

1 THE GENETIC ARCHITECTURE OF SEXUAL DIMORPHISM IN THE MOSS CERATODON  
2 PURPUREUS

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21

22 **ABSTRACT**

23 A central problem in evolutionary biology is to identify the forces that maintain genetic variation  
24 for fitness in natural populations. Sexual antagonism, in which selection favors different variants  
25 in males and females, can slow the transit of a polymorphism through a population or can  
26 actively maintain fitness variation. The amount of sexually antagonistic variation to be expected  
27 depends in part on the genetic architecture of sexual dimorphism, about which we know  
28 relatively little. Here, we used a multivariate quantitative genetic approach to examine the  
29 genetic architecture of sexual dimorphism in a scent-based fertilization syndrome of the moss  
30 *Ceratodon purpureus*. We found sexual dimorphism in numerous traits, consistent with a history  
31 of sexually antagonistic selection. The cross-sex genetic correlations ( $r_{mf}$ ) were generally  
32 heterogeneous with many values indistinguishable from zero, which typically suggests that  
33 genetic constraints do not limit the response to sexually antagonistic selection. However, we  
34 detected no differentiation between the female- and male-specific trait (co)variance matrices ( $\mathbf{G}_f$   
35 and  $\mathbf{G}_m$ , respectively), meaning the evolution of sexual dimorphism may be constrained. The  
36 cross-sex cross-trait covariance matrix  $\mathbf{B}$  contained both symmetric and asymmetric elements,  
37 indicating that the response to sexually antagonistic or sexually concordant selection, and the  
38 constraint to sexual dimorphism, is highly dependent on the traits experiencing selection. The  
39 patterns of genetic variances and covariances among these fitness components is consistent  
40 with partly sex-specific genetic architectures having evolved in order to partially resolve  
41 multivariate genetic constraints (i.e. sexual conflict), enabling the sexes to evolve toward their  
42 sex-specific multivariate trait optima.

43

## 44 INTRODUCTION

45 Males and females achieve fitness through different strategies [1–3], which can drive the  
46 evolution of sexual dimorphism [4,5]. The ubiquity of sexual dimorphism suggests that selection  
47 frequently favors different trait optima in males and females. Sexual conflict occurs when an  
48 allelic substitution that increases fitness in one sex decreases fitness in the other, and thus both  
49 sexes are prevented from reaching their respective fitness optimum [6]. Theory and empirical  
50 evidence show that opposing selection in males and females can maintain genetic variation for  
51 fitness [7–15]. However, whether sexual conflict in a population is evolutionarily transient or  
52 persistent will depend on both the nature of sex-specific selection and the nature of sex-specific  
53 genetic architecture for traits [16–20] the latter of which remains poorly understood, especially in  
54 non-model organisms.

55 The simplest means to evaluate the constraint imposed by a shared underlying genetic  
56 architecture for homologous traits between the sexes is to measure the cross-sex genetic  
57 correlation ( $r_{mf}$ ) [6]. A strongly positive  $r_{mf}$  for a trait will cause selection in one sex to generate a  
58 correlated response in the other sex [4,21] precluding the evolution of sexual dimorphism.  
59 Poissant et al. [22] found that half of the estimates of  $r_{mf}$  in 114 studies were above  $\sim 0.8$ ,  
60 indicating that sexual dimorphism may often be constrained by traits having shared genetic  
61 architecture in males and females. Additional evidence for constraint on the evolution of sexual  
62 dimorphism is provided by studies identifying opposing selection gradients on correlated traits  
63 [22,23]. The resolution of sexual conflict can occur by the evolution of sex linkage or various  
64 forms of sex-biased gene expression (sex-specific genetic modifiers, and genomic imprinting)  
65 [4,24–26] and allows differential response to selection in males and females.

66 Single trait analyses, however, fail to account for covariances among traits within and  
67 between the sexes, which are important for predicting the response to selection [21]. The  
68 multivariate constraint to sexual dimorphism is captured by the sex-specific genetic variance-  
69 covariance matrix ( $\mathbf{G}_{mf}$ ), which represents a more complete framework for studying genetic

70 architecture [18,27,28].  $\mathbf{G}_{mf}$  consists of the female- and male-specific submatrices  $\mathbf{G}_f$  and  $\mathbf{G}_m$ ,  
71 respectively, as well as the cross-sex cross-trait covariance matrix,  $\mathbf{B}$  (and its transpose,  $\mathbf{B}^T$ ):

72

$$\mathbf{G}_{mf} = \begin{bmatrix} \mathbf{G}_f & \mathbf{B} \\ \mathbf{B}^T & \mathbf{G}_m \end{bmatrix}. \quad \text{Eq. 1}$$

73

74

75 The diagonals of  $\mathbf{G}_m$  and  $\mathbf{G}_f$  represent the genetic variances of the traits in males and females,  
76 respectively, and the off-diagonals within  $\mathbf{G}_m$  or  $\mathbf{G}_f$  are the sex-specific genetic covariances  
77 between pairs of traits. The within-trait cross-sex covariances along the diagonal of the  $\mathbf{B}$  matrix  
78 can be standardized into estimates of  $r_{mf}$ , while the off-diagonal elements of  $\mathbf{B}$  represent the  
79 cross-sex cross-trait covariances – i.e. covariances between a trait in one sex and a different  
80 trait in the opposite sex. While  $\mathbf{G}_m$  and  $\mathbf{G}_f$  are symmetric matrices,  $\mathbf{B}$  is a square matrix that may  
81 not be symmetrical (i.e.,  $\mathbf{B}$  need not equal  $\mathbf{B}^T$ ). Asymmetries in  $\mathbf{B}$  may play an important role in  
82 the evolution of sexual dimorphism, although the prevalence of such asymmetry is unknown  
83 outside of a few model systems [20,29].

