



1 Topographic Control of Southern Ocean Gyres and the Antarctic

2 Circumpolar Current: A Barotropic Perspective

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ABSTRACT

18 In the Southern Ocean the Antarctic Circumpolar Current is significantly
19 steered by large topographic features, and sub-polar gyres form in their lee.
20 The geometry of topographic features in the Southern Ocean is highly vari-
21 able, but the influence of this variation on the large-scale flow is poorly un-
22 derstood. Using idealised barotropic simulations of a zonal channel with a
23 meridional ridge, it is found that the ridge geometry is important for deter-
24 mining the net zonal volume transport. A relationship is observed between
25 ridge width and volume transport that is determined by the form stress gener-
26 ated by the ridge. Gyre formation is also highly reliant on the ridge geometry.
27 A steep ridge allows gyres to form within regions of unblocked geostrophic
28 (f/H) contours, with an increase in gyre strength as the ridge width is re-
29 duced. These relationships between ridge width, gyre strength, and net zonal
30 volume transport emerge in order to simultaneously satisfy the conservation
31 of momentum and vorticity.

32 **1. Introduction**

33 The Antarctic Circumpolar Current (ACC) and Southern Ocean gyres are key components of
34 the global climate system. The Southern Ocean forms the primary pathway for communication
35 between the Atlantic, Indian and Pacific Oceans (Talley 2013; Naveira Garabato et al. 2014).
36 Water, heat, salt and other important tracers are transported zonally between these ocean basins
37 around Antarctica via the ACC (Talley 2013), which has an estimated total volume transport of
38 173.3 ± 10.7 Sv (Donohue et al. 2016) ($1 \text{ Sv} = 10^6 \text{ m}^3 \text{ s}^{-1}$). A double overturning cell is responsible
39 for the meridional exchange of water-masses between the Southern Ocean and the basins to the
40 north (Speer et al. 2000). The lower cell of this overturning is reliant on diabatic processes that
41 predominately occur in the vicinity of Southern Ocean gyres (Naveira Garabato et al. 2014) and,
42 thus, gyre dynamics are implicated in overturning activity.

43 The Southern Ocean has numerous topographic features with scales similar to terrestrial moun-
44 tain ranges, spanning distances of $\mathcal{O}(1000 \text{ km})$. Large-scale topographic features are of particular
45 importance in the Southern Ocean (Hughes and Killworth 1995) and are known to have a sig-
46 nificant effect on steering the path of the ACC (Gordon et al. 1978; Killworth 1992). Figure 1
47 highlights the effect of topography on the ACC, illustrating the influence of topographic steering.
48 A notable feature that steers the ACC is the Pacific-Antarctic Ridge, which deflects the current
49 northward over the western flank of the ridge until it passes through the fracture zones to the
50 north.

51 The primary influence of topographic steering is best described in terms of vorticity and vertical
52 stretching. The context for describing large-scale flow in this way was first outlined by Rossby
53 (1936) and later named in Rossby et al. (1940) as potential vorticity. Flow must conserve potential
54 vorticity and to leading-order it does so by maintaining f/H , where f is the Coriolis parameter

55 and $H = h + \eta$ is the water column thickness, with h the distance from the resting ocean surface
56 to the bottom topography and η the sea surface height anomaly. As flow is directed towards the
57 peak of a ridge, it travels equatorward to satisfy conservation of potential vorticity. Flow then
58 reverses direction and travels poleward as the water column thickness increases on the lee side of
59 the ridge. Conservation of potential vorticity means that flow tends to align with contours of f/H
60 (geostrophic contours).

61 The process of topographic steering has a central role in the momentum balance of the Southern
62 Ocean. Wind stress provides a source of momentum at the surface of the ocean. In order to
63 satisfy the momentum balance there must be an equal and opposite sink. The meridional deflection
64 of the ACC by topography is associated with form stress, the primary zonal momentum sink
65 balancing the wind stress in the Southern Ocean (Munk and Palmén 1951; Wolff et al. 1991;
66 Stevens and Ivchenko 1997; Masich et al. 2015). Form stress develops where the ACC is subject
67 to inertial effects or bottom stress as it traverses topography (Naveira Garabato et al. 2013). Under
68 these conditions, the ACC deviates from geostrophic contours leading to a lateral offset in the sea
69 surface height with respect to the topography. A net pressure force across topography associated
70 with this offset in the sea surface height leads to a generation of form stress (Stewart and Hogg
71 2017). Topography is important in regulating the net zonal transport of the ACC. One aspect of
72 this topographic control is related to form stress (Munk and Palmén 1951). A zonal momentum
73 balance between bottom stress and wind stress results in an unrealistically large volume transport
74 in comparison to a balance between form stress and wind stress (Munk and Palmén 1951).

75 The volume transport through a channel is also sensitive to the proportion of blocked geostrophic
76 contours. In an area of unblocked geostrophic contours, the dynamics are described by a ‘linear
77 free mode’ (Read et al. 1986; Hughes et al. 1999; Tansley and Marshall 2001) and consequently
78 a through channel flow can develop. The space of blocked geostrophic contours emerges through

79 the presence of ‘land masses’, creating an area where Sverdrup balance dominates and classical
80 gyres form as a result (LaCasce and Isachsen 2010). As ridge height increases, the topography acts
81 to block geostrophic contours and zonal volume transport reduces in strength (Krupitsky and Cane
82 1994; Wang and Huang 1995; Nadeau and Ferrari 2015). This binary view of the Southern Ocean
83 is only directly applicable to a linear barotropic setting and we emphasise that many other factors
84 add complexity to this simple theory. Much of the ACC, governed by an ‘almost free mode’,
85 drifts into regions of globally blocked geostrophic contours (Hughes et al. 1999). Nevertheless,
86 the simple view that net zonal volume transport is dependent on the level of blocked f/H is a
87 useful construct for this barotropic study.

88 Linear studies show that the net zonal volume transport in a channel is also dependent on ridge
89 width (Johnson and Hill 1975; Krupitsky and Cane 1994; Wang and Huang 1995). Varying topog-
90 raphy in this way does not affect the level of blocked f/H and it isolates the dependence on the
91 ridge geometry itself. These existing studies investigate the linear dynamics in two settings, one
92 where all geostrophic contours are blocked (Krupitsky and Cane 1994; Wang and Huang 1995)
93 and one where there is only partial blocking of geostrophic contours (Johnson and Hill 1975).
94 Localised blocking of geostrophic contours is dynamically distinct from the partially unblocked
95 case because of the way that form stress develops in a linear system. Form stress can only develop
96 where bottom stress curl permits flow to cross geostrophic contours and this process is more read-
97 ily attained where geostrophic contours are locally blocked (Wang and Huang 1995). However,
98 in the Southern Ocean, few continental boundaries exist for the blocking of geostrophic contours.
99 As a result, it is indicated that a large proportion of the form stress momentum sink occurs over
100 topography that has no association with blocked geostrophic contours (Masich et al. 2015). The
101 lack of requirement for localised blocked geostrophic contours in the Southern Ocean stems from
102 non-linearity. The form stress is largely governed by topographic Rossby waves (Thompson and

103 Naveira Garabato 2014), which require non-linear dynamics (McCartney 1976; Johnson 1977).
104 This highlights the importance of understanding the case with locally unblocked geostrophic con-
105 tours in a non-linear system.

106 Progress has been made on the non-linear case with dynamical discussions given by Treguier
107 and McWilliams (1990), Wolff et al. (1991) and Stevens and Ivchenko (1997). However, unlike
108 the linear case, questions remain around the effects of geometric variations. The relationship
109 between ridge height and volume transport has been investigated in a non-linear setting by Nadeau
110 and Ferrari (2015) but changes in ridge height effect the level of blocked f/H . A non-linear
111 dynamical understanding of the effects of ridge geometry in a region of unblocked geostrophic
112 contours is currently missing from the literature.

113 Not only is ridge topography important in determining the ACC volume transport but it is also
114 crucial to Southern Ocean gyre formation. With the prevailing theory of potential vorticity, pole-
115 ward ACC flow should dominate the eastern flanks of ridges in the Southern Ocean, but this is not
116 uniformly the case. Figure 1 shows that particular locations east of ridge topography are domi-
117 nated by gyre circulations. In classical gyre theory, western boundary currents are supported by
118 the intersection of geostrophic contours with continental boundaries, which lead to the formation
119 of gyres (see Patmore 2018). Departing from this theory, circulations such as the Ross Gyre occur
120 in the absence of continental boundaries. Instead, these gyres form in the lee of large meridional,
121 submarine topographic features where geostrophic contours are locally unblocked. Modelling re-
122 sults have been presented where gyres form without the need for a western boundary (Krupitsky
123 and Cane 1994; Wang and Huang 1995; Munday et al. 2015). However, the northern boundary
124 in these simulations emulate a continent by blocking geostrophic contours. As a result, the gyres
125 coincide with blocked geostrophic contours and it is not clear this regime is representative of
126 Southern Ocean dynamics, since no northern boundary exists. Nadeau and Ferrari (2015) propose

127 that Southern Ocean gyres can be supported via a threshold of topographic gradients alone. How-
128 ever, their simulations also contain geostrophic contours that are blocked by a northern wall and
129 so the effects of topographic gradients are not isolated.

130 This study investigates the role of topographic geometry in ACC dynamics and the formation
131 of Southern Ocean gyres in a non-linear, barotropic setting with unblocked geostrophic contours.
132 Specifically we aim to examine the hypothesis of Nadeau and Ferrari (2015) that topographic
133 gradients alone can produce gyres, and we delve deeper into the details of why this might occur.
134 We also explore the unknown effects of topographic geometry on non-linear barotropic dynamics
135 in unblocked geostrophic contours. Although the system we present permits barotropic eddies and
136 non-linear effects, it is not in the barotropic eddy-saturated regime demonstrated by Constantinou
137 (2018). We therefore frame the discussion of the gyre dynamics in terms of bottom stress, in
138 order to make a clear exposition of the dynamics. A sink of vorticity is required for the formation
139 of gyres and it is well established that bottom stress can take this role (Stommel 1948). In the
140 same vein, baroclinicity is also omitted from this study. A barotropic system is sufficient to test
141 the hypothesis of Nadeau and Ferrari (2015) and build on the linear ACC theory outlined by
142 Johnson and Hill (1975), Krupitsky and Cane (1994) and Wang and Huang (1995). With this
143 simple barotropic representation, many aspects of Southern Ocean flow are missing and it must be
144 stressed that it is not the intention to provide an exact representation of Southern Ocean dynamics.
145 To make this distinction clear, the barotropic representation of the ACC in the model results will
146 be referred to as a ‘circumpolar current’. The limitations of our reduced system are discussed in
147 Section 5 along with some speculation about how the ideas presented in this study might transfer
148 to more complex cases.

149 The remainder of this paper is structured as follows. Section 2 outlines the methods, presenting
150 the model utilised and all equations of motion relevant to the results of this study. In Section

151 3, results are presented detailing the effect of topographic variation on a barotropic circumpolar
152 current and the zonal momentum budget. Section 4 gives a new insight into the role of topography
153 in the formation of Southern Ocean gyres. Section 5 contains a general discussion of how our
154 results relate to the current literature. Lastly, a summary is provided in Section 6.

155 2. Methods

156 a. Governing Equations

157 For a fluid with uniform density, the hydrostatic Navier-Stokes equations are given by:

$$\rho_0 \left(\frac{D\mathbf{u}}{Dt} + f\mathbf{k} \times \mathbf{u} \right) = -\nabla p - \rho_0 g \mathbf{k} + \mu \nabla^2 \mathbf{u}, \quad (1)$$

158 with conservation of mass

$$\nabla \cdot \mathbf{u} = 0, \quad (2)$$

159 where ρ_0 is the reference density; $D\mathbf{u}/Dt = \partial\mathbf{u}/\partial t + \mathbf{u} \cdot \nabla\mathbf{u}$ is the material derivative; $\mathbf{u} =$
160 $\{u, v, w\}$ is the velocity vector where u , v and w are the velocity components in the x , y and z
161 directions; f is the Coriolis parameter; \mathbf{k} is the unit vector pointing upwards; p is the pressure;
162 μ is the dynamic viscosity coefficient, and the horizontal components of the Earth's rotation have
163 been neglected. For convenience u will be referred to as the eastward velocity and v the northward
164 velocity.

165 This study uses three forms of equation (1): the barotropic vorticity equation, barotropic poten-
166 tial vorticity equation and barotropic zonal momentum equation (see Patmore (2018) for deriva-
167 tions). The merits of barotropic vorticity and potential vorticity are well described in Jackson et al.
168 (2006). These equations are equivalent to each other in a domain with a flat bottom, and it is
169 only when topography is introduced that the benefit of each becomes clear. Potential vorticity and
170 barotropic vorticity are primarily used to understand gyre dynamics. The barotropic zonal mo-

171 momentum equation is useful for understanding the interaction between topography and circumpolar
 172 flow.

173 1) BAROTROPIC VORTICITY EQUATION

174 Taking the depth integral of the momentum equations (1) gives the barotropic momentum
 175 equations. The vertical component of the curl of the barotropic momentum equations gives the
 176 barotropic vorticity equation. The steady barotropic vorticity equation is:

$$\rho_0 \left(\mathbf{k} \cdot \nabla \times \left(\overline{H\mathbf{u}} \cdot \nabla \overline{\mathbf{u}} + \overline{H\mathbf{u}' \cdot \nabla \mathbf{u}'} \right) + \overline{H\beta\bar{v}} \right) = \mathbf{k} \cdot \nabla \overline{p_b} \times \nabla h + \mathbf{k} \cdot \nabla \times (\overline{\boldsymbol{\tau}_w} - \overline{\boldsymbol{\tau}_b}) + \mu \overline{H} \nabla^2 \overline{\zeta}, \quad (3)$$

177 where overbars signify the time-mean; primes denote the deviation from the time-mean; $H = h + \eta$
 178 is the water column thickness, with h the distance from the resting ocean surface to the bottom
 179 topography and η the sea surface height anomaly; $\beta = df/dy$; $p_b = \rho_0 g H$ is the bottom pressure;
 180 $\boldsymbol{\tau}_w$ is the wind stress; $\boldsymbol{\tau}_b$ is the bottom stress and $\zeta = dv/dx - du/dy$ is the relative vorticity. The
 181 term $\mathbf{k} \cdot \nabla p_b \times \nabla h$ is referred to as the bottom pressure torque. This is the Reynolds averaged
 182 form of the barotropic vorticity equation. Covariance in the constituents of the H' terms that result
 183 from Reynolds averaging are assumed small and are neglected.

184 The barotropic vorticity equation is useful for decomposing the dynamics of gyres. In a domain
 185 with variable topography, the barotropic vorticity equation quantifies the influence of the topogra-
 186 phy through bottom pressure torque (Holland 1972; Hughes and De Cuevas 2001; Jackson et al.
 187 2006). The primary barotropic vorticity balance over topography is between $\mathbf{k} \cdot \nabla \overline{p_b} \times \nabla h$ and
 188 $\rho_0 \overline{H\beta\bar{v}}$ (Holland 1972). The time-mean form of the equation provides insight into the influence
 189 of eddy effects on the time-mean flow through the Reynolds stress term $\rho_0 \mathbf{k} \cdot \nabla \times (\overline{H\mathbf{u}' \cdot \nabla \mathbf{u}'})$
 190 (Hughes and Ash 2001; Thompson and Richards 2011).

