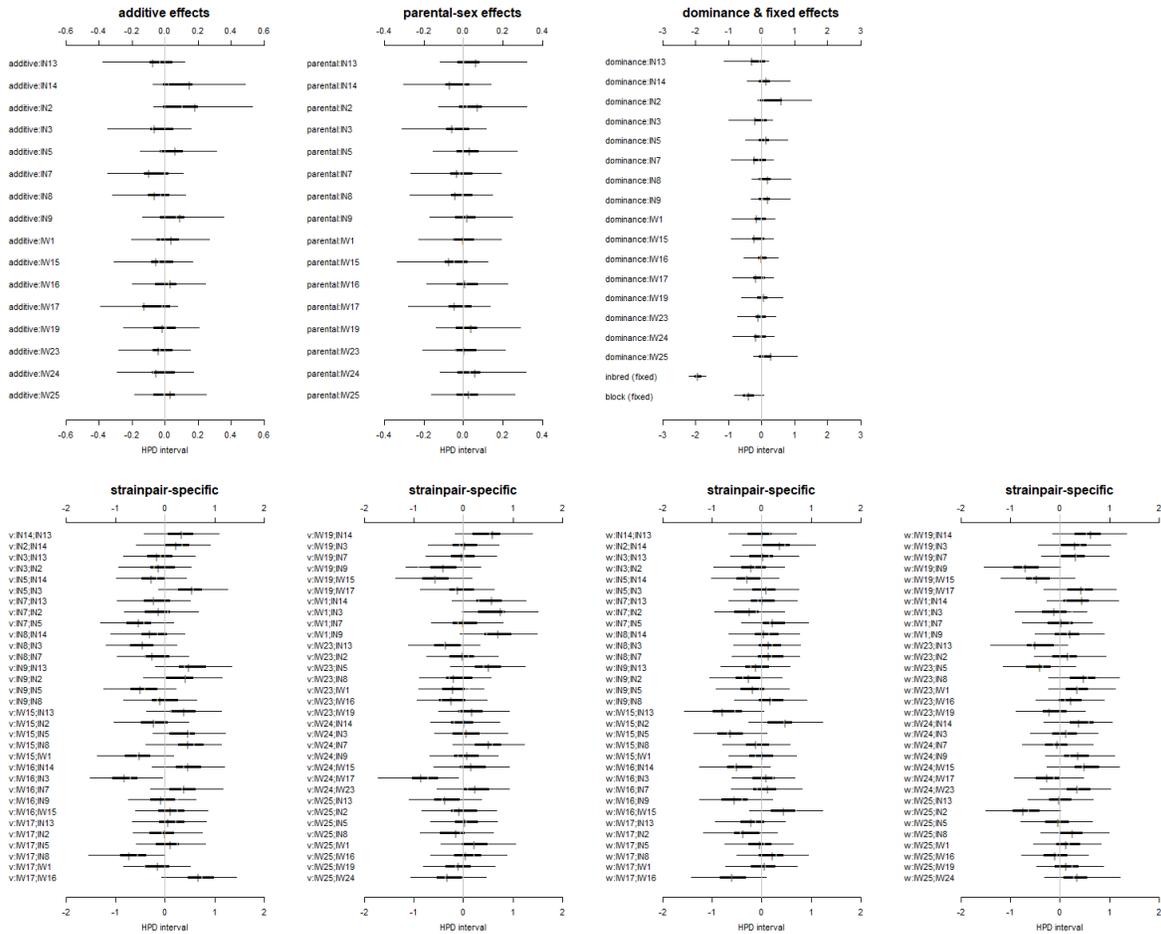


752

753 **Figure 4.** Variance contributions of distinct class effects on female fecundity (z-score). Reporting

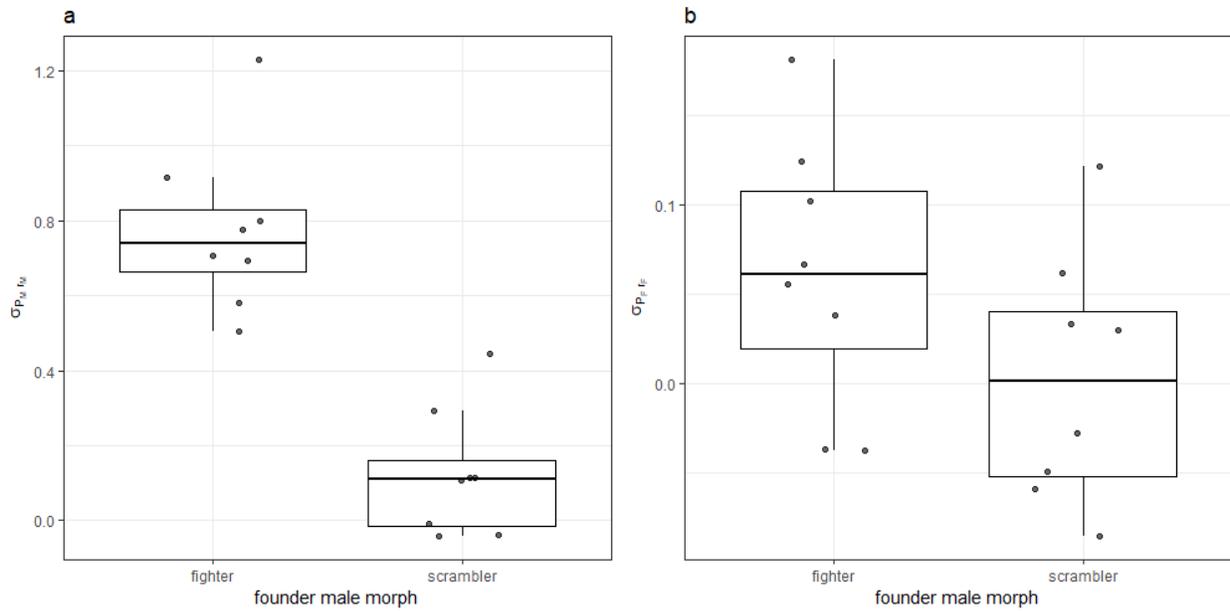
754 posterior means and 95% HPDs of variance projections.

755



756

757 **Figure 5.** Diallel effects on female fecundity (z-score) of (top row) strain-specific additive, parental sex,  
 758 and dominance effects, also fixed effects of block and main effect of inbreeding, and (bottom row)  
 759 epistatic strainpair-specific effects (labels “v” and “w” respectively refer to symmetric and non-  
 760 symmetric epistatic effects) on female fecundity. Represented for each parameter: thin line: 95% HPD;  
 761 thick line: 50% HPD; vertical break: median HPD; dash: mean HPD. The grey vertical line indicate 0,  
 762 where intervals that exclude 0 have non-negligible effects on male morph. Positive values indicate  
 763 increasing contribution to female fecundity and negative values decreasing contribution to female  
 764 fecundity. IN or IW followed by a number provides inbred lines ID and indicate lines founded by a  
 765 scrambler or fighter male, respectively (i.e. IN# = scrambler founded inbred line and IW# = fighter  
 766 founded inbred line).



767

768 **Figure 6.** Estimates of the relative amount of recessive allelic variation for a) morph ( $\sigma_{PM,rM}$ ) and b)  
 769 fecundity ( $\sigma_{PF,rF}$ ) between founder morph treatments. Boxes are composed of the median and hinge  
 770 values (25th and 75th percentiles), with whiskers  $\pm$  interquartile range \* 1.5. Individual points denote  
 771 each inbred lines mean array covariance for male morph and female fecundity (a:  $\sigma_{PM,rM}$ , b:  $\sigma_{PF,rF}$ ).