84 The moss *Ceratodon purpureus* is an emerging model for studying sex-specific genetic  
85 architecture. Nearly 60% of moss species have separate males and females, and sexual  
86 dimorphism is common, most notably in the production of volatile organic compounds (VOCs)  
87 [30]. *Ceratodon purpureus* females produce a wider variety and greater quantity of VOCs than  
88 males. In choice experiments with *C. purpureus*, microarthropods, such as mites and springtails,  
89 were more attracted to female than male moss VOCs [29]. Furthermore, co-cultivating mosses  
90 with microarthropods increases moss fertilization success by ~5X [31]. These observations  
91 suggest that mosses and microarthropods are engaged in scent-based fertilization analogous to  
92 pollinator mutualisms in flowering plants. An increase in VOC production may attract more  
93 sperm-dispersing arthropods, enhancing both fertilization and the opportunity for mate choice

94 [32]. In males, however, VOC production may expend resources that could be allocated to other  
95 fitness components (e.g., sperm production). Thus, the evolution of VOC production toward sex-  
96 specific fitness optima could conceivably be limited by genetic covariances between traits,  
97 sexes and trait/sex combinations.

98         The moss system has several technical features that make it an excellent model for sex-  
99 specific quantitative genetic analyses. The dimorphic part of the life cycle is haploid, meaning  
100 there is no dominance component of genetic variation in dimorphic traits. Sex in this system is  
101 determined at meiosis, by the segregation of the U and V sex chromosomes (as opposed to  
102 XY/ZW systems, where sex is determined at fertilization). The diploid sporophyte is always  
103 heterozygous (i.e., UV). This is because only the haploid male gametophytes make sperm, and  
104 only the female gametophytes make eggs – each chromosome is transmitted through only one  
105 sex. At meiosis, spores inheriting a U develop into female haploid gametophytes, while spores  
106 inheriting a V are males [31]. Thus, each sex contains a non-recombining sex-limited  
107 chromosome, meaning that the various asymmetries associated with the sex chromosome  
108 content in XY or ZW systems are absent [33]. Finally, the gametophytes are clonally replicable,  
109 which enables large sample sizes and limits environmental variation, increasing statistical power  
110 to estimate genetic (co)variances.

111         Here, we take advantage of these features to study the genetic architecture of  
112 multivariate sexual dimorphism in a natural population of the moss *C. purpureus*. We estimate  
113  $\mathbf{G}_{mf}$  and explicitly compare the male and female variance-covariance matrices, test for  
114 asymmetry in  $\mathbf{B}$ , and compare the results of single-trait and multi-trait analyses. The cross-sex  
115 correlations were heterogeneous across traits and mostly indistinguishable from zero,  
116 suggesting that the evolution of sexual dimorphism is relatively unconstrained. We detected no  
117 differences between the female and male (co)variance matrices ( $\mathbf{G}_f$  and  $\mathbf{G}_m$ ), suggesting the  
118 sexes are likely to exhibit a similar response to selection. However, this in combination with  
119 asymmetry in the  $\mathbf{B}$  matrix indicates that even sexually concordant selection could generate

120 sexual dimorphism. Nevertheless, **B** also contained symmetric components, suggesting  
121 possible ongoing sexual conflict in the form of lasting, unresolved constraints to the evolution of  
122 further sexual dimorphism.

123

124

## Materials and Methods

### ***Haploid sibling family cultivation***

126 To generate a genetically diverse sample of haplotypes to estimate the phenotypic and  
127 genetic variation in *C. purpureus*, we generated axenic cultures of 45 haploid sibling families  
128 each consisting of a minimum of 3 male and 3 female siblings [34]. These families were  
129 generated from 45 sporophytes collected in Portland, OR, with each sporophyte representing a  
130 single family. This design is analogous to genotyping the sperm from a single male in an XY  
131 system which allows us to compare the underlying genetic architecture of male and female traits  
132 within a family and understand sex specific differences.

133 To establish axenic lines from field-collected plants, we surface-sterilized operculate  
134 sporophytes and created spore solutions following published protocols [35,36]. We plated 100  
135  $\mu\text{L}$  of the spore suspension on BCD media with 0.5 mM ammonium tartrate [37]. We germinated  
136 spores under fluorescent lights (18 hours dark and 6 hours light) and isolated single haplotypes.  
137 We confirmed sex following Norrell et al. [38] and by observing sex structures.

138

### ***Collection of growth, development, morphology, and physiology traits***

140

141 We grew a total of five replicates from 345 genotypes. We grew two replicates in a  
142 greenhouse in Portland, OR. From these plants we collected volatiles at peak sex expression,  
143 as this is when the moss was observed to be most fragrant. Following volatile collection (see  
144 below), we calculated a dry weight, analyzed leaf measurements using automated methods in  
145 ImageJ, and dissected tissue to confirm the presence of sex structures, measure reproductive  
146 effort, and eliminate non-sex expressing profiles.