191 2) BAROTROPIC POTENTIAL VORTICITY EQUATION

192 The barotropic potential vorticity equation is obtained by taking the depth-average of the vertical
 193 component of the curl of the momentum equations. The barotropic potential vorticity equation is:

$$\frac{D}{Dt} \left(\frac{f + \zeta}{H} \right) = \frac{1}{\rho_0 H} \mathbf{k} \cdot \nabla \times \left(\frac{\tau_w - \tau_b}{H} \right) + \frac{\nu}{H} \nabla^2 \zeta, \quad (4)$$

194 where $\nu = \mu/\rho_0$ is the kinematic viscosity coefficient. This equation is a useful alternative to
 195 the barotropic vorticity equation for assessing gyre dynamics and highlighting the effects of to-
 196 pographic steering in general. In this study, potential vorticity is reserved solely for theoretical
 197 discussion of both gyre and circumpolar current dynamics. As a leading-order approximation,
 198 equation (4) can be simplified to

$$\frac{D(f/H)}{Dt} = 0, \quad (5)$$

199 where flow follows contours of f/H in order to conserve potential vorticity. ζ can be neglected
 200 from the left-hand side of equation (4) when scales are larger than the Rhines scale $(U/\beta)^{1/2}$
 201 (Naveira Garabato et al. 2013). Neglecting ζ gives the linearised form of potential vorticity. Terms
 202 on the right-hand side of the linearised form of (4) cause flow to deviate from contours of f/H and
 203 are important for the formation of gyres. Potential vorticity is therefore a natural context in which
 204 to frame gyre formation in a conceptual sense. The Reynolds stress term is associated with ζ and
 205 thus, Reynolds-averaging is not relevant for the linearised form of potential vorticity.

206 3) BAROTROPIC ZONAL MOMENTUM EQUATION

207 The barotropic zonal momentum equation is the depth and zonal integral of the zonal momentum
 208 equation. The steady, Reynolds-averaged barotropic zonal momentum equation is defined as:

$$\begin{aligned} \rho_0 \left(\oint \bar{H} (\bar{\zeta} \bar{v} + \bar{\zeta}' v') dx + \oint \frac{\bar{H}}{2} \frac{\partial (\bar{u}^2 + \bar{v}^2)}{\partial x} dx + \oint \frac{\bar{H}}{2} \frac{\partial (u^2 + v^2)}{\partial x} dx \right) = \\ \oint \bar{p}_b \frac{\partial h}{\partial x} dx + \oint \bar{\tau}_w^x dx - \oint \bar{\tau}_b^x dx + \mu \oint \bar{H} \nabla^2 \bar{u} dx. \end{aligned} \quad (6)$$

209 Circular integrals denoted by $\oint dx$ are taken over a zonally re-entrant channel domain. The Coriolis
210 term is absent in (6) because $\oint Hfv dx = 0$ in this channel setting.

211 In the Southern Ocean, the primary source of momentum is wind stress. The key zonal mo-
212 mentum sink balancing the wind stress is form stress, $\oint \bar{p}_b(\partial h/\partial x) dx$, which is generated in the
213 presence of topographic variations. The barotropic zonal momentum equation is used in this study
214 to link variations in topography to changes in volume transport.

215 *b. Model*

216 Idealised modelling experiments are conducted with the Massachusetts Institute of Technology
217 general circulation model (MITgcm, (Marshall et al. 1997a,b)), a model capable of simulating the
218 full Navier-Stokes equations. Velocities are taken to be uniform in the vertical, achieved by using
219 a grid with one layer. Variable seabed topography is incorporated using partial cells. The density
220 is taken to be constant everywhere.

221 Table 1 gives a summary of the variations in model configuration for all simulations presented
222 in this study. All simulations are based on a 1-layer channel of 5000 m depth, to which a variety of
223 ridge geometries are added. The initial domain has size: $L_x = 7200$ km and $L_y = 7200$ km, where
224 L_x and L_y represent the length of the domain in the zonal and meridional directions respectively.
225 All models have a zonally uniform surface wind stress. The initial results have a domain uniform
226 zonal wind stress of magnitude $\tau_0 = 0.144$ N m⁻². The initial results in Section 4 with $L_y =$
227 3600 km are forced with a ‘sinusoidal’ zonal wind stress which varies in the meridional direction
228 according to $\tau_w^x = 0.5\tau_0(1 - \cos(2\pi y/L_y))$, where $\tau_0 = 0.144$ N m⁻² is the peak wind stress. In
229 these latter runs, both the wind stress and its curl drop to zero at the domain boundaries to the north
230 and south. The extended domain in Section 4 with $L_y = 7200$ km uses the same wind forcing in
231 the southern half of the domain and $\tau_w^x = 0$ otherwise.

232 The horizontal grid spacing is 12.5 km. The time-step is one hour. All simulations are run for
233 10 years. The output is recorded at intervals of 24 hours. All results are averaged over the outputs
234 from the final simulation year, when the model is statistically steady. The model uses the β -plane
235 approximation, with the Coriolis parameter $f = f_0 + \beta y$, where $f_0 = 2\omega \sin \phi_0$, $\beta = (2\omega \cos \phi_0)/a$,
236 $\omega = 7.2921 \cdot 10^{-5} \text{ s}^{-1}$ is the angular velocity of the Earth, ϕ_0 is a fixed latitude and $a = 6371 \text{ km}$
237 is the Earth's radius. In all model simulations the southern latitudinal boundary of the model is set
238 to $\phi_0 = -60.85^\circ$ such that $f_0 = -1.27393 \cdot 10^{-4} \text{ s}^{-1}$ and $\beta = 1.1144 \cdot 10^{-11} \text{ m}^{-1} \text{ s}^{-1}$. The model
239 uses a constant reference density ρ_0 . The hydrostatic approximation means that $p = \rho_0 g(\eta - z)$,
240 where $g = 9.8 \text{ m s}^{-2}$. All solid lateral boundaries have a free-slip condition. The upper boundary
241 is governed by a non-linear free surface, the lower by a quadratic drag with drag coefficient of
242 $C_d = 2.5 \cdot 10^{-3}$, and there is a constant kinematic viscosity coefficient of $\nu = 10 \text{ m}^2 \text{ s}^{-1}$.

243 **3. Topographic Control of the Antarctic Circumpolar Current**

244 Previous studies have shown that topography can regulate the volume transport of the ACC
245 (Munk and Palmén 1951; Wolff et al. 1991; Tansley and Marshall 2001; Nadeau and Ferrari 2015).
246 The mechanism for this is form stress balancing wind stress in the zonal momentum balance. Form
247 stress can only exist where there is topographic variation, and without it the volume transport of the
248 ACC would be orders of magnitude larger than observed (Munk and Palmén 1951). Relationships
249 between seabed ridge width and zonal volume transport are well established for the linear case
250 for regions of both blocked and unblocked geostrophic contours (Krupitsky and Cane 1994; Wang
251 and Huang 1995). Linear dynamics are significantly distinct from the non-linear counterpart due
252 to the absence of topographic Rossby waves (Wang and Huang 1995). The effects of geometric
253 variations are yet to be explored in the non-linear setting with unblocked geostrophic contours.

254 This section considers the role of ridge width on the dynamics of a barotropic circumpolar current
255 in this setting and investigates the dynamical details of the relationships that emerge.

256 *a. The Relationship between Ridge Width and Channel Flow Dynamics*

257 To assess the impact of topography on a circumpolar current, an idealised experiment is con-
258 ducted where ridge width is varied. The simulations in this experiment are forced with a uni-
259 form zonal wind over the entire domain in order to simplify the dynamics. Figure 2a-c shows the
260 barotropic streamfunction for simulations 02, 04 and 08 with varying ridge widths (1000 km, 2000
261 km and 4000 km). Unlike experiments that vary ridge height (Krupitsky and Cane 1994; Wang
262 and Huang 1995; Krupitsky et al. 1996; Nadeau and Ferrari 2015), varying ridge width has no ef-
263 fect on the range of blocked f/H here. The results show deviation of flow over topography due to
264 conservation of potential vorticity, demonstrating the leading-order role of (5). The equatorward
265 deflection of geostrophic contours causes a proportion of them to become blocked through inter-
266 section with the solid domain boundaries to the north and south. Areas of unblocked geostrophic
267 contours are signified in Figure 2a-c by the shaded region. Flow approximately follows contours
268 of f/H and is confined to this shaded area. Flow cannot intersect with a solid boundary and little
269 flow develops in the unshaded region. The results in Figure 2a-c show that the volume transport
270 increases as the ridge width increases. This is confirmed by results in Figure 2g, which shows
271 the volume transport for a larger set of ridge width variations. The barotropic zonal momentum
272 budget has been calculated for the same set of experiments, with the quantities shown in Figure
273 2h. The momentum budget in Figure 2h confirms that the primary balance is between form stress
274 and wind stress (Munk and Palmén 1951; Wolff et al. 1991; Stevens and Ivchenko 1997; Masich
275 et al. 2015).

276 For all simulations, there is a small proportion of the wind stress that is balanced by bottom
 277 stress, which increases with ridge width (Figure 2h). As ridge width increases there is a small de-
 278 crease in the momentum sink via form stress. Bottom stress accounts for the reduction, increasing
 279 with increased ridge width. The relationship outlined is a result of the bottom stress term in the
 280 zonal momentum budget being a function of zonal velocities. As the volume transport through
 281 the channel increases there is an increase in the zonal velocities resulting in a larger bottom stress
 282 momentum sink.

283 *b. Form Stress*

284 Flow over topography results in the generation of form stress. Whilst form stress is well known
 285 in the literature, the concept is integral to our analysis and as a result, we provide a detailed
 286 background of this term.

287 In equation (6), the term associated with form stress is $\oint \bar{p}_b (\partial h / \partial x) dx$. Since $\bar{p}_b = \rho_0 g (\bar{\eta} + h)$
 288 under the hydrostatic approximation, and $\oint h (\partial h / \partial x) dx = 0$, form stress can be re-written as

$$\begin{aligned} \oint \bar{p}_b \frac{\partial h}{\partial x} dx &= \rho_0 g \oint (\bar{\eta} + h) \frac{\partial h}{\partial x} dx \\ &= \rho_0 g \oint \bar{\eta} \frac{\partial h}{\partial x} dx, \end{aligned} \quad (7)$$

289 where η is defined as before: the anomaly in the sea surface height.

290 Form stress represents a pressure difference across a topographic feature, which is associated
 291 with meridional flow induced by topographic steering due to conservation of potential vorticity. In
 292 the Southern Hemisphere, the sea surface height (SSH) increases towards the left of a large-scale
 293 geostrophic flow. The equatorward flow on the western flank of a ridge and poleward flow on the
 294 eastern flank results in a SSH dip towards the ridge crest, illustrated in the conceptual schematic
 295 shown in Figure 3a. Under the assumption of a symmetric linear topographic profile, form stress

296 would be:

$$\begin{aligned} \rho_0 g \oint \bar{\eta} \frac{\partial h}{\partial x} dx &= \rho_0 g \int_{x_0}^{x_2} \bar{\eta} \frac{\partial h}{\partial x} dx \\ &= \rho_0 g \left(\int_{x_0}^{x_1} \bar{\eta} \frac{\partial h}{\partial x} dx + \int_{x_1}^{x_2} \bar{\eta} \frac{\partial h}{\partial x} dx \right) \\ &= \rho_0 g \left| \frac{\partial h}{\partial x} \right| \left(\int_{x_1}^{x_2} \bar{\eta} dx - \int_{x_0}^{x_1} \bar{\eta} dx \right), \end{aligned} \quad (8)$$

297 where x_0 represents the leading ridge base, x_1 the ridge peak and x_2 the trailing ridge base. If
298 the dip in the sea surface lies symmetrically over the topography $\int_{x_1}^{x_2} \bar{\eta} dx = \int_{x_0}^{x_1} \bar{\eta} dx$ and there
299 would be no form stress. The conditions for form stress to exist are encapsulated by the fact
300 that $\oint \bar{\eta} (\partial h / \partial x) dx \neq 0$ if and only if there is a zonal offset of the topography and the anomaly
301 in SSH. A zonal offset results in a thicker water column over the western ridge flank versus the
302 eastern flank and hence a difference in pressure across the ridge.

303 *c. The Source of the Lateral Offset*

304 The lateral offset in the SSH anomaly is associated with a vorticity sink perturbing flow
305 from geostrophic contours, which can result from the presence of either bottom stress or iner-
306 tia (Naveira Garabato et al. 2013). Where there is an exact balance in equation (3) between the
307 advection of planetary vorticity ($-\rho_0 \bar{H} \beta \bar{v}$) and the bottom pressure torque ($\mathbf{k} \cdot \nabla \bar{p}_b \times \nabla h$), flow
308 is aligned with geostrophic contours (Jackson et al. 2006). Where this balance is imperfect, flow
309 deviates from geostrophic contours. The vorticity contributions of bottom stress and inertia are
310 linked to an asymmetric deviation of flow relative to geostrophic contours as it traverses topogra-
311 phy.

312 Bottom stress curl associated with the circumpolar jet is anti-cyclonic to the left of the jet centre
313 and cyclonic to the right. On the downstream ridge flank, the bottom stress curl works in concert
314 with bottom pressure torque to the left and in opposition to the right of the jet centre, which

315 is associated with a down-slope deviation of the flow (Jackson et al. 2006). The meridionally
316 uniform topography reduces the bottom pressure torque to $-(d\bar{p}_b/dy) \cdot (dh/dx)$, with a change in
317 sign across the ridge. As a result, the relationship with bottom stress curl is reversed and on the
318 upstream ridge flank flow deviates up-slope.

319 The role of inertia is similar to that of bottom stress, but differences occur in the associated
320 downstream dynamics. The existence of stationary topographic Rossby waves causes flow to
321 oscillate about geostrophic contours eastward of the ridge crest (McCartney 1976). The overall
322 downstream deviation is then a linear combination of the down-slope deflection (as described for
323 the bottom stress case) and Rossby wave oscillation (McCartney 1976).

324 The asymmetry in a linear case with blocked geostrophic contours is achieved through bottom
325 stress curl only (Krupitsky and Cane 1994; Wang and Huang 1995). The blocked geostrophic
326 contours generate a lateral boundary layer, which is dynamically similar to a Stommel gyre western
327 boundary current (Stommel 1948). The flow crosses geostrophic contours via the presence of
328 bottom stress curl and an asymmetry develops across the topography.

329 The asymmetric deviation of flow due to either bottom stress or inertia is associated with an SSH
330 anomaly which is displaced eastward, as depicted in Figure 3. The offset of the SSH profile gen-
331 erates a pressure difference across the topography, creating the form stress and a momentum sink.
332 In the non-linear unblocked case explored in this Section, the lateral offset occurs in association
333 with both Rossby waves and bottom stress curl.

334 *d. Mechanisms for Perturbing Form Stress*

335 It has been shown by Figure 2h that for changing topography, form stress remains the primary
336 momentum sink for the wind stress. The wind stress remains constant between simulations, and
337 so must the form stress. Despite form stress remaining approximately constant, it has two varying

338 components between simulations, the ridge width (dx) and the SSH (η). Although dx varies, it has
 339 no net effect on the form stress because changes in the two dx terms of (7) cancel as the bounds of
 340 integration change. η on the other hand is determined by the dynamics and form stress is strongly
 341 dependent on this term. How η evolves in response to changes in topography is integral to the
 342 relationships that we observe.

343 Figure 3 illustrates two ways in which the sea surface influences form stress. The first mecha-
 344 nism, shown in Figure 3b, comprises a reduction in the lateral offset between the SSH profile and
 345 the topography. The dip in the sea surface shifts westward. The sea surface rises to the east of the
 346 ridge peak and sinks to the west of the ridge peak. As a result, $\int_{x_1}^{x_2} \eta dx$ decreases in magnitude and
 347 $\int_{x_0}^{x_1} \eta dx$ increases in magnitude. This causes a reduction in the magnitude of $\int_{x_1}^{x_2} \eta dx - \int_{x_0}^{x_1} \eta dx$
 348 and through (8) form stress is reduced. The second, illustrated in Figure 3c, constitutes a reduction
 349 in the sea surface dip induced by the meridional velocities over the ridge. A change in form stress
 350 due an adjustment in the dip of sea surface is well illustrated by Stewart and Hogg (2017) and
 351 the details of this effect can be seen by reforming the form stress term. Following LaCasce and
 352 Isachsen (2010), integration by parts gives:

$$\rho_0 g \oint \bar{\eta} \frac{\partial h}{\partial x} dx = -\rho_0 g \oint h \frac{\partial \bar{\eta}}{\partial x} dx = -\rho_0 g \oint f h v_g dx, \quad (9)$$

353 where v_g is the geostrophic meridional velocity. Any changes in the sea surface dip are associated
 354 with changes in $\partial \eta / \partial x$ and hence the meridional velocities. Thus, by (9) a larger dip (or $\partial \eta / \partial x$)
 355 is associated with a larger form stress.

356 *e. The Role of Form Stress in Regulating Volume Transport*

357 The relationship between volume transport and ridge width shown in Figure 2 can be explained
 358 in terms of form stress. Figure 4a shows the profiles of η over the topography as the ridge width is

359 varied. As the ridge width is decreased, the sea surface dip reduces. There is a simultaneous shift
 360 in the profile to the east, which is observed in Figure 4b as an eastward shift in the minimum point
 361 of the sea surface profile. These changes have opposing effects on the form stress. The eastward
 362 shift causes an increase in form stress and the decreased dip causes a decrease in form stress. The
 363 opposing effects act to maintain form stress as the primary balance form the wind stress. The shift
 364 must have a slightly larger effect than the dip in order to create the overall marginal increase in
 365 form stress shown in Figure 2h.

366 Figure 4c shows the depth and meridionally integrated meridional velocities over the ridge,
 367 where the x-axis is scaled by ridge width. The meridional velocities over the topography are
 368 similar for all ridge widths. They are linked directly to form stress via (9) and are sustained by the
 369 topographic controls described above.

370 The relationship between volume transport and ridge width results from the insensitivity of the
 371 meridional velocities shown in Figure 4c. The meridional velocities are approximately constant
 372 between simulations (Figure 4c), whilst zonal velocities increase with ridge width (not shown).
 373 As ridge width increases, the geostrophic contours become more zonal. The flow primarily aligns
 374 with geostrophic contours and in order for meridional velocities to remain the same the flow speed
 375 must increase, leading to elevated zonal velocities. Higher zonal velocities causes an increase in
 376 the volume transport. An equivalent description is as follows. For $U = \int_{-h}^{\eta} u dz$ and $V = \int_{-h}^{\eta} v dz$,

$$\frac{U}{V} \approx \frac{w}{2L_{\beta}}, \quad (10)$$

377 where w is the ridge width and L_{β} is the meridional deviation of an f/H contour between the
 378 base and peak of the ridge. An approximation of volume transport is found by taking a meridional
 379 integral of (10),

$$T = \int_0^{L_y} U dy \approx \frac{w}{2L_{\beta}} \int_0^{L_y} V dy, \quad (11)$$

380 where T represents the volume transport through the channel. The relationship provided by (11)
381 shows ridge geometry links the meridional velocities to the volume transport. A constant $\int_0^{L_y} V dy$
382 and decreasing w results in a lowered volume transport. This means that the changing circum-
383 polar transport in these simulations can be understood as consequence of the constant meridional
384 velocity magnitudes over the ridge.

385 In summary, this sub-section has described why a steeper ridge is associated with reduced cir-
386 cumpolar transport. The full mechanism is as follows:

- 387 1. Form stress remains approximately constant, matching wind stress.
- 388 2. As ridge width increases, the zonal offset in the SSH dip relative to the ridge decreases. If
389 unopposed, this would reduce form stress.
- 390 3. An increasing SSH dip opposes the zonal offset, acting to maintain the form stress.
- 391 4. This increasing dip is associated with constant zonal SSH gradients, associated with merid-
392 ional velocities that are independent of ridge width.
- 393 5. Wider ridges alter the geostrophic contours such that the unvarying meridional velocities
394 require an increased zonal volume transport.

395 *f. Dynamical Sensitivity to Changes in Bottom Stress*

396 The momentum sink provided by bottom stress is small in comparison to form stress (Figure
397 2h). Despite this, it can be important to the dynamics in less direct ways. The presence of form
398 stress is reliant on bottom stress and/or inertia to generate an offset in the SSH anomaly from the
399 topography (Naveira Garabato et al. 2013). The indirect role that bottom stress has in generating
400 form stress highlights the potential importance of this term to the dynamical system presented. As

401 such, additional simulations are carried out where the bottom stress coefficient is varied (Figure 5)
402 and we discuss the associated dynamics of this term.

403 Figure 5a shows that there is a reduction in volume transport in response to an increased bottom
404 stress coefficient, which requires reduced velocities to maintain the bottom stress momentum sink.
405 However, this response cannot retain the exact same momentum balance and a slight adjustment
406 occurs. Figure 5b shows that the proportion of the wind stress that is balanced by the bottom stress
407 increases as the bottom stress coefficient increases. A larger reduction in volume transport would
408 be required to maintain the bottom stress momentum sink at its previous level.

409 Figure 5b shows that the increase in the bottom stress momentum sink is balanced by a decrease
410 in form stress. Any change in form stress can be observed in the sea surface profile. Figure 5c
411 and 5d show the SSH profile for the simulations where the bottom stress coefficient is varied. The
412 decrease in form stress is primarily associated with reduction in sea surface dip (Figure 5c) and
413 there is little change in the sea surface offset (Figure 5d).

414 The results show that the relative importance of form stress in the zonal momentum budget re-
415 duces with increased bottom stress coefficient. An increase in the bottom stress coefficient causes
416 a decreased volume transport, reducing the sea surface dip and form stress reduces as a result. The
417 volume transport reduction is not sufficient to maintain the bottom stress momentum sink at the
418 same level. Bottom stress increases, balancing the reduction of the form stress momentum sink.

419 This relationship between volume transport and bottom stress coefficient is contrary to existing
420 results and it is often found that increasing the bottom stress coefficient increases the net zonal
421 volume transport (Tansley and Marshall 2001; Nadeau and Straub 2012; Nadeau and Ferrari 2015;
422 Marshall et al. 2017; Constantinou 2018). The reversed relationship in many of the existing results
423 relies on the presence of a baroclinicity that gives rise to the vertical structure described by Straub

424 (1993). The reversed relationship can also occur in a barotropic setting if the forcing is strong and
425 the bottom stress coefficient is below a particular threshold (Constantinou 2018).

426 **4. Topographic Control of Southern Ocean Gyres**

427 The above sections have shown that the geometry of topography has a significant influence
428 on the volume transport through a channel which is representative of the Southern Ocean. The
429 investigation is now directed towards the role of topography on Southern Ocean gyres. Gyre
430 formation requires a curl in the wind stress. The simulations discussed above were forced with
431 a uniform wind stress and hence gyres did not form; the following simulations are forced with a
432 wind stress with non-zero curl.

433 *a. The Dynamics of Gyres in regions of blocked Geostrophic Contours*

434 The established knowledge of gyre formation in the Southern Ocean indicates a requirement for
435 blocking of geostrophic contours (LaCasce and Isachsen 2010; Nadeau and Ferrari 2015; Munday
436 et al. 2015). In early modelling studies, gyres were formed through the intersection of geostrophic
437 contours with a meridional wall which extends to the surface (LaCasce and Isachsen 2010). How-
438 ever, circulations such as the Ross Gyre occur in absence of any meridional wall. Simulations
439 have been presented where gyres form without the need for a meridional boundary (Krupitsky and
440 Cane 1994; Wang and Huang 1995; Krupitsky et al. 1996; Nadeau and Ferrari 2015; Munday et al.
441 2015) but these results still rely on blocked geostrophic contours. In these domains, absent of a
442 meridional wall, submarine topography introduces an intersection of geostrophic contours with the
443 northern and southern boundaries of a channel domain. An example of this kind of gyre formation
444 is given in Figure 6. In a channel domain without topography (Figure 6a and 6b), geostrophic
445 contours are strictly zonal and do not intersect with any boundary. A linear free mode develops

446 and flow aligns with the zonal geostrophic contours, producing a zonal flow with an enormous
447 volume transport. Topography reduces the volume transport in this situation (Wolff et al. 1991;
448 Tansley and Marshall 2001). As topography is introduced, geostrophic contours become blocked
449 by the domain's northern and southern walls (Figure 6c and 6d). Topographic Sverdrup balance
450 ensues and gyres form in the region of blocked geostrophic contours (Krupitsky et al. 1996). Once
451 all geostrophic contours intersect with the boundaries (Figure 6g and 6h) there is virtually no cir-
452 cumpolar flow (≈ 2 Sv). As a result, topographic Sverdrup balance dominates and the system is
453 very similar to a walled domain representative of a mid-latitude gyre (Figure 6i and 6j).

454 The pathway for gyre formation through blocked geostrophic contours to the north and south
455 outlined via Figure 6 is not representative of circulations such as the Ross Gyre. In the Pacific
456 sector of the Southern Ocean, where the Ross Gyre forms, no northern boundary exists with which
457 geostrophic contours can intersect. The question of how Southern Ocean gyres form therefore
458 remains unanswered. Contrary to many existing ideas, the geostrophic contours in Figure 1 suggest
459 that gyres can form in regions of unblocked geostrophic contours.

460 Nadeau and Ferrari (2015) hypothesise that gyre formation in this context is determined by
461 gradients in potential vorticity. However, the effect of increasing gradients in potential vorticity is
462 not fully isolated by Nadeau and Ferrari (2015) because gyre formation is shown to occur through
463 increasing topographic ridge height. Setting up the experiment in this way not only varies gradients
464 in potential vorticity but also the range of blocked geostrophic contours. As highlighted in Figure
465 6, blocked geostrophic contours are known to generate gyres, therefore the relationship to potential
466 vorticity gradients in the results of Nadeau and Ferrari (2015) are unclear. We attempt to confirm
467 the hypothesis of Nadeau and Ferrari (2015) here by creating an experiment whereby topographic
468 gradients are varied without any change in the level of blocked f/H . This is achieved through
469 varying ridge width rather than ridge height in a domain with unblocked geostrophic contours.

470 *b. Unblocked Geostrophic Contours and Topography*

471 The results in Figure 7 indicate that gyres can form without blocking geostrophic contours.
472 Figure 7b shows the 2000 m ridge results from Figure 6. Extending the northern boundary of
473 this case unblocks a large proportion of the geostrophic contours. Previous theory would suggest
474 that a linear free mode would develop and this region of unblocked geostrophic contours would
475 be dominated by an ACC type flow. Contrary to this expectation, sizeable gyres remain. In the
476 extended domain shown by Figures 7c, 7f and 7i, increasing ridge width diminishes the gyres. In
477 concurrence with the uniform wind case presented in Section 3, the net zonal volume transport in
478 Figures 7c, 7f and 7i increases with increased ridge width. The largest ridge width shows very
479 little capability of supporting gyre formation. These results suggest that a submarine ridge can
480 support gyres in regions of unblocked geostrophic contours if the ridge is narrow enough.

481 *c. The Vorticity Balance*

482 The mechanism for the gyres to appear in regions of unblocked geostrophic contours requires
483 a consideration of vorticity. Gyres are absent in results of Section 3 due to a lack of curl in
484 the wind forcing, which would induce vorticity. In classical gyre theory, flow is advected across
485 geostrophic contours in the interior of a basin. This interior flow is generated because of a source
486 of vorticity from a curl in the wind stress (Sverdrup 1947). The flow returns meridionally as a
487 narrow western boundary current, closing the circulation (Stommel 1948). This circulation holds
488 in a flat-bottomed, closed basin where geostrophic contours are strictly zonal, intersecting with
489 the western boundary. For the flow to return across geostrophic contours, a sink of vorticity is
490 required. In the earliest example, this vorticity sink is provided by bottom stress curl (Stommel
491 1948). Later ideas introduce a sloping topography along the western boundary (Holland 1967;
492 Salmon 1992). Over the slope, geostrophic contours are deflected equatorward and flow in the

493 western boundary is quasi-meridional as a result (Salmon 1992; Hughes and De Cuevas 2001;
494 Jackson et al. 2006). With the introduction of topography, the point where geostrophic contours
495 intersect a boundary is not necessarily along the western boundary. The influence of topography
496 could result in this position being along a northern or southern boundary and for this reason the
497 position can be labelled the ‘dynamical west’. Although the paths of the geostrophic contours
498 are altered, the vorticity balance is essentially the same. There is an interior source of vorticity
499 from the wind stress which moves the flow across geostrophic contours. Wherever the geostrophic
500 contours intersect with a boundary, flow is advected back to its original value of f/H due to
501 vorticity generated by bottom stress, which is associated with a lateral shear in the flow (Salmon
502 1992).

503 Although the gyres in Figures 7c, 7f and 7i form in a region of unblocked geostrophic contours,
504 the vorticity balance described above remains. Wind stress curl provides a source of vorticity to
505 flux fluid parcels across geostrophic contours. A sink of vorticity is then required for flow to return
506 across the geostrophic contours and close the circulation. Although classical studies cite bottom
507 stress as the vorticity sink, several terms of the barotropic vorticity equation (3) are capable of
508 taking this role. The vorticity sink can arise through the bottom stress curl ($-\mathbf{k} \cdot \nabla \times \bar{\tau}_b$), eddy
509 inertial term ($\rho_0 \mathbf{k} \cdot \nabla \times (\overline{H\mathbf{u}' \cdot \nabla \mathbf{u}'})$) or lateral viscosity ($\mu \bar{H} \nabla^2 \bar{\zeta}$) (Jackson et al. 2006). The
510 mean inertial term can alter the characteristics of a gyre (Fofonoff 1954; Veronis 1966) but cannot
511 provide a net sink of vorticity. Taking an area integral bounded by a closed streamline, the mean
512 inertial term ($\mathbf{k} \cdot \nabla \times (\overline{H\mathbf{u} \cdot \nabla \mathbf{u}})$) integrates to zero in a steady ocean (Böning 1986; Jackson et al.
513 2006).