147 We used the remaining three replicates in a common growth chamber experiment to  
148 survey variation in growth and development. We grew each genotype on BCDA media, following  
149 Burtscher et al.[39]. Starting on day 0 and every 7 days after for 21 days, we collected  
150 measurements of juvenile growth (protonema) and development, including area, perimeter, and  
151 circularity (a measure of how much the growth pattern deviated from a perfect circle ( $C$ ;  
152 Supplemental methods Eq. S1)). Protonemal growth patterns in which the measured perimeter  
153 matched the estimated perimeter (assuming that the measured area was a perfect circle) return  
154  $C = 1$ , while growth patterns with larger measured perimeters (e.g., more star-shaped) return  
155 values  $C < 1$ . Plants with circularity near 1 are largely comprised of chloronema (less mature  
156 cell type). Having a larger perimeter relative to area ( $C < 1$ ) suggests more mature, longer  
157 celled caulonema, and indicates faster maturation. Throughout this manuscript, we refer to  
158 perimeter and circularity of protonemal tissue after 21 days of growth as “juvenile growth” and  
159 “juvenile growth form”, respectively. We also observed the accumulation of mature leafy  
160 gametophores after 21 days, recording the total number of gametophores present. We refer to  
161 the accumulation of gametophores as “mature tissue”.

### 162 ***Collection of volatile organic compounds (VOCs)***

164 We sampled VOC emissions over 9 consecutive days using a proton transfer reaction  
165 time of flight mass spectrometer (PTR-TOF-MS 1000, Ionicon), incorporating a custom  
166 designed sampling apparatus with hydronium ( $H_3O^+$ ) as the primary reagent ion (ESM1 Figure  
167 S1). Prior to VOC collection, we dark-adapted replicates for 12 hours and measured chlorophyll  
168 fluorescence (Opti-Sciences OP5+,Hudson, New Hampshire) to assess overall plant health  
169 and remove stressed plants from the study which could lead to outliers in VOC profiles. For  
170 each replicate we carefully extracted 200 mg (wet weight) of mature gametophore tissue,  
171 removing remnants of soil, BCDA media, and other contaminants. We placed the plant tissue in  
172 5 ml vials with distilled water to avoid dehydrating the plant during static head space

173 accumulation. We placed all sample and blank cuvettes under an LED light source at 1000 PAR  
174 for two hours at 35°C. All 75 masses we report are protonated species; however, we represent  
175 volatile production as the number of different masses produced (“total masses”) and total  
176 concentration of overall volatile production (“total concentration”).

177

## 178 **Estimating the Genetic (Co)variance Matrix**

179 We used a multivariate framework to estimate the extent to which the shared genome  
180 between males and females imposes a constraint on the evolution of sexual dimorphism. All of  
181 these analyses involve analyzing a fitted  $\mathbf{G}_{mf}$ . We fit the genetic (co)variance matrix,  $\mathbf{G}_{mf}$ , as a  
182 random effect in a general linear mixed-effects model (GLMM) using Bayesian Markov chain  
183 Monte Carlo (MCMC) simulations in the package ‘MCMCglmm’ (v. 2.29, [40]). We fit two models  
184 to estimate  $\mathbf{G}_{mf}$ : one for growth and development traits and another representing morphology  
185 and physiology traits. Our model for growth and development traits included juvenile growth,  
186 juvenile growth form, and mature tissue, while the model for morphology and physiology traits  
187 included total masses produced, total concentration across all masses, relative reproductive  
188 effort, and leaf length. We fit two models because traits were collected on plants grown in  
189 different environments (growth chamber vs greenhouse) and at different stages. Thus, the  
190 categories of traits are arbitrary and titles for each model are simply for convenience. All traits in  
191 both models were zero-centered and variance-standardized across sexes. To account for sex  
192 specific reproductive strategies, reproductive effort was first divided by the sex-specific means  
193 (i.e., transformed to relative reproductive effort) and then zero centered and variance  
194 standardized across the sexes. Total concentration was calculated by first dividing each of the  
195 75 detected masses by their respective means, summing the concentrations for each  
196 observation, and log transforming this sum. We used MCMCglmm()’s ‘trait’ function to identify  
197 our multivariate list of traits in the response variable as a fixed effect (trait), which we interacted

198 with the fixed effect of 'sex' (trait:sex) to estimate the degree of sexual dimorphism for each trait,  
199 making the full GLMM:  
200

$$y = \text{trait-1} + \text{trait:sex} + \mathbf{G}_{\text{mf}} + \text{sampleID} + q + e \quad (\text{Eq. 1})$$

201  
202 where  $y$  is a phenotypic vector of the traits, trait-1 indicates a model fit without an intercept,  $\mathbf{G}_{\text{mf}}$   
203 was estimated over the 45 haploid sibling families ('famid'), sampleID is the random effect of  
204 clonal replicate,  $q$  is an additional random effect (see below), and  $e$  is the unexplained residual  
205 variance (a Gaussian error structure was assumed for all traits). The best fitting model (as  
206 inferred by DIC comparisons; see below) for growth and development was a 3-trait ( $6 \times 6 \mathbf{G}_{\text{mf}}$ )  
207 where  $q$  was 'plate', while the best fitting model for morphology and physiology was a 4-trait  
208 ( $8 \times 8 \mathbf{G}_{\text{mf}}$ ) where  $q$  was 'date'. We modeled (co)variances using the following random effects  
209 structure of MCMCglmm: random = ~us(trait:sex):famid. Residual covariances were fixed to  
210 zero (rcov = ~idh(trait:sex):units), as male and female measures were made on separate  
211 individuals.