514 To investigate the vorticity balance, all terms of the barotropic vorticity equation for the central
515 part of the simulations with unblocked geostrophic contours are shown in Figure 8. In the absence
516 of topography in a channel, the vorticity input via wind stress curl is locally balanced everywhere

517 by bottom stress curl (not shown). The introduction of topography causes this balance to become
518 non-local and much of the wind stress curl is balanced over the topography. The main balance over
519 the topography in Figure 8 is between the advection of planetary vorticity ($-\rho_0 \bar{H} \beta \bar{v}$) and the bot-
520 tom pressure torque ($\mathbf{k} \cdot \nabla \bar{p}_b \times \nabla h$), which is indicative of flow generally following geostrophic
521 contours (Jackson et al. 2006). There is a contribution of vorticity from the mean-inertial term
522 but as discussed above this has no net influence along the entirety of a streamline. The lateral
523 viscosity term is clearly not responsible for the formation of gyres in these experiments as it is
524 negligible in all cases. The vorticity sources from the bottom stress and the eddy inertial terms are
525 non-negligible for these simulations. Both terms increase as ridge width decreases. The dynamics
526 presented suggest that both eddies and bottom stress could be the balancing terms for the vorticity
527 induced by the wind stress. It will be shown below that the same results hold in the absence of
528 eddies with bottom stress providing a sufficient representation of the dynamics.

529 *d. The Details of the Bottom Stress Vorticity Sink*

530 We have shown how the dynamics allow for gyre formation but why gyres form in place of
531 circumpolar flow is yet to be explained. There is an existing suggestion that geostrophic contours
532 are not required to intersect with a boundary for gyres to form in a North Atlantic setting (Salmon
533 1992). Salmon (1992) outlines that the ‘frictional’ (vorticity) balance within a gyre will be met
534 regardless of the topography. Bottom stress curl is dependent on velocity gradients, which are
535 enhanced where geostrophic contours converge. In a domain where geostrophic contours do not
536 intersect with a boundary, the vorticity balance can be met via the generation of bottom stress curl
537 where gradients in geostrophic contours are largest. As a result, the vorticity sink in the results we
538 present occurs on the ridge slope where geostrophic contours converge and gradients in potential
539 vorticity increase.

540 A dynamical difference between the North Atlantic and the Southern Ocean exists due to the
541 presence of the ACC. The entire vorticity sink balancing the wind vorticity source occurs via a
542 western boundary current in the North Atlantic setting, whereas, in the Southern Ocean a propor-
543 tion of this vorticity sink is accounted for by the ACC. Figure 9 shows the bottom stress curl over
544 the topography for two ridge widths. The dominant dipole that spans the ridge is associated with
545 the convergence of the circumpolar current across the topography (Figure 9b), an absent charac-
546 teristic when there is no wind vorticity source (Section 3). The bottom stress curl associated with
547 the gyres is more subtle (Figure 9a, 9c). Figure 9c shows that the vorticity associated with the
548 upslope gyre flow coincides with streamlines crossing geostrophic contours, directed towards the
549 circumpolar current. The flow joins the circumpolar jet, enhancing the vorticity sink generated in
550 the downslope flow. Unlike classical gyre dynamics, both the circumpolar current and the gyres
551 are responsible for balancing the vorticity associated with the wind stress curl.

552 The results suggest that the gyres become increasingly important in balancing the wind vorticity
553 source as the ridge width and circumpolar transport reduces. The vorticity input via the wind
554 is constant between simulations. A reduction in ridge width induces a vorticity sink associated
555 with the gyres, which indicates a reduction in the vorticity sink associated with the circumpolar
556 current. Thus, gyres form and increase in strength with decreasing ridge width to maintain the
557 vorticity balance when the circumpolar current reduces in strength. Momentum conservation is
558 also important to the gyre results and we will discuss this below.

559 *e. The Combined Control of Vorticity and Momentum*

560 The experiments in this study investigate the dynamics of a non-linear system. In general, in-
561 creasing the bottom stress coefficient damps the inertia of a system, reducing the effect of non-
562 linear terms. Figure 10 shows the response of the gyre and circumpolar transport to an increase

563 in the bottom stress coefficient. As the coefficient is increased, the gyre strength increases for
564 the 1000 km and 2000 km wide simulations and remains unchanged for the 4000 km wide ridge.
565 The absence of any notable gyre in the 4000 km case shown by Figure 7i is the reason for the
566 insensitivity of the gyre transport in this case. Figure 10b shows that, in alignment with results of
567 Section 3, the circumpolar transport decreases for all simulations as the bottom stress coefficient
568 is increased. Figure 11 shows the streamfunction and terms of the barotropic vorticity equation for
569 two 2000 km cases shown in Figure 10. The inertial (non-linear) terms become negligible in this
570 case and it is only bottom stress curl that balances the wind stress curl. The fact that the same re-
571 lationships remain in a more linear case show that bottom stress alone is capable of generating the
572 required vorticity sink for the formation of gyres in a region of unblocked geostrophic contours.

573 In the case with a non-zero wind stress curl, the wind stress is a source of both vorticity and
574 momentum and a balance must be achieved for both. In the system presented, bottom stress
575 balances the wind stress in terms of vorticity, which can develop via the circumpolar current and
576 the gyres. In the presence of topography, form stress is the primary balance for the wind stress in
577 terms of momentum. The circumpolar current is not the only route for the generation of form stress
578 across topography. Gyre flow that crosses geostrophic contours along a ridge slope is associated
579 with a pressure difference across the topography (Naveira Garabato et al. 2013). Therefore, gyres
580 are also capable of creating the form stress required to balance the zonal wind stress (Wang and
581 Huang 1995; Naveira Garabato et al. 2013). As gyre transport increases more gyre flow crosses
582 geostrophic contours over the ridge leading to an increase in the form stress associated with the
583 gyres. This indicates that the gyre response not only maintains the balance of vorticity but it
584 also acts to conserve momentum, compensating for changes in form stress associated with the
585 circumpolar current. Figures 10 and 11 highlight that as circumpolar transport reduces, gyres
586 form in order satisfy both vorticity and momentum conservation.

587 *f. The Influence of Topographic Sverdrup Balance*

588 The focus above has been on the momentum and vorticity sinks that are generated over the
589 topography. The presence of gyres results from the curl in the wind stress. The following results
590 suggest that the change in topography also has an effect on the response of the gyres to the wind
591 forcing.

592 Gyres are primarily forced by the wind stress curl over the ocean surface. A reduction in the area
593 over which the gyres are forced implies a reduction in gyre strength (Munk 1950). Topographic
594 Sverdrup balance dictates that wind forcing of a gyre is a function of the wind stress curl between
595 bounding geostrophic contours (Holland 1967). In the blocked simulations (Figure 7b, 7e and
596 7h), the area in which the gyres form reduces with increased ridge width indicating that they are
597 being influenced by a changing topographic Sverdrup balance. Figures 12a-f show the wind stress
598 curl over each gyre shown in Figures 7b, 7e and 7h. The boundary between the two gyres is the
599 geostrophic contour which lies along the line of zero wind stress curl in the flat bottomed part of
600 the domain. The gyres are also bounded by the domain walls and coincident geostrophic contours
601 in the interior. The gyre bounds are deflected equatorward with the geostrophic contours over the
602 topography. The northern gyre emerges due to positive wind stress curl and the southern gyre is
603 due to negative wind stress curl. In all cases, the area of wind forcing over the gyres reduces as
604 ridge width increases. The southern gyre flows into an area of opposing wind stress curl in the
605 northern part of the domain. As a result, there is an additional sink of vorticity in the northern
606 section of the domain which acts in opposition to the prevailing forcing of this gyre. The area of
607 opposing wind stress curl reduces as ridge width reduces. Figure 12g shows the area integral of
608 the wind stress curl over each gyre, normalised against the northern gyre forcing of the narrow
609 ridge simulation. There is a clear reduction in the wind forcing over each gyre as the ridge width

610 is increased. This reduction aligns with the reduction in gyre strength with increased ridge width
611 seen in Figure 12h. This indicates that there is a sensitivity of gyre strength due to a response of
612 the area of wind forcing to the changes in ridge geometry.

613 The grey lines in Figure 12h show that the change in gyre strength is much larger in the ex-
614 tended domain in comparison to results in Figure 12, which has the same wind forcing. Although
615 the topographic Sverdrup balance is shown to have a primary influence on the blocked domain,
616 the difference suggests this is not the case for the extended domain. There is a relationship be-
617 tween ridge width and gyre strength associated with the changes in vorticity and momentum sinks
618 described in the previous sections and changes in topographic Sverdrup balance are indicated to
619 have a second order effect.

620 **5. Discussion**

621 The results presented in this study represent simplified barotropic dynamics. Although the
622 barotropic component of the ACC is not negligible, especially near large topography (Peña-Molino
623 et al. 2014; Donohue et al. 2016), the Southern Ocean is not in the barotropic limit. As a result,
624 some complexities of the Southern Ocean are not represented in our simplified a system. Theories
625 outlined in this paper are intended to enhance our understanding of a more complex, baroclinic
626 eddy system. As such, it is important to discuss how this study might relate to the less idealised
627 setting.

628 We have investigated the non-linear system, where topographic form stress is associated with
629 standing meanders in the lee of topography (Johnson 1977; Stevens and Ivchenko 1997). In many
630 parts of the Southern Ocean, baroclinic Rossby waves are suppressed from westward propagation
631 (Hughes et al. 1998) and standing meanders are predominantly associated with Rossby waves
632 of barotropic wavelength (Hughes 2005; Thompson and Naveira Garabato 2014). Despite the fact

633 that barotropic standing meanders are well captured in our results due to non-linearity, stratification
634 can alter the level of topographic form stress associated with particular stationary Rossby waves
635 (Johnson 1977; Stewart and Hogg 2017). With stratification, the balance of momentum remains
636 between wind stress and topographic form stress but the two are not connected directly. The
637 pressure force associated with topographic form stress is thought to communicate through the
638 water column to the bottom topography via interfacial form stress (Johnson and Bryden 1989).
639 The absence of density variations in our barotropic experiments neglects any representation of
640 interfacial form stress and topographic form stress is a function of the sea surface profile alone. The
641 vertical density structure in the ACC can obscure this surface signal reducing the total topographic
642 form stress contribution to the momentum budget (Stewart and Hogg 2017). This reduction in
643 topographic form stress would indicate a larger volume transport than the barotropic counterpart
644 (Stewart and Hogg 2017). As such, stratification could augment results presented in Section 3.
645 However, this effect is sensitive to the particular density structure and it is also possible for this
646 feature of stratification to have the opposite, or even no effect.

647 Eddy effects are also clearly important to Southern Ocean dynamics (Rintoul 2018) and can
648 be a determining factor of form stress and volume transport. Whilst the simulations presented here
649 show some evidence of eddy motions (for narrow topography in particular), eddies are not a
650 dominant feature. Eddies can influence net zonal volume transport via a processes of ‘eddy satu-
651 ration’ (Straub 1993), where the ACC is observed to be largely insensitive to changes in the wind
652 forcing due to adjustment in the associated eddy kinetic energy (Meredith and Hogg 2006). This
653 is a process that is observed to occur via both baroclinic and barotropic instabilities (Constantinou
654 and Hogg 2019). Instabilities can feed back on meander dynamics and influence topographic form
655 stress (Naveira Garabato et al. 2014; Youngs et al. 2017). However, stability analysis suggests
656 that the amplitude of the topography we present is too large to exhibit significant barotropic eddy

657 saturation (Hart 1979; Constantinou 2018) and the barotropic instabilities that impact the topo-
658 graphic meander are likely missing. One evident result of the lack in eddy kinetic energy is shown
659 by the contrasting relationship observed in Section 3f to previous studies (Tansley and Marshall
660 2001; Nadeau and Straub 2012; Nadeau and Ferrari 2015; Marshall et al. 2017). We expect that an
661 increase in eddy kinetic energy in our results would reverse the sensitivity of the ACC's volume
662 transport to changes in the bottom stress coefficient.

663 Eddy motions also play a role in gyre dynamics. We have confirmed the hypothesis of
664 Nadeau and Ferrari (2015), showing that the required vorticity sink for gyre formation is gener-
665 ated when potential vorticity gradients increase, with no reliance on blocked geostrophic contours.
666 In a barotropic eddy-saturated case, eddies are dominant in diffusing potential vorticity across
667 geostrophic contours (Constantinou 2018). The vorticity sink in our simulations is described in
668 terms of bottom stress but we expect that with a stronger eddy field geostrophic eddies would
669 have a similar effect. An indication of this is given in Figure 8. The Reynolds stresses are en-
670 hanced with reduced topographic width, scaling similarly to bottom stress with changes in ridge
671 topography and diffusing potential vorticity in a similar way. Further evidence points to this re-
672 lationship remaining comparable in the presence baroclinic instabilities with both barotropic and
673 baroclinic eddies become intensified with increased topographic gradients (Barthel et al. 2017).
674 We speculate that in a highly eddy setting the vorticity dynamics we present will remain, with
675 Reynolds stress superseding the role of bottom stress.

676 The Southern Ocean is far from the barotropic limit and the theory presented is not directly
677 applicable due to the lack of baroclinicity and strong eddy effects. However, the aim of our in-
678 vestigation is not to give a realistic representation of the Southern Ocean but to derive some simple
679 relationships that can aid our understanding of the complex system that exists. Despite caveats,
680 our results provide insight into the general process by which Southern Ocean gyres form. Further,

681 we have made a contribution in understanding the role of form stress in flow over topography. The
682 dynamics are expected to change with the introduction of stratification and a strong eddy field. We
683 have identified some of the possible consequences of including these effects. Using our study as
684 a basis, it would be useful for future studies to fully investigate how these effects might influence
685 the relationships we present concerning Southern Ocean flow in regions of unblocked geostrophic
686 contours.

687 **6. Summary**

688 There are many unexplored aspects of topographically influenced flow. This study has sought to
689 investigate the role of varying geometry on flow in the Southern Ocean. A series of experiments
690 are carried out exploring the response of Southern Ocean gyres and the ACC to variations in the
691 width of a meridionally-aligned ridge. Investigation into the direct effects of stratification and
692 eddies has been omitted; it is noted that these are worthy of future investigation. However, our
693 study particularly highlights the dynamical need to balance momentum and vorticity, a general
694 result that would hold regardless of the presence of eddies and baroclinicity.