212 We used parameter expanded priors (as in Grieshop et al. [41]) for the growth and  
213 development model and inverse-Gamma priors (as in Puentes et al. [42]) for the morphology  
214 and physiology model. To determine the robustness of the posterior distribution to the prior  
215 [43,44] we compared models to other priors. The joint posterior distribution was estimated from  
216 1,000,000 MCMC iterations after a burn-in period of 5,000 iterations, and every 1,000<sup>th</sup> posterior  
217 estimate was stored – providing 1,000 uncorrelated posterior estimates for downstream  $\mathbf{G}_{\text{mf}}$   
218 analyses. Model convergence was assessed using Gelman and Rubin diagnostics [45] and  
219 through visual inspection.

220 Because variance estimates of  $\mathbf{G}$  matrices are bounded by zero, we evaluated whether  
221 (sex-specific) genetic variances were significantly different from zero via univariate model  
222 comparisons. All univariate models were fit using the inverse-Gamma priors while keeping all  
223 else equal to the respective multivariate models. Sex-specific genetic variance was detected as  
224 a delta DIC of 2 or more [46] between models with and without the “sex” term in the random  
225 effect of  $\mathbf{G}_{mf}$  (making it simply  $\mathbf{G}$ ), and genetic variance was detected in the same way by  
226 comparing models with and without  $\mathbf{G}$  (ESM2 table S1). We conducted all statistical analyses  
227 using R (version 4.0.2; R Development Core Team 2020).

228

## 229 **Descriptive statistics**

230 Sex specific genetic variances, intersexual genetic correlations ( $r_{mf}$ ), and sexual  
231 dimorphisms for each trait were estimated directly by our MCMC model. Male and female  
232 genetic variances were estimated on the diagonal of the two sex-specific sub matrices  $\mathbf{G}_f$  and  
233  $\mathbf{G}_m$  – we report the highest posterior density (HPD) mean estimates with upper and lower 95%  
234 HPD intervals as credibility intervals (CIs) in table 1. The cross-sex genetic correlations for  
235 traits,  $r_{mf}$ , were estimated along the diagonal of the *correlation* matrix for  $\mathbf{B}$  (i.e., the  
236 standardized covariances, which are estimated directly by `MCMCglmm()`) – we report the HPD  
237 mode  $r_{mf}$  estimates with upper and lower 95% CIs (table 1). If  $r_{mf} = 1$ , it means that selection  
238 acting to increase a trait value in one sex would cause a correlated response of that same trait  
239 in the opposite sex – i.e. response to selection would be constrained. Consequently, an  $r_{mf}$  of  
240 zero would enable that trait to respond to sex-specific selection with no effect in the other sex.  
241 Lastly, we report the sign (male – female) and magnitude of sexual dimorphism for each trait as  
242 the HPD means and CIs for the estimated fixed effect trait:sex, with p-values provided by  
243 `MCMCglmm()` (table 1).

244

245 **Similarity between  $\mathbf{G}_f$  and  $\mathbf{G}_m$**

246 To compare the size, shape, and orientation of  $\mathbf{G}_f$  and  $\mathbf{G}_m$ , we calculate Hansen's  
247 difference  $d$  [19] and a simplified version of the eigentensor comparison [47,48]. Hansen's  $d$   
248 estimates the average distance between endpoints of response vectors generated from random  
249 selection gradients on the  $\mathbf{G}_f$  and  $\mathbf{G}_m$  matrices [19], similar to a random skewers method [49].  
250 An eigentensor analysis [50,51] comparing two symmetric matrices reduces to a simple  
251 difference between the matrices. Thus, we obtained an estimate of the difference between  $\mathbf{G}_f$   
252 and  $\mathbf{G}_m$  by taking the difference between the 1,000 paired posterior estimates of  $\mathbf{G}_f$  and  $\mathbf{G}_m$  and  
253 calculating the trace (sum of the eigenvalues) of this difference matrix. We report the HPD mode  
254 and 95% CIs of that trace. A test of the significance of this difference was obtained by  
255 comparison to that of a null distribution, which was generated by randomly swapping the sex  
256 labels of the 1,000 paired  $\mathbf{G}_m$  and  $\mathbf{G}_f$  estimates. With the mode of these null estimates being  
257 very near zero and the true estimate being positive, the two-tailed p-value is simply the  
258 proportion the 1,000 posterior estimates of the true difference that were < their respective null  
259 estimates of the difference, times two [41]. The eigentensor comparison of  $\mathbf{G}_f$  and  $\mathbf{G}_m$  provided  
260 qualitatively similar results (see ESM3 figure S2).

261

262 **Symmetry of  $\mathbf{B}$**

263 Asymmetry in the  $\mathbf{B}$  matrix indicates differences in the underlying genetic architecture for  
264 traits between the males and females [50,51]. For example, an off-diagonal element of  $\mathbf{B}$  with a  
265 covariance of 1 between trait  $i$  in males and trait  $j$  in females would suggest that selection on  
266 trait  $i$  in males would cause a correlated response to trait  $j$  in females. Asymmetry in  $\mathbf{B}$  means  
267 that selection on trait " $i$ " in females will produce a correlated response on trait " $j$ " in males, but  
268 that correlated response differs if the sexes are reversed – i.e., selection on trait  $i$  in males  
269 produces a different correlated response in females. Thus, the relative proportion of  $\mathbf{B}$  that is  
270 symmetric versus asymmetric reveals the relative magnitude of cross-sex cross-trait pleiotropic

271 constraints versus sex-specific genetic architecture, respectively. Thus, we partitioned **B** into its  
272 symmetric and asymmetric (or skew symmetric) components using matrix decomposition  
273 [29,52]. Any square matrix - **A** (e.g. **B**) - is the summation of the two components **S** and **N**:  
274

$$\mathbf{A} = \mathbf{S} + \mathbf{N} \quad (\text{Eq. 3})$$

275 the symmetric and asymmetric components, respectively, where  $\mathbf{S} = \frac{1}{2}(\mathbf{A} + \mathbf{A}^T)$  and  $\mathbf{N} = \frac{1}{2}(\mathbf{A} -$   
276  $\mathbf{A}^T)$ . The proportions of **B** that are symmetric and asymmetric are given by the ratio of the sums  
277 of squares of those components to that of the total, **B** [51,52]. We report the HPD mode and  
278 95% CIs for these proportions by resampling them from the 1,000 stored posterior estimates of  
279 **B**.

280

### 281 **Antagonistic and concordant genetic variation**

282 To evaluate the relative proportion of genetic variation in this population that would  
283 respond to sexually concordant versus sexually antagonistic selection, we estimated the matrix  
284  $\mathbf{G}_{ca}$ , following Sztepanacz and Houle [52]. The submatrices of  $\mathbf{G}_{ca}$ ,  $\mathbf{G}_a$  and  $\mathbf{G}_c$  predict the  
285 response of the sex difference in trait values to sexually antagonistic selection, and the  
286 response of trait means to sexually concordant selection, respectively. We projected  $\mathbf{G}_{mf}$  onto a  
287 set of arbitrary orthonormal vectors ( $\mathbf{S}_m$ ) that spanned the concordant and antagonistic  
288 subspaces of  $\mathbf{G}_{mf}$ . If an n-trait  $\mathbf{G}_{mf}$  has 2n dimensionality (e.g. 8 in the case of the 4-trait  
289 morphology and physiology matrix), then  $\mathbf{S}_m$  was constructed by first taking the set of n  
290 eigenvectors that span the space of an n-dimensional identity matrix, dividing them (arbitrarily)  
291 by the square root of two (giving  $\mathbf{E}_m$ ), and arranging them into the following 2n-dimensional  
292 matrix:  $\mathbf{S}_m = \begin{bmatrix} \mathbf{E}_m & \mathbf{E}_m \\ \mathbf{E}_m & -\mathbf{E}_m \end{bmatrix}$ . The unit-length vectors of the first n columns of  $\mathbf{S}_m$  therefore span the

293 sexually concordant subspace of  $\mathbf{G}_{mf}$  and the unit-length vectors of the second  $n$  columns of  $\mathbf{S}_m$   
294 span the sexually antagonistic subspace of  $\mathbf{G}_{mf}$  [52].  $\mathbf{G}_{mf}$  was projected onto this space:

$$\mathbf{G}_{ca} = \mathbf{S}_m^T \mathbf{G}_{mf} \mathbf{S}_m, \quad (\text{Eq. 4})$$

295 where the upper-left and bottom-right  $n$ -dimensional submatrices of  $\mathbf{G}_{ca}$  are covariance matrices  
296 that represent the sexually concordant ( $\mathbf{G}_c$ ) and sexually antagonistic ( $\mathbf{G}_a$ ) subspaces of  $\mathbf{G}_{mf}$ ,  
297 respectively [52]. The proportion of  $\mathbf{G}_{mf}$  that is sexually concordant and sexually antagonistic is  
298 therefore given by the ratio of the trace of  $\mathbf{G}_c$  to  $\mathbf{G}_{mf}$  and  $\mathbf{G}_a$  to  $\mathbf{G}_{mf}$ , respectively [52]. Again, we  
299 report the HPD mode and 95% CIs for these overall proportions, as well as for each eigenvector  
300 of  $\mathbf{G}_{mf}$ ,  $\mathbf{G}_c$  and  $\mathbf{G}_a$ , by resampling the 1,000 stored posterior estimates of  $\mathbf{G}_{mf}$ .

301

## 302 RESULTS

### 303 Sex-specific genetic variances, $r_{mf}$ , and sexual dimorphism

304 We found that leaf length and total masses were sexually dimorphic in our multivariate  
305 models. The sign (male - female) and magnitude of sexual dimorphism for each trait are  
306 reported as the HPD means and CIs estimated by the trait:sex fixed effect (table 1). We  
307 identified non-zero genetic variance in all traits, and non-zero sex-specific genetic variance in all  
308 traits except leaf length (ESM2 table S1). Male and female genetic variances were estimated on  
309 the diagonal of the two sex-specific sub matrices  $\mathbf{G}_f$  and  $\mathbf{G}_m$  – we report the HPD mean  
310 estimates and 95% CIs in table 1. The magnitude of sex-specific genetic variances ranged from  
311 0.1 to 0.2 in growth and development and 0.001 to 0.1 in morphology and physiology (table 1).  
312 Many of our estimated genetic covariances were strong but accompanied by large uncertainties  
313 (ESM4 figure S4, S6) which is not uncommon [40]. Juvenile growth form and leaf length had  
314 positive  $r_{mf}$  estimates with CIs that did not include zero (table 1).