695 Previous work highlights that topography is highly influential on the dynamics of large-scale
696 flow (Munk and Palmén 1951; Hughes and Killworth 1995). It has long been acknowledged that
697 topography has a large influence on the path of the ACC (Gordon et al. 1978; Killworth 1992).
698 Idealised channel simulations have been carried out of flow over topography to gain insight into
699 ACC dynamics. We build on existing studies by investigating non-linear dynamics in a region
700 of unblocked geostrophic contours. The results show that the volume transport of a barotropic
701 circumpolar current is highly sensitive to ridge width variations. As ridge width is increased there
702 is a large increase in the volume transport. The underlying mechanism for this relationship is
703 shown here to be related to form stress, the primary sink of zonal momentum balancing the zonal

704 wind stress over the the Southern Ocean (Munk and Palmén 1951; Wolff et al. 1991; Stevens
705 and Ivchenko 1997; Masich et al. 2015). The steady-state results show that, for different ridge
706 width variations, the form stress remains the primary sink through an adjustment in the sea surface
707 height profile over the topography. This adjustment is then associated with a change in zonal vol-
708 ume transport with changing ridge width. This indicates that the observed ACC volume transport
709 is determined by the geometry of large-scale topographic features in the Southern Ocean. An ad-
710 ditional relationship has also been observed. As ridge width is increased there is a small reduction
711 in the proportion of wind stress which is balanced by form stress in the zonal momentum balance.
712 This reduction is accounted for by an increase in bottom stress. It is shown that this proportional
713 balance is associated with the volume transport and an increased bottom stress coefficient leads to
714 a reduced volume transport as a result.

715 Established theory bases the formation of Southern Ocean gyres on the intersection of
716 geostrophic contours with a land mass to the ‘dynamical west’ (LaCasce and Isachsen 2010).
717 It is highlighted here that gyre circulations in the Southern Ocean do not necessarily form in this
718 manner. The Ross Gyre forms in the lee of a topographic feature where all geostrophic contours
719 are unblocked. Established theory would suggest that this space should be occupied by the ACC.
720 This study shows that gyres can occur in the absence of geostrophic contours intersecting with
721 boundaries. In the presence of wind forcing with a non-zero curl, the wind stress must be balanced
722 in terms of both momentum and vorticity. The necessary balances for the wind stress can develop
723 through the dynamics of both gyres and the circumpolar current. Zonal momentum constraints are
724 associated with a reduction in circumpolar volume transport with a reduced ridge width, in turn
725 reducing the bottom stress curl. The bottom stress curl must be maintained to balance the wind
726 stress curl and gyres form in order for this to happen. In addition, there is an auxiliary effect of the
727 ridge width variation on the character of gyres. Due to topographic Sverdrup balance, the change

728 in topography alters the geostrophic contours, which is associated with a reduction in the wind
729 forcing of the gyres. The curtailed wind forcing is linked to a reduction in the gyre strength and
730 a proportion of the relationship between ridge width and gyre strength is linked to topographic
731 Sverdrup balance.

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735 **References**

736 Armitage, T. W. K., R. Kwok, A. F. Thompson, and G. Cunningham, 2018: Dynamic topography
737 and sea level anomalies of the Southern Ocean: Variability and teleconnections. *Journal of*
738 *Geophysical Research: Oceans*, **123** (1), 613–630.

739 Barthel, A., A. McC. Hogg, S. Waterman, and S. Keating, 2017: Jet-topography interactions affect
740 energy pathways to the deep Southern Ocean. *Journal of Physical Oceanography*, **47** (7), 1799–
741 1816.

742 Böning, C. W., 1986: On the influence of frictional parameterization in wind-driven ocean circu-
743 lation models. *Dynamics of Atmospheres and Oceans*, **10** (1), 63 – 92.

744 Constantinou, N. C., 2018: A barotropic model of eddy saturation. *Journal of Physical Oceanog-*
745 *raphy*, **48** (2), 397–411.

746 Constantinou, N. C., and A. M. Hogg, 2019: Eddy saturation of the southern ocean: a baroclinic
747 versus barotropic perspective. *Geophysical Research Letters*, **46**.

- 748 Donohue, K. A., K. L. Tracey, D. R. Watts, M. P. Chidichimo, and T. K. Chereskin, 2016: Mean
749 Antarctic Circumpolar Current transport measured in Drake Passage. *Geophysical Research*
750 *Letters*, **43 (22)**, 11,760–11,767.
- 751 Fofonoff, N. P., 1954: Steady flow in a frictionless homogeneous ocean. *Journal of Marine Re-*
752 *search*, **13**, 254–262.
- 753 Gordon, A. L., E. Molinelli, and T. Baker, 1978: Large-scale relative dynamic topography of the
754 Southern Ocean. *Journal of Geophysical Research: Oceans*, **83 (C6)**, 3023–3032.
- 755 Hart, J. E., 1979: Barotropic quasi-geostrophic flow over anisotropic mountains. *Journal of the*
756 *Atmospheric Sciences*, **36 (9)**, 1736–1746.
- 757 Holland, W. R., 1967: On the wind-driven circulation in an ocean with bottom topography. *Tellus*,
758 **19 (4)**, 582–600.
- 759 Holland, W. R., 1972: Baroclinic and topographic influences on the transport in western boundary
760 currents. *Geophysical & Astrophysical Fluid Dynamics*, **4 (1)**, 187–210.
- 761 Hughes, C. W., 2005: Nonlinear vorticity balance of the Antarctic Circumpolar Current. *Journal*
762 *of Geophysical Research: Oceans*, **110 (C11)**, c11008.
- 763 Hughes, C. W., and E. R. Ash, 2001: Eddy forcing of the mean flow in the Southern Ocean.
764 *Journal of Geophysical Research: Oceans*, **106 (C2)**, 2713–2722.
- 765 Hughes, C. W., and B. A. De Cuevas, 2001: Why western boundary currents in realistic oceans are
766 inviscid: A link between form stress and bottom pressure torques. *Journal of Physical Oceanog-*
767 *raphy*, **31 (10)**, 2871–2885.

- 768 Hughes, C. W., M. S. Jones, and S. Carnochan, 1998: Use of transient features to identify eastward
769 currents in the Southern Ocean. *Journal of Geophysical Research: Oceans*, **103 (C2)**, 2929–
770 2943.
- 771 Hughes, C. W., and P. D. Killworth, 1995: Effects of bottom topography in the large-scale circu-
772 lation of the Southern Ocean. *Journal of Physical Oceanography*, **25 (11)**, 2485–2497.
- 773 Hughes, C. W., M. P. Meredith, and K. J. Heywood, 1999: Wind-driven transport fluctuations
774 through drake passage: A southern mode. *Journal of Physical Oceanography*, **29 (8)**, 1971–
775 1992.
- 776 Jackson, L., C. W. Hughes, and R. G. Williams, 2006: Topographic control of basin and channel
777 flows: The role of bottom pressure torques and friction. *Journal of Physical Oceanography*,
778 **36 (9)**, 1786–1805.
- 779 Johnson, E. R., 1977: Stratified Taylor columns on a beta-plane. *Geophysical & Astrophysical*
780 *Fluid Dynamics*, **9 (1)**, 159–177.
- 781 Johnson, G. C., and H. L. Bryden, 1989: On the size of the Antarctic Circumpolar Current. *Deep*
782 *Sea Research Part A. Oceanographic Research Papers*, **36 (1)**, 39 – 53.
- 783 Johnson, J., and R. Hill, 1975: A three-dimensional model of the Southern Ocean with bottom
784 topography. *Deep Sea Research and Oceanographic Abstracts*, **22 (11)**, 745 – 751.
- 785 Killworth, P. D., 1992: An equivalent-barotropic mode in the Fine Resolution Antarctic Model.
786 *Journal of Physical Oceanography*, **22 (11)**, 1379–1387.
- 787 Krupitsky, A., and M. A. Cane, 1994: On topographic pressure drag in a zonal channel. *Journal*
788 *of Marine Research*, **52 (1)**, 1–23.

- 789 Krupitsky, A., V. M. Kamenkovich, N. Naik, and M. A. Cane, 1996: A Linear Equivalent
790 Barotropic Model of the Antarctic Circumpolar Current with Realistic Coastlines and Bottom
791 Topography. *Journal of Physical Oceanography*, **26 (9)**, 1803–1824.
- 792 LaCasce, J., and P. Isachsen, 2010: The linear models of the ACC. *Progress in Oceanography*,
793 **84 (3)**, 139 – 157.
- 794 Marshall, D., 1995: Topographic steering of the Antarctic Circumpolar Current. *Journal of Phys-
795 ical Oceanography*, **25 (7)**, 1636–1650.
- 796 Marshall, D. P., M. H. P. Ambaum, J. R. Maddison, D. R. Munday, and L. Novak, 2017: Eddy satu-
797 ration and frictional control of the antarctic circumpolar current. *Geophysical Research Letters*,
798 **44 (1)**, 286–292.
- 799 Marshall, J., A. Adcroft, C. Hill, L. Perelman, and C. Heisey, 1997a: A finite-volume, incompress-
800 ible Navier Stokes model for studies of the ocean on parallel computers. *Journal of Geophysical
801 Research: Oceans*, **102 (C3)**, 5753–5766.
- 802 Marshall, J., C. Hill, L. Perelman, and A. Adcroft, 1997b: Hydrostatic, quasi-hydrostatic, and
803 nonhydrostatic ocean modeling. *Journal of Geophysical Research: Oceans*, **102 (C3)**, 5733–
804 5752.
- 805 Masich, J., T. K. Chereskin, and M. R. Mazloff, 2015: Topographic form stress in the Southern
806 Ocean State Estimate. *Journal of Geophysical Research: Oceans*, **120 (12)**, 7919–7933.
- 807 McCartney, M., 1976: The interaction of zonal currents with topography with applications to the
808 Southern Ocean. *Deep Sea Research and Oceanographic Abstracts*, **23 (5)**, 413 – 427.
- 809 Meredith, M. P., and A. M. Hogg, 2006: Circumpolar response of Southern Ocean eddy activity
810 to a change in the Southern Annular Mode. *Geophysical Research Letters*, **33 (16)**.

- 811 Munday, D. R., H. L. Johnson, and D. P. Marshall, 2015: The role of ocean gateways in the dynam-
812 ics and sensitivity to wind stress of the early Antarctic Circumpolar Current. *Paleoceanography*,
813 **30 (3)**, 284–302.
- 814 Munk, W. H., 1950: On the wind-driven ocean circulation. *Journal of Meteorology*, **7 (2)**, 80–93.
- 815 Munk, W. H., and E. Palmén, 1951: Note on the dynamics of the Antarctic Circumpolar Current.
816 *Tellus*, **3 (1)**, 53–55.
- 817 Nadeau, L.-P., and R. Ferrari, 2015: The role of closed gyres in setting the zonal transport of the
818 Antarctic Circumpolar Current. *Journal of Physical Oceanography*, **45 (6)**, 1491–1509.
- 819 Nadeau, L.-P., and D. N. Straub, 2012: Influence of wind stress, wind stress curl, and bottom fric-
820 tion on the transport of a model Antarctic Circumpolar Current. *Journal of Physical Oceanog-*
821 *raphy*, **42 (1)**, 207–222.
- 822 Naveira Garabato, A. C., A. G. Nurser, R. B. Scott, and J. A. Goff, 2013: The impact of small-
823 scale topography on the dynamical balance of the ocean. *Journal of Physical Oceanography*,
824 **43 (3)**, 647–668.
- 825 Naveira Garabato, A. C., A. P. Williams, and S. Bacon, 2014: The three-dimensional overturning
826 circulation of the Southern Ocean during the WOCE era. *Progress in Oceanography*, **120**, 41 –
827 78.
- 828 Orsi, A. H., T. Whitworth, and W. D. Nowlin, 1995: On the meridional extent and fronts of the
829 Antarctic Circumpolar Current. *Deep Sea Research Part I: Oceanographic Research Papers*,
830 **42 (5)**, 641 – 673.
- 831 Patmore, R. D., 2018: Topographic control of Southern Ocean gyres and the Antarctic Circumpo-
832 lar Current. Ph.D. thesis, University of Southampton.

- 833 Peña-Molino, B., S. R. Rintoul, and M. R. Mazloff, 2014: Barotropic and baroclinic contributions
834 to along-stream and across-stream transport in the Antarctic Circumpolar Current. *Journal of*
835 *Geophysical Research: Oceans*, **119** (11), 8011–8028.
- 836 Read, P., P. Rhines, and A. White, 1986: Geostrophic scatter diagrams and potential vorticity
837 dynamics. *Journal of the Atmospheric Sciences*, **43** (24), 3226–3240.
- 838 Rintoul, S. R., 2018: The global influence of localized dynamics in the southern ocean. *Nature*,
839 **558** (7709), 209.
- 840 Rossby, C.-G., 1936: *Dynamics of steady ocean currents in the light of experimental fluid mechan-*
841 *ics*, Vol. 1. Massachusetts Institute of Technology and Woods Hole Oceanographic Institution.
- 842 Rossby, C.-G., and Coauthors, 1940: Planetary flow patterns in the atmosphere. *Quarterly Journal*
843 *of the Royal Meteorological Society*, **66**, 68–87.
- 844 Salmon, R., 1992: A two-layer Gulf Stream over a continental slope. *Journal of Marine Research*,
845 **50** (3), 341–365.
- 846 Speer, K., S. R. Rintoul, and B. Sloyan, 2000: The diabatic Deacon cell. *Journal of Physical*
847 *Oceanography*, **30** (12), 3212–3222.
- 848 Stevens, D. P., and V. O. Ivchenko, 1997: The zonal momentum balance in an eddy-resolving
849 general-circulation model of the Southern Ocean. *Quarterly Journal of the Royal Meteorologi-*
850 *cal Society*, **123** (540), 929–951.
- 851 Stewart, A. L., and A. M. Hogg, 2017: Reshaping the Antarctic Circumpolar Current via Antarctic
852 Bottom Water export. *Journal of Physical Oceanography*, **47** (10), 2577–2601.
- 853 Stommel, H., 1948: The westward intensification of wind-driven ocean currents. *Eos, Transac-*
854 *tions American Geophysical Union*, **29** (2), 202–206.

- 855 Straub, D. N., 1993: On the transport and angular momentum balance of channel models of the
856 Antarctic Circumpolar Current. *Journal of Physical Oceanography*, **23** (4), 776–782.
- 857 Sverdrup, H. U., 1947: Wind-driven currents in a baroclinic ocean; with application to the equa-
858 torial currents of the eastern Pacific. *Proceedings of the National Academy of Sciences*, **33** (11),
859 318–326.
- 860 Talley, L. D., 2013: Closure of the global overturning circulation through the Indian, Pacific, and
861 Southern oceans: Schematics and transports. *Oceanography*, **26**, URL [https://doi.org/10.5670/](https://doi.org/10.5670/oceanog.2013.07)
862 [oceanog.2013.07](https://doi.org/10.5670/oceanog.2013.07).
- 863 Tansley, C. E., and D. P. Marshall, 2001: On the dynamics of wind-driven circumpolar currents.
864 *Journal of Physical Oceanography*, **31** (11), 3258–3273.
- 865 Thompson, A. F., and A. C. Naveira Garabato, 2014: Equilibration of the Antarctic Circumpolar
866 Current by standing meanders. *Journal of Physical Oceanography*, **44** (7), 1811–1828.
- 867 Thompson, A. F., and K. J. Richards, 2011: Low frequency variability of Southern Ocean jets.
868 *Journal of Geophysical Research: Oceans*, **116** (C9).
- 869 Treguier, A. M., and J. C. McWilliams, 1990: Topographic influences on wind-driven, stratified
870 flow in a β -plane channel: An idealized model for the antarctic circumpolar current. *Journal of*
871 *Physical Oceanography*, **20** (3), 321–343.
- 872 Veronis, G., 1966: Wind-driven ocean circulation - part 2. numerical solutions of the non-linear
873 problem. *Deep Sea Research and Oceanographic Abstracts*, **13** (1), 31 – 55.
- 874 Wang, L., and R. X. Huang, 1995: A linear homogeneous model of wind-driven circulation in a
875 β -plane channel. *Journal of Physical Oceanography*, **25** (4), 587–603.