315

## 316 **Comparing $\mathbf{G}_m$ and $\mathbf{G}_f$**

317 We used two methods to assess the overall similarity between the male and female  
318 (co)variance sub-matrices  $\mathbf{G}_m$  and  $\mathbf{G}_f$ . Hansen's difference  $d$  indicated that there were broadly  
319 no differences between  $\mathbf{G}_m$  and  $\mathbf{G}_f$  in terms of their multidimensional size, shape or orientation  
320 for growth and development traits ( $d = 0.094$ , CIs: -0.043, 0.228) or morphology and physiology  
321 traits ( $d = 0.062$ , CIs: -0.005, 0.129) (figure 1, table 2). The simplified eigentensor analysis (as  
322 well as the formal version, ESM3 figure S2) showed that  $\mathbf{G}_m$  and  $\mathbf{G}_f$  were similar for both growth  
323 and development traits (difference = -0.173, CIs: -0.544, 0.121,  $p = 0.284$ ) and morphology and  
324 physiology traits (difference = -0.073, CIs: -0.269, 0.091,  $p = 0.24$ ) (figure 1, table 2).

325

## 326 **Analyzing $\mathbf{B}$**

327 We estimated symmetry and asymmetry in the  $\mathbf{B}$  matrix by comparing the off-diagonal  
328 elements. Across growth and development traits, the proportion of the  $\mathbf{B}$  matrix that was  
329 asymmetric was 0.112 (CIs: 0.002, 0.448) and the proportion that was symmetric was 0.884  
330 (CIs: 0.552, 0.998) (figure 1A, table 2, ESM4 figure S3,S4). Across morphology and physiology  
331 measurements, the proportion of the  $\mathbf{B}$  matrix that was asymmetric was 0.312 (CIs: 0.064,  
332 0.513) and the proportion that was symmetric was 0.688 (CIs: 0.487, 0.936) (figure 1B, table 2,  
333 ESM4 figure S5,S6).

334

## 335 **Concordant and antagonistic subspace of $\mathbf{G}_{mf}$**

336 For growth and development traits, proportionally 0.367 (CIs: 0.248, 0.476) of the total  
337 genetic variances laid within the antagonistic subspace while proportionally 0.633 (CIs: 0.524,  
338 0.752) of the total genetic variances laid within the concordant subspace (table 2). For  
339 morphology and physiology traits, 0.241 (CIs: 0.121, 0.466) of the total genetic variances laid  
340 within the antagonistic subspace while 0.759 (CIs: 0.534, 0.879) laid within concordance  
341 subspace (table 2).

342 We plot the genetic variances for the eigenvectors of the concordant ( $\mathbf{G}_C$ ) and  
343 antagonistic ( $\mathbf{G}_A$ ) subspaces alongside that of  $\mathbf{G}_{mf}$  for both growth and development traits and  
344 morphology and physiology traits in figure 2. For the growth and development traits, the genetic  
345 variances of the first two out of six ( $1/3^{\text{rd}}$  of the) eigenvectors of  $\mathbf{G}_{mf}$  were fully accounted for by  
346 sexually concordant genetic variance (i.e. the first two eigenvectors of  $\mathbf{G}_C$ ), and the third  
347 eigenvectors of  $\mathbf{G}_{mf}$  was only partly explained by sexually concordant genetic variance (figure  
348 2A). The remaining unexplained genetic variances in  $\mathbf{G}_{mf}$ 's third eigenvector is apparently  
349 sexually antagonistic, as indicated by the overabundance of genetic variance in the first  
350 eigenvector of  $\mathbf{G}_A$  relative to the fourth eigenvector of  $\mathbf{G}_{mf}$ , and so on. By contrast, for the  
351 morphology and physiology traits only the first one out of eight ( $1/8^{\text{th}}$  of the) eigenvectors of  $\mathbf{G}_{mf}$   
352 were fully accounted for by sexually concordant genetic variance (i.e. the first eigenvectors of  
353  $\mathbf{G}_C$ ), and all remaining eigenvectors of  $\mathbf{G}_{mf}$  had some fraction of their genetic variances  
354 comprised of SA genetic variance ( $\mathbf{G}_A$ ; figure 2B).

355

## 356 **DISCUSSION**

357 Mosses engage in scent-based fertilization in which female plants use specific VOCs to  
358 attract sperm-dispersing microarthropods, thereby increasing sexual reproduction [30–32]. Male  
359 mosses, in contrast, appear to produce fewer compounds, and in lower abundances, suggesting  
360 that VOC production may undergo sexually dimorphic selection [30,31]. Here, we used a  
361 multivariate approach based on field-collected, natural crosses to estimate the genetic  
362 architecture of variation in VOC production and life history traits in the moss *C. purpureus*. The  
363 study population contained genetic variance for all traits, consistent with previous studies of life  
364 history traits in other populations [34,53]. We found clear evidence for sexual dimorphism in the  
365 total number of masses produced and leaf length. Most traits have cross-sex correlations that  
366 were indistinguishable from zero, which would suggest that selection on one sex would elicit at  
367 most a modest response in the other sex. However, both Hansen's  $d$  and the simplified

368 eigentensor analysis showed that the multi-trait genetic (co)variance matrices,  $\mathbf{G}_f$  and  $\mathbf{G}_m$ , were  
369 aligned, which would intuitively suggest that the multivariate pleiotropic constraints to the  
370 response to selection would be shared between the sexes. Still, the cross-trait cross-sex genetic  
371 (co)variance matrix ( $\mathbf{B}$ ) had asymmetric elements, indicating some opportunity for sex-limited  
372 responses to selection in spite of the putative multivariate genetic constraints indicated by the  
373 similarity between  $\mathbf{G}_f$  and  $\mathbf{G}_m$ .