- 876 Wolff, J.-O., E. Maier-Reimer, and D. J. Olbers, 1991: Wind-driven flow over topography in
877 a zonal β -plane channel: A quasi-geostrophic model of the Antarctic Circumpolar Current.
878 *Journal of Physical Oceanography*, **21** (2), 236–264.
- 879 Youngs, M. K., A. F. Thompson, A. Lazar, and K. J. Richards, 2017: ACC Meanders, energy
880 transfer, and mixed barotropic-baroclinic instability. *Journal of Physical Oceanography*, **47** (6),
881 1291–1305.

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883 **Table 1.** List of all model configurations. The columns represent: model identification
884 number; zonal length of domain; meridional width of domain; existence of
885 central meridional wall; height of submarine topography; width of submarine
886 topography; ‘Curl’ for the sinusoidal wind forcing and ‘Uniform’ for uniform
887 surface wind forcing; prescribed bottom stress coefficient. 42

888 TABLE 1. List of all model configurations. The columns represent: model identification number; zonal length
889 of domain; meridional width of domain; existence of central meridional wall; height of submarine topography;
890 width of of submarine topography; ‘Curl’ for the sinusoidal wind forcing and ‘Uniform’ for uniform surface
891 wind forcing; prescribed bottom stress coefficient.

ID	L_x	L_y	Wall	Ridge Height	Ridge Width	Wind	C_d
01	7200 km	7200 km	n	2000 m	500 km	Uniform	0.0025
02	7200 km	7200 km	n	2000 m	1000 km	Uniform	0.0025
03	7200 km	7200 km	n	2000 m	1500 km	Uniform	0.0025
04	7200 km	7200 km	n	2000 m	2000 km	Uniform	0.0025
05	7200 km	7200 km	n	2000 m	2500 km	Uniform	0.0025
06	7200 km	7200 km	n	2000 m	3000 km	Uniform	0.0025
07	7200 km	7200 km	n	2000 m	3500 km	Uniform	0.0025
08	7200 km	7200 km	n	2000 m	4000 km	Uniform	0.0025
09	7200 km	7200 km	n	2000 m	1000 km	Uniform	0.0050
10	7200 km	7200 km	n	2000 m	1000 km	Uniform	0.0075
11	7200 km	7200 km	n	2000 m	2000 km	Uniform	0.0050
12	7200 km	7200 km	n	2000 m	2000 km	Uniform	0.0075
13	7200 km	7200 km	n	2000 m	4000 km	Uniform	0.0050
14	7200 km	7200 km	n	2000 m	4000 km	Uniform	0.0075
15	7200 km	3600 km	n	0 m	1000 km	Curl	0.0025
16	7200 km	3600 km	n	500 m	1000 km	Curl	0.0025
17	7200 km	3600 km	n	1000 m	1000 km	Curl	0.0025
18	7200 km	3600 km	n	2000 m	1000 km	Curl	0.0025
19	7200 km	3600 km	y	2000 m	1000 km	Curl	0.0025
20	7200 km	3600 km	n	2000 m	2000 km	Curl	0.0025
21	7200 km	3600 km	n	2000 m	4000 km	Curl	0.0025
22	7200 km	7200 km	n	2000 m	1000 km	Curl	0.0025
23	7200 km	7200 km	n	2000 m	2000 km	Curl	0.0025
24	7200 km	7200 km	n	2000 m	4000 km	Curl	0.0025
25	7200 km	7200 km	n	2000 m	1000 km	Curl	0.0050
26	7200 km	7200 km	n	2000 m	2000 km	Curl	0.0050
27	7200 km	7200 km	n	2000 m	4000 km	Curl	0.0050

892 **LIST OF FIGURES**

- 893 **Fig. 1.** f/h for the Southern Hemisphere with ocean fronts and gyre contours overlaid. f/h shading
 894 is bounded by the f/h values used in Marshall (1995). The three ACC fronts are plotted
 895 using data from Orsi et al. (1995) and are defined as: the Subantarctic Front (SAF), the
 896 Polar Front (PF) and the Southern Antarctic Circumpolar Current Front (SACCF). The two
 897 gyres, the Weddell Gyre (WG) and the Ross Gyre (RG), are plotted using recent satellite
 898 data from Armitage et al. (2018). 46
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 902 geostrophic (f/h) contours. The beige fill represents any region of unblocked geostrophic
 903 contours, defined by contours which do not intersect with the model walls to the north or
 904 south. The box to the top-left of (a)-(c) signifies the contour spacing of the streamfunction.
 905 (d)-(f) show the topographic profiles of (a)-(c) respectively. The coloured box to the top-
 906 right of (d)-(f) is associated with ridge width. This colour association remains throughout
 907 this study. (g) Net zonal volume transport against ridge width for models 01-08. (h) Domain
 908 integral of terms in the zonal momentum budget for varying ridge width for models 01-08.
 909 The momentum terms shown are: the negative of the form stress ($-\int \bar{p}_b \cdot \partial h / \partial x dA$); the
 910 wind stress ($\int \bar{\tau}_w^x dA$) and the sum of the negative of the form stress and the bottom stress
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 915 downwards arrows signify that the pressure is larger on the western ridge flank than the
 916 eastern flank leading to a net westward force, which is associated with form stress. (b), (c)
 917 Mechanisms for changes in form stress arising from adjustments in sea surface height. (b)
 918 Shows a form stress reduction through a reduced lateral offset in the sea surface height with
 919 respect to the topographic ridge. (c) Shows a form stress reduction via a reduced dip in the
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 924 velocities. True distances are given for the x-axes in (a) and (b), whereas in (c), the x-axis
 925 is scaled to the ridge width of each simulation. 49
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 927 (models 02, 04, 08 and 09-14). Grey dots represent data shown in Figure 2. (b) Domain inte-
 928 gral of terms in the zonal momentum budget for varying ridge width and bottom stress coef-
 929 ficient. The momentum terms shown are: the negative of the form stress ($-\int \bar{p}_b \cdot \partial h / \partial x dA$);
 930 the wind stress ($\int \bar{\tau}_w^x dA$) and the sum of the negative of the form stress and the bottom stress
 931 ($-\int \bar{p}_b \cdot \partial h / \partial x + \bar{\tau}_b^x dA$). (c) Meridionally integrated sea surface height for varying ridge
 932 width and bottom stress coefficient. (d) Meridionally integrated sea surface height near the
 933 ridge peak. The dots represent the minima of the curves. 50
- 934 **Fig. 6.** Plan view of the barotropic streamfunction for channel simulations with a meridional ridge
 935 topography varying in height (models 15-19). A side profile from the south is shown in (a),
 936 (c), (e), (g) and (i) to highlight the topography. The ridge heights are: (a,b) 0 m (model 15),
 937 (c,d) 500 m (model 16), (e,f) 1000 m (model 17), (g,h) 2000 m (model 18) and (i,j) 2000
 938 m (model 19). Result (i,j) has a meridional wall over the ridge peak reaching the ocean

939 surface. The coloured boxes to the top-right of (a), (c), (e), (g) and (i) are associated with
 940 ridge width. For colouring and contouring see Figure 2. The broken streamlines represent
 941 circumpolar flow and the solid streamlines represent stationary eddies or gyre flow. 51

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 943 (b), (e) and (h) show results for a 2000 m ridge height with 3600 km meridional extent
 944 (models 18, 20 and 21 respectively). The grey section signifies land. (c), (f) and (i) show
 945 results for a 2000 m ridge height with 7200 km meridional extent (models 22, 23
 946 and 24 respectively). The ridge widths are: (b,c) 1000 km, (e,f) 2000 km and (h,i) 4000
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 948 top-right of (a), (d) and (g) are associated with ridge width. For colouring and contouring
 949 see Figure 2. The broken streamlines represent circumpolar flow and the solid streamlines
 950 represent stationary eddies or gyre flow. 52

951 **Fig. 8.** Terms of the barotropic vorticity equation for the extended simulations shown in Figure 7
 952 (models 22-24). Simulations have a meridionally aligned ridge of 2000 m in height and of
 953 varying ridge widths. Rows are associated with particular ridge widths (model 22: 1000
 954 km, model 23: 2000 km and model 24: 4000 km). Columns represent differing barotropic
 955 vorticity terms: mean inertial term, eddy vorticity flux, advection of planetary vorticity,
 956 bottom pressure torque, wind stress curl, bottom stress curl and viscosity. The coloured
 957 boxes to the left of (a), (h) and (o) are associated with ridge width. 53

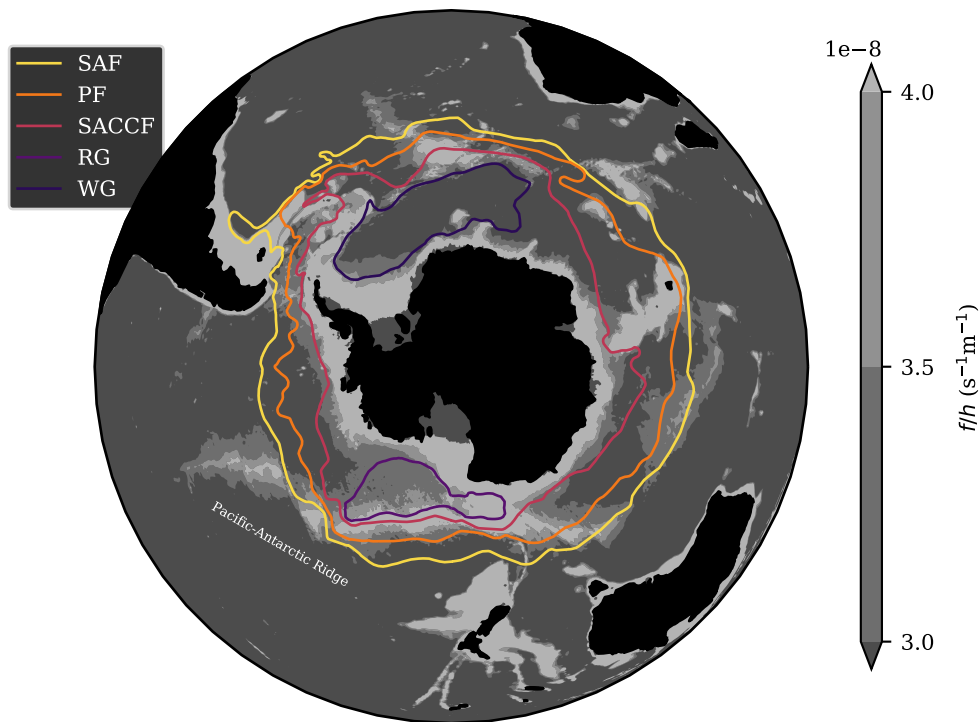
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 960 km respectively. Solid grey lines in (a) and (b) are contours of f/h . (c) shows $\mathbf{k} \cdot \nabla \times \boldsymbol{\tau}_b$
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 962 overlaid in black. The broken black streamlines represent circumpolar flow and the solid
 963 black streamlines represent stationary eddies or gyre flow. Broken grey lines in (c) are
 964 contours of f/h . The box to the top-right of (c) shows the streamline spacing in Sverdrups.
 965 The coloured boxes above (a)-(c) are associated with ridge width. 54

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 967 0.0050 (models 22-27). The simulations with bottom stress coefficient of 0.0025 are same
 968 as presented in Figures 7c, 7f, 7i and 8. (a) Gyre strength versus ridge width for varying
 969 bottom stress coefficient. (b) Circumpolar transport versus ridge width for varying bottom
 970 stress coefficient. 55

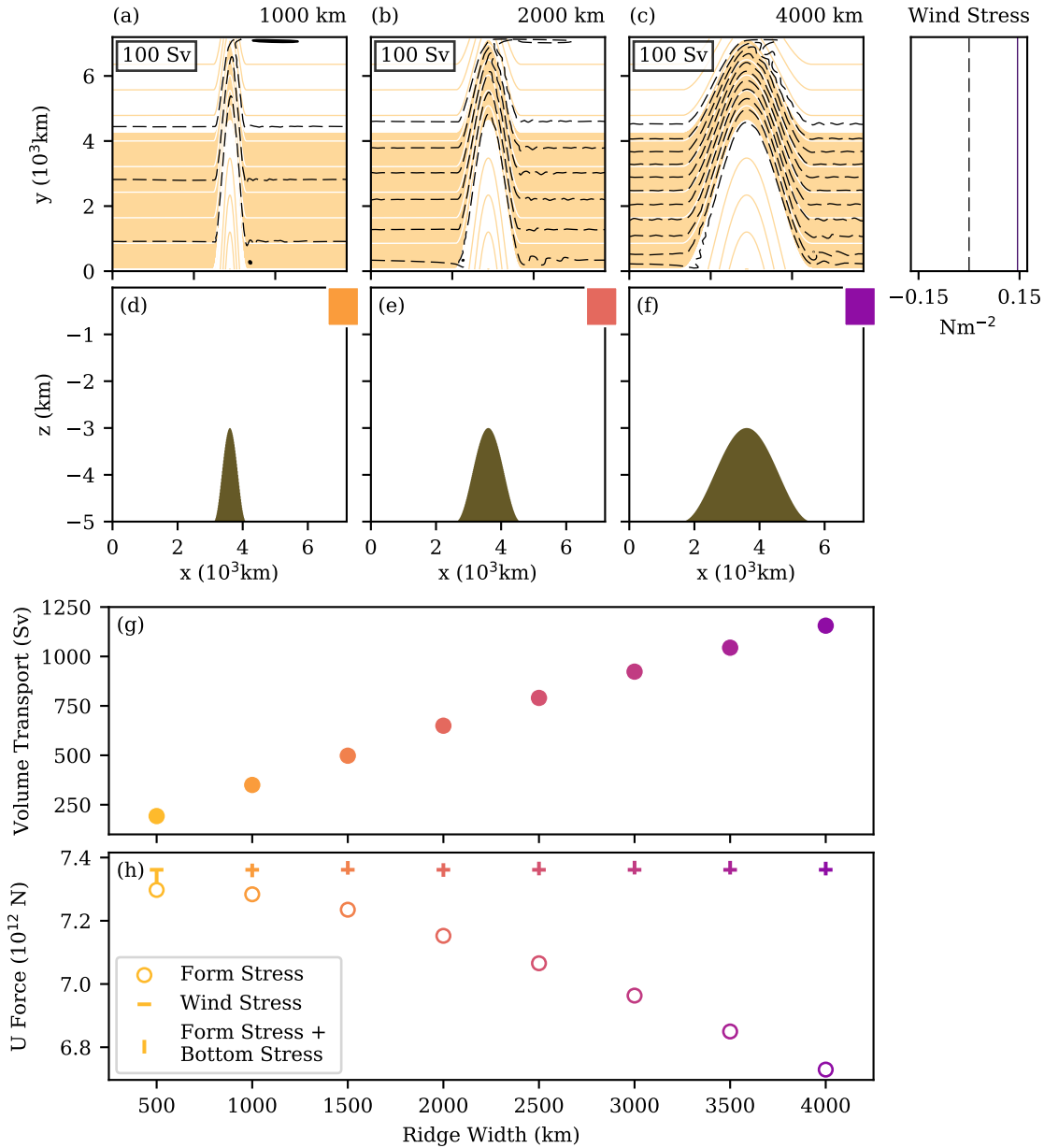
971 **Fig. 11.** Barotropic streamfunction and terms of the barotropic vorticity equation for simulations
 972 with a meridionally aligned ridge of 2000 m in height 2000 km in width. Results are for
 973 model simulations 23 and 26 shown in Figure 10 with varying bottom stress coefficient
 974 (C_d). (a) and (b) show the barotropic streamfunction of results with bottom stress coefficient
 975 of 0.0025 and 0.0050 respectively. For colouring and contouring see Figure 2. The broken
 976 streamlines represent circumpolar flow and the solid streamlines represent stationary eddies
 977 or gyre flow. Rows of panels (c)-(p) are associated with a particular bottom stress coefficient
 978 ((c)-(i): 0.0025 and (j)-(p): 0.0050). Columns of panels (c)-(p) represent differing barotropic
 979 vorticity terms: mean inertial term, eddy vorticity flux, advection of planetary vorticity,
 980 bottom pressure torque, wind stress curl, bottom stress curl and viscosity. The coloured
 981 boxes above (a) and (b) then to the left of (c) and (j) are associated with ridge width. 56