374         The constraint on the continued evolution of sexual dimorphism is typically evaluated by  
375 estimating the cross-sex correlations ( $r_{mf}$ ) between homologous traits, and indeed the overall  
376 mixed  $r_{mf}$  values we found here are consistent with estimates from other populations of *C.*  
377 *purpureus* [50]. We found no relationship between  $r_{mf}$  and sexual dimorphism further supporting  
378 the inadequacy of  $r_{mf}$  as a metric of constraint. For example, total masses was sexually  
379 dimorphic but had a nearly zero  $r_{mf}$  while leaf length was similarly dimorphic and had a high non-  
380 zero  $r_{mf}$  (table 1). Additionally, juvenile growth form was not sexually dimorphic yet had a high  
381 non-zero  $r_{mf}$ . In other populations of *C. purpureus*, McDaniel [34] found a different relationship  
382 between dimorphism and  $r_{mf}$ , suggesting that this relationship may be highly population  
383 dependent. While diploid organisms may resolve constraints to sexual dimorphism via sex-  
384 specific dominance effects [14,54,55], conflict resolution in this haploid moss may be limited to  
385 alternative mechanisms such as sex-linkage or sex-chromosome mediated gene regulation. We  
386 suspect that a key factor explaining the mix of  $r_{mf}$  values in *C. purpureus* is the fact that females  
387 and males each have a large sex-limited chromosome (U: 3,450 genes and V: 3,411 genes,  
388 respectively) [56], where the U is passed from mother to daughter and the V from father to son,  
389 which could enable rapid resolution to sexual conflict. If so, this could mean that U- or V-linked  
390 variants may represent evolutionary changes aimed at resolving autosomal sexual conflict.

391         It is widely appreciated that single trait analyses, like  $r_{mf}$  may fail to capture the true  
392 underlying constraint on the evolution of sexual dimorphism. Indeed, estimates showing that  
393 male and female genetic (co)variance matrices are similar suggest that the response to

394 selection of one sex could be quite similar in the other in spite of the low cross-sex correlations  
395 for individual homologous traits. Similar to findings in other studies [50,52,57–59], we found that  
396 the overall genetic (co)variance structure was similar between males and females (table 2).  
397 Despite similar sex specific covariance matrices, there are some observable differences,  
398 including the negative covariance of leaf length and total masses in males but not females, and  
399 reproductive effort and leaf length positively covary in females but not in males (figure 1). Many  
400 of the most differentiated covariances involved leaf traits and relative reproductive effort with  
401 VOC production in mature plants. The fact that many traits show cross-trait covariances that are  
402 sexually dimorphic suggests that genetic control is both highly pleiotropic (between traits) and  
403 potentially involves strong epistatic interactions with loci on the U and V sex chromosomes. In  
404 addition, this suggests that similar patterns of selection acting on males or females could  
405 generate different phenotypic responses, potentially increasing or decreasing the population-  
406 level sexual dimorphism.

407 Intuitively, it would make sense that similarity between  $\mathbf{G}_f$  and  $\mathbf{G}_m$  would impose genetic  
408 constraint. However, Cheng and Houle [20] demonstrated that similarity in male and female  
409 covariance matrices coupled with some degree of  $\mathbf{B}$  matrix asymmetry suggests a greater  
410 opportunity for sexual dimorphism in response to sexually concordant selection than to sexually  
411 antagonistic selection. Thus, our estimates of the proportion of standing genetic variation that  
412 could respond to sexually antagonistic selection represent lower bounds for the potential  
413 sexually dimorphic response, as further sexual dimorphism could evolve in response to sexually  
414 concordant selection. We therefore base our findings regarding multivariate genetic constraint  
415 on the estimated proportions of asymmetry and symmetry on our  $\mathbf{B}$  matrix analysis [51,52].

416 Though  $\mathbf{B}$  was largely symmetrical, indicating multivariate constraints to sexual  
417 dimorphism, a portion of the  $\mathbf{B}$  matrix was asymmetric in both trait categories (growth and  
418 development and morphology and physiology). If the  $\mathbf{B}$  matrix were completely symmetrical, the  
419 response to selection on males would be manifest in both the male and female offspring of the

420 following generation. By contrast, asymmetry in the off diagonals of the **B** matrix means that the  
421 multivariate responses to selection between males and females can be different [29,50,59,60].  
422 The asymmetry in **B** likely results from sex-biased gene regulation mediated by epistatic  
423 interactions between autosomal variants and the U and V sex chromosomes (possibly also  
424 mediated by epigenetic factors; see Wang et al. [61]). There seems to be at least a putative  
425 difference between the growth and development traits and the morphology physiology traits in  
426 the degree of **B** asymmetry (table 2), which is also visually apparent in figure 1. The levels of **B**  
427 asymmetry that we find in the growth and development traits and morphology physiology traits  
428 is toward the lower and upper end, respectively, of the range of estimates among populations of  
429 *Drosophila serrata* [51], which ranged from ~15-30% (table 2). This possibly suggests a richer  
430 history of sex-specific and/or sexually antagonistic selection in morphology and physiology traits  
431 relative to growth and development traits, triggering the evolution of resolved genetic  
432 constraints.

433 An analysis of the degree of multivariate sexually antagonistic genetic variation in  $\mathbf{G}_{mf}$   
434 provides insight to the capacity for further response to sexually antagonistic selection [20,52].  
435 The overall percentages of sexually antagonistic genetic variance were estimated with wide,  
436 highly overlapping CIs between our two trait categories (table 2). However, the eigenvector-  
437 specific analysis showed a greater proportion of sexually antagonistic genetic variance  
438 comprising the eigenvectors of  $\mathbf{G}_{mf}$  in morphology and physiology traits relative to the growth  
439 and development traits. Further, that sexually antagonistic genetic variance was dispersed  
440 across proportionally more of the eigenvectors relative to that exhibited by the growth and  
441 development traits (figure 2). Indeed, 25-35% of the multivariate genetic variance in our  
442 population was sexually antagonistic (table 2), considerably more than, for example, the  
443 multivariate genetic architecture of wing morphology in *D. melanogaster* (4.32% sexually  
444 antagonistic genetic variance [52]). Thus, our morphology and physiology traits may possess a  
445 greater opportunity to respond to sexually antagonistic selection than the growth and

446 development traits, echoing the greater proportion of the **B** matrix that was found to be  
447 asymmetric relative to that of growth and development traits (figure 1, table 2).

448         The rich bouquet of VOCs produced by this population may contribute to variation in  
449 attracting sperm-dispersing arthropods, with potentially major fitness consequences. Both  
450 females and males contain genetic variation for VOC production, but the structure of covariation  
451 in the sexes is sufficiently different such that sex-specific coevolution between the moss scents  
452 and arthropod behaviors could play a major role in the maintenance of genetic variation for  
453 fitness in natural populations of *C. purpureus*. The complexity of the underlying genetic  
454 architecture also highlights the potential for scent-based fertilization to contribute to pre-zygotic  
455 speciation barriers in mosses, much like the role pollination plays in angiosperms. For example,  
456 mosses may evolve suites of VOCs which match the preferences of the local mesofauna. Odor-  
457 mediated fertilization could promote the evolution of pre-zygotic isolation if moss VOCs elicit  
458 species-specific responses from sperm-dispersing microarthropods or other members of these  
459 communities. It is possible that the interaction involves additional microbial partners upon which  
460 the mesofauna feed – indeed, mosses appear to host diverse sex- and species-specific  
461 microbiomes [62–64]. Collectively these results highlight how ecological interactions may shape  
462 the evolution of sexual dimorphism [65,66], which may in turn contribute to the maintenance of  
463 genetic variation in fitness and the evolution of reproductive isolation.

464

#### 465 **Data accessibility**

466 Data and scripts to reproduce the results of the study are available on the Dryad Repository:  
467 <https://doi.org/10.5061/dryad.59zw3r266>.

468

#### 469 **Contributions**

470 L.M.K. led the study. L.M.K, T.N.R, and S.F.M designed the study. L.M.K. collected the data,  
471 with assistance from T.N.C., T.K., A.J.J., D.N.S., and C.T.C. for the life history traits, and E.T.G.  
472 and S.K. for the PTR-TOF-MS data. L.M.K. and K.G. performed the statistical analyses where

473 K.G. supervised statistical analyses and interpretation. L.M.K. and S.F.M. wrote the manuscript,  
474 E.T.G. and K.G. contributed to writing the methods and K.G. contributed to writing results and  
475 editing the manuscript.

476  
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490  
491 **Figure Captions**

492 **Figure 1.** Genetic correlations (Gmf) among traits within and between males and females  
493 represented by ellipses. A narrow ellipse is representative of a stronger correlation while a wider  
494 ellipse depicts a weaker correlation. A represents the genetic correlations between growth and  
495 developmental traits whereas B represents the correlations between morphology and  
496 physiology.

497

498 **Figure 2.** A comparison of the genetic variance of Gmf against the concordant and antagonistic  
499 subspaces. The height of each bar represents the estimated genetic variance for each  
500 eigenvector while the error bars show the 95% HPD. Plot A (6 dimensions) represents the  
501 growth and development traits, and plot B (8 dimensions) represents the morphology and  
502 physiology traits.

503

504 **Table 1.** Estimates of sex specific genetic variance and associated 95% HPD intervals and  
505 cross- sex correlations (rmf) and associated 95% HPD intervals. The degree sexual dimorphism  
506 was calculated as the difference between point estimates of male and female posterior means  
507 (male – female). A negative value for sexual dimorphism suggests the females have a larger  
508 posterior mean. All traits with an “\*\*” are sexually dimorphic ( $p < 0.05$ ).

509

510 **Table 2.** Summary table with estimates and corresponding 95% HPD intervals and p- values  
511 where applicable. Estimates include comparisons between Gm and Gf (Hansen’s difference d  
512 and simplified eigentensor analysis), asymmetry and symmetry of B, and proportion of  
513 antagonistic and concordant subspace relative to the total genetic variance in Gmf.

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