982 **Fig. 12.** The wind stress curl over each gyre in Figures 7b (model 18), 7e (model 20) and 7h (model
 983 21). (a)-(f) show a plan view of the wind forcing over each gyre with ridge width displayed
 984 in the top-right of each plot. (g) shows an area integral of the forcing in (a)-(f) normalised
 985 to the area integral for (b). (h) shows the gyre strength versus ridge width. The grey lines in

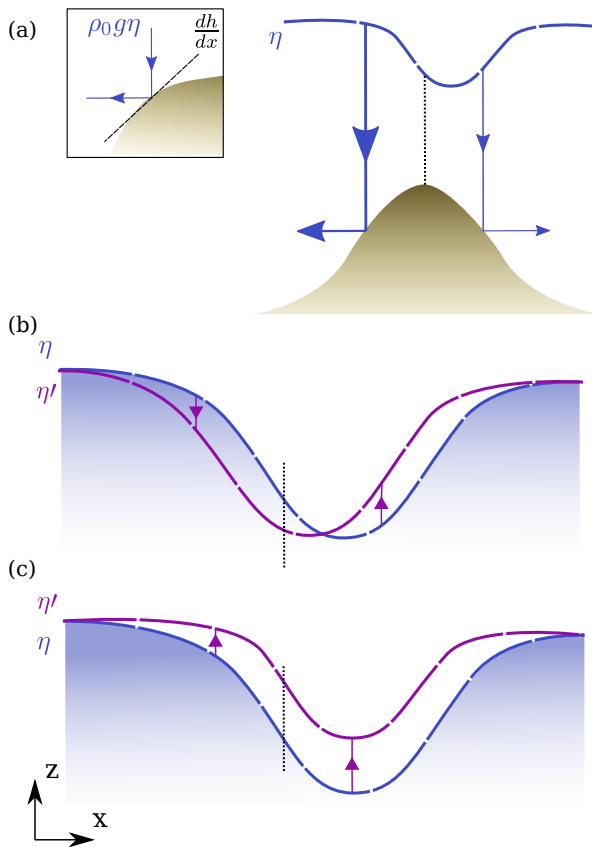
986 (h) correspond to the normalised gyre strength of models 22-24 where the meridional extent
987 is 7200 km (See Figures 7c, 7f and 7i). The coloured boxes to the left of (a), (c) and (e) are
988 associated with ridge width. 57



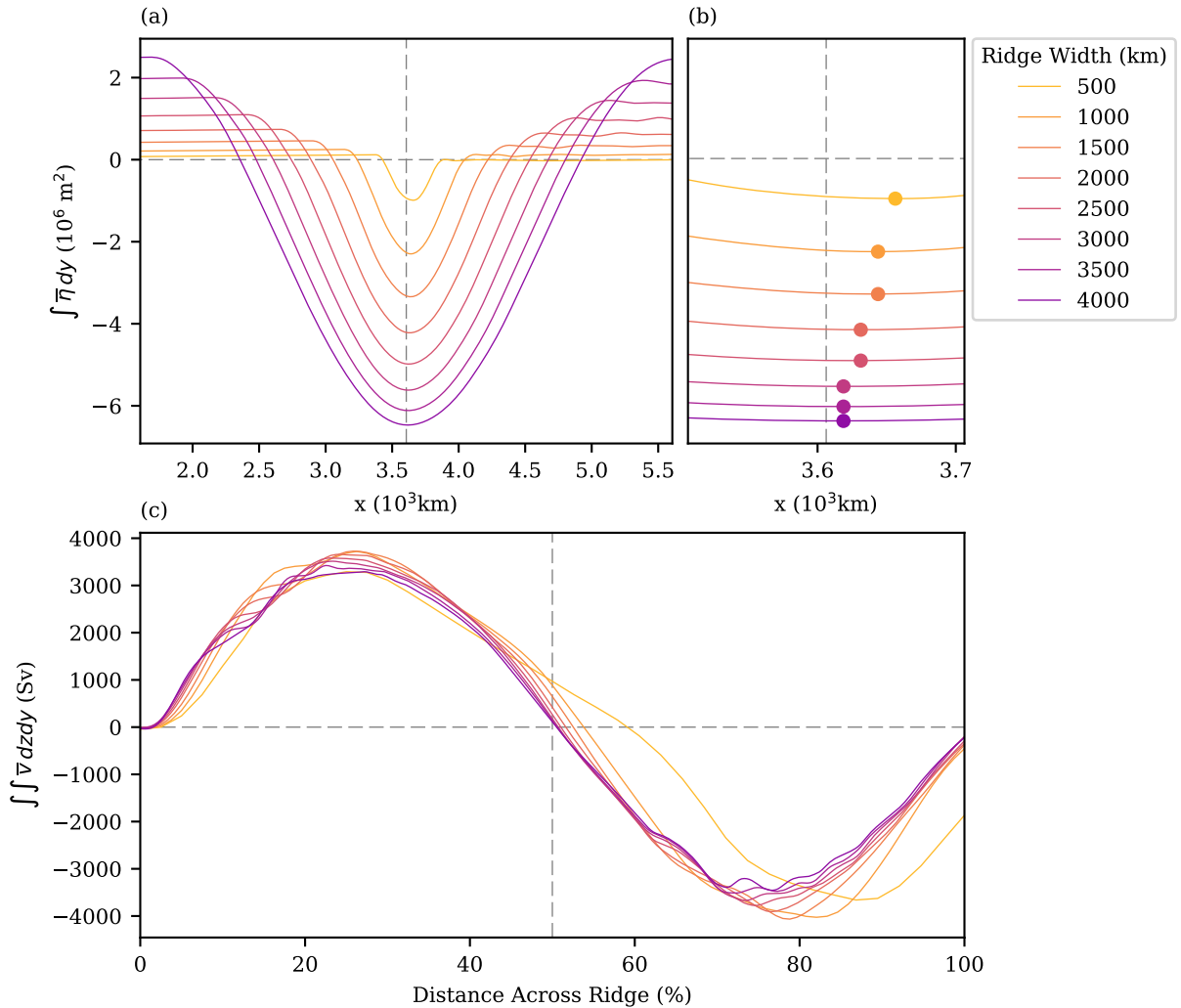
989 FIG. 1. f/h for the Southern Hemisphere with ocean fronts and gyre contours overlaid. f/h shading is
 990 bounded by the f/h values used in Marshall (1995). The three ACC fronts are plotted using data from Orsi
 991 et al. (1995) and are defined as: the Subantarctic Front (SAF), the Polar Front (PF) and the Southern Antarctic
 992 Circumpolar Current Front (SACCF). The two gyres, the Weddell Gyre (WG) and the Ross Gyre (RG), are
 993 plotted using recent satellite data from Armitage et al. (2018).



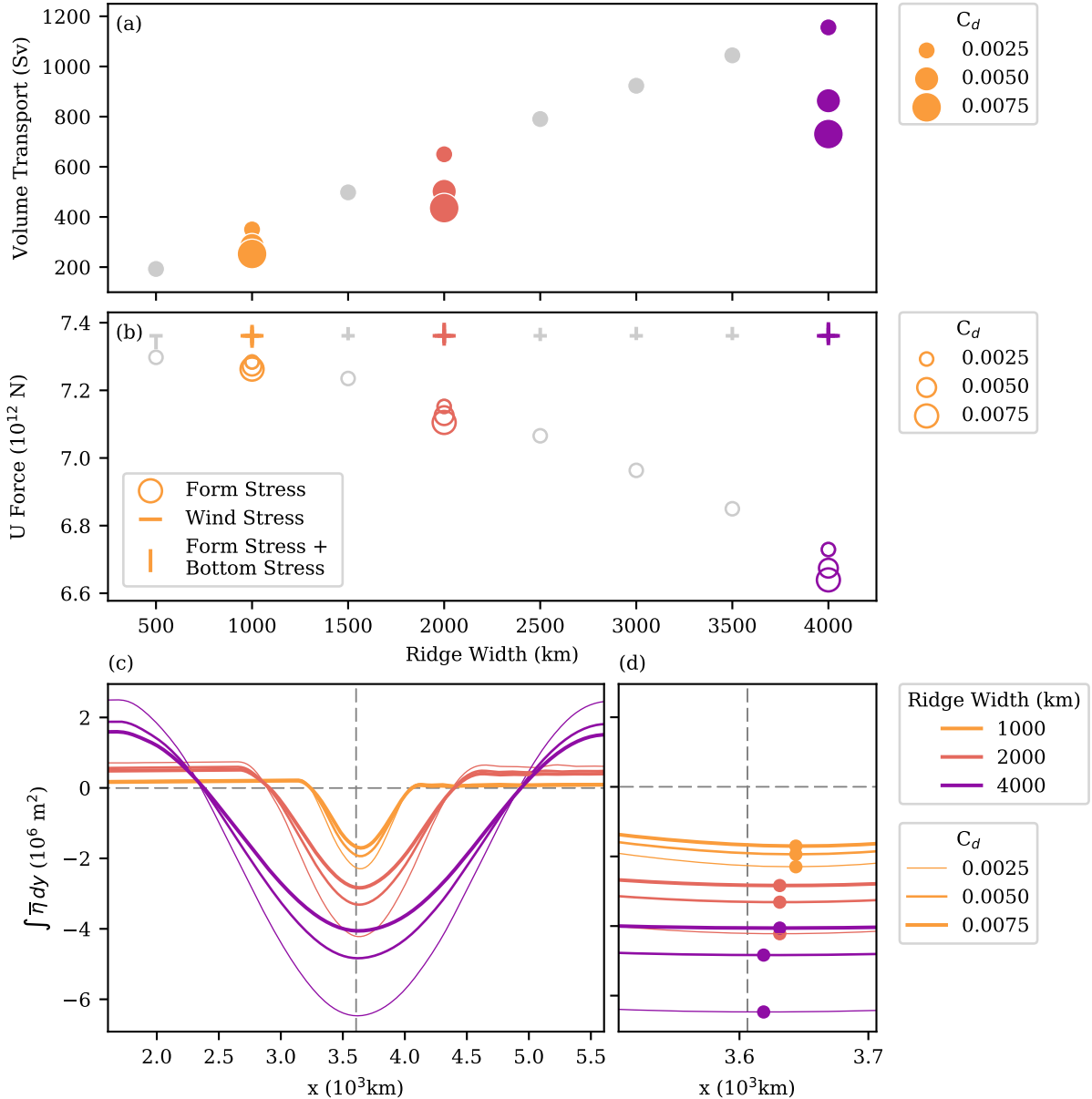
994 FIG. 2. Results for ridge width variations with uniform wind forcing for models 01-08. (a)-(c) The barotropic
 995 streamfunction for 3 ridge widths: (a) 1000 km (model 02), (b) 2000 km (model 04) and (c) 4000 km (model 08).
 996 Black lines are streamlines. Beige/white lines represent geostrophic (f/h) contours. The beige fill represents any
 997 region of unblocked geostrophic contours, defined by contours which do not intersect with the model walls to the
 998 north or south. The box to the top-left of (a)-(c) signifies the contour spacing of the streamfunction. (d)-(f) show
 999 the topographic profiles of (a)-(c) respectively. The coloured box to the top-right of (d)-(f) is associated with
 1000 ridge width. This colour association remains throughout this study. (g) Net zonal volume transport against ridge
 1001 width for models 01-08. (h) Domain integral of terms in the zonal momentum budget for varying ridge width for
 1002 models 01-08. The momentum terms shown are: the negative of the form stress ($-\int \bar{p}_b \cdot \partial h / \partial x dA$); the wind
 1003 stress ($\int \bar{\tau}_w^x dA$) and the sum of the negative of the form stress and the bottom stress ($-\int \bar{p}_b \cdot \partial h / \partial x + \bar{\tau}_b^x dA$).



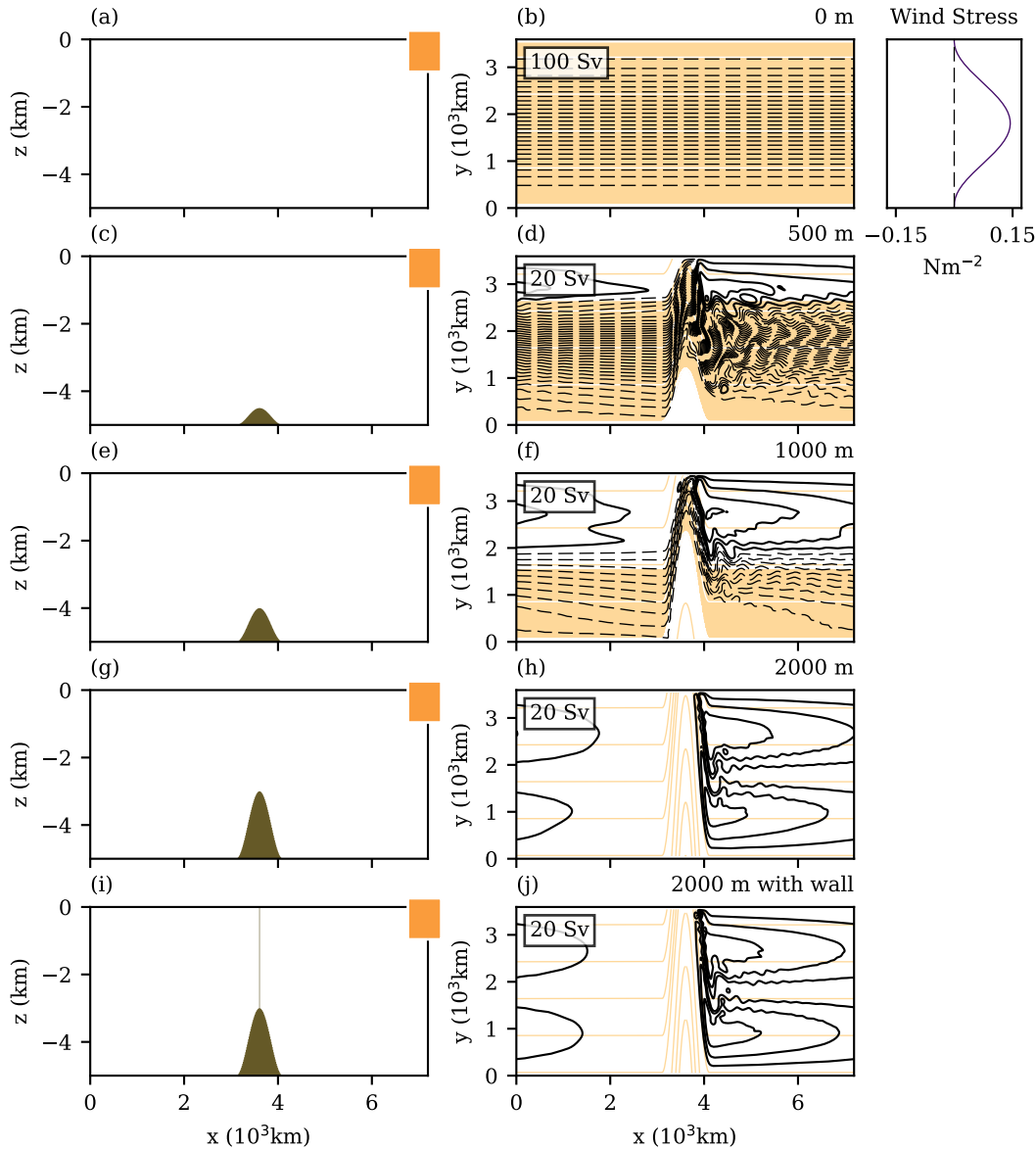
1004 FIG. 3. (a) Schematic representation of form stress. A lateral offset in the sea surface causes the water column
 1005 to be thicker on the western ridge flank than the eastern flank. The difference in water column thickness is
 1006 associated with a pressure difference across the ridge. The downwards arrows signify that the pressure is larger
 1007 on the western ridge flank than the eastern flank leading to a net westward force, which is associated with form
 1008 stress. (b), (c) Mechanisms for changes in form stress arising from adjustments in sea surface height. (b) Shows
 1009 a form stress reduction through a reduced lateral offset in the sea surface height with respect to the topographic
 1010 ridge. (c) Shows a form stress reduction via a reduced dip in the sea surface height. The vertical line represents
 1011 the location of the ridge peak.



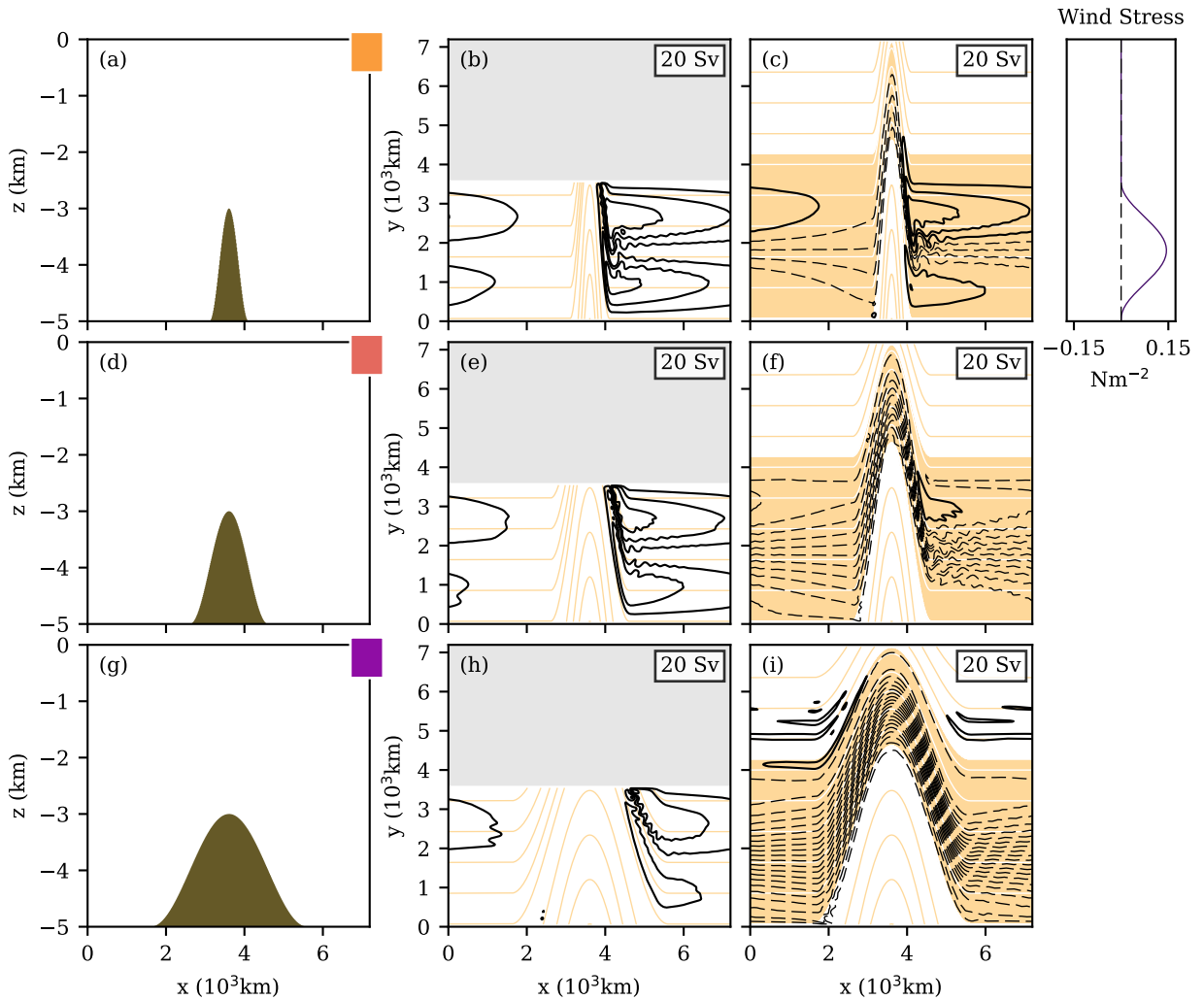
1012 FIG. 4. Meridionally integrated quantities for varying ridge width (models 01-08). (a) Meridionally integrated
 1013 sea surface height. (b) Meridionally integrated sea surface height near the ridge peak. The dots represent the
 1014 minima of the curves. (c) Meridionally integrated meridional velocities. True distances are given for the x-axes
 1015 in (a) and (b), whereas in (c), the x-axis is scaled to the ridge width of each simulation.



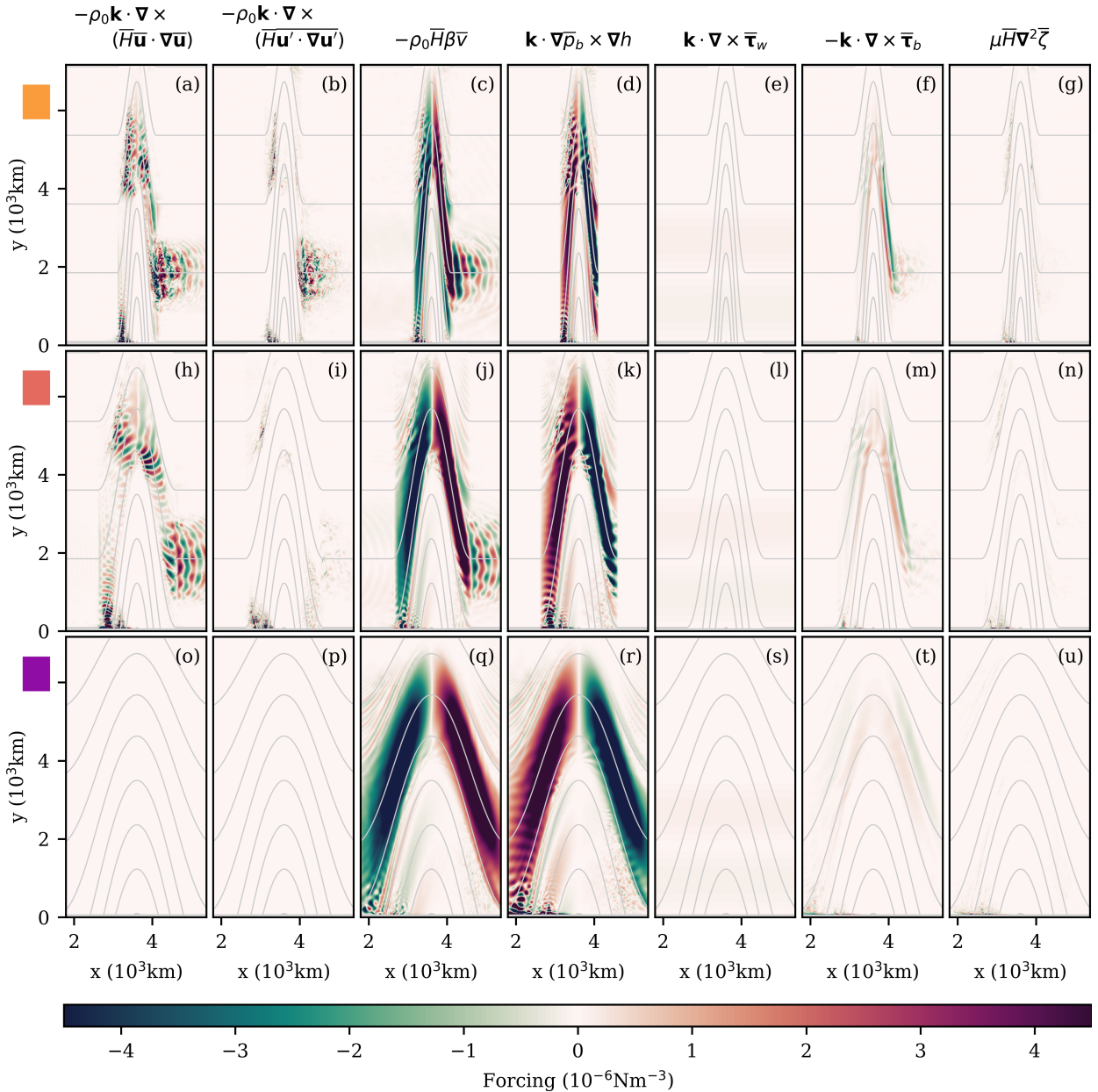
1016 FIG. 5. (a) Net zonal volume transport against ridge width for varying bottom stress coefficient (models 02,
 1017 04, 08 and 09-14). Grey dots represent data shown in Figure 2. (b) Domain integral of terms in the zonal
 1018 momentum budget for varying ridge width and bottom stress coefficient. The momentum terms shown are: the
 1019 negative of the form stress ($-\int \bar{p}_b \cdot \partial h / \partial x dA$); the wind stress ($\int \bar{\tau}_w^x dA$) and the sum of the negative of the form
 1020 stress and the bottom stress ($-\int \bar{p}_b \cdot \partial h / \partial x + \bar{\tau}_b^x dA$). (c) Meridionally integrated sea surface height for varying
 1021 ridge width and bottom stress coefficient. (d) Meridionally integrated sea surface height near the ridge peak.
 1022 The dots represent the minima of the curves.



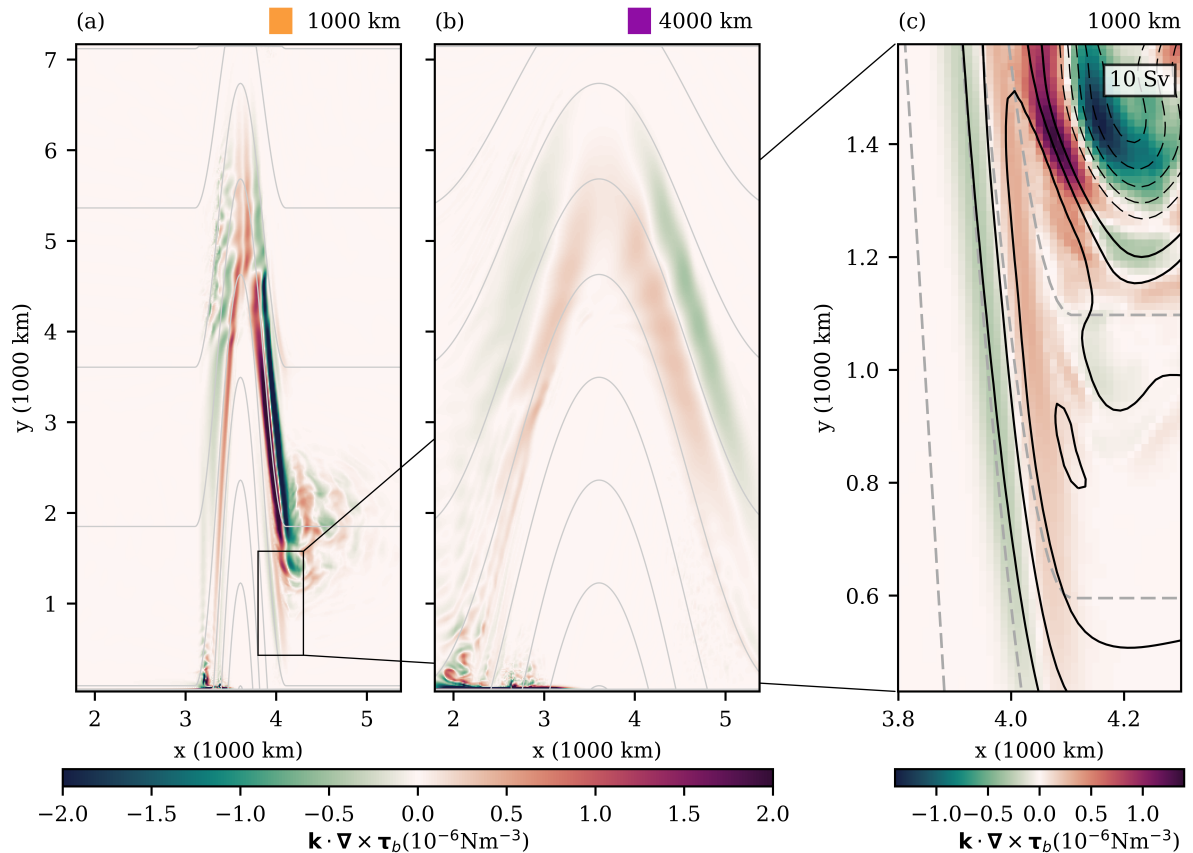
1023 FIG. 6. Plan view of the barotropic streamfunction for channel simulations with a meridional ridge topography
 1024 varying in height (models 15-19). A side profile from the south is shown in (a), (c), (e), (g) and (i) to highlight
 1025 the topography. The ridge heights are: (a,b) 0 m (model 15), (c,d) 500 m (model 16), (e,f) 1000 m (model 17),
 1026 (g,h) 2000 m (model 18) and (i,j) 2000 m (model 19). Result (i,j) has a meridional wall over the ridge peak
 1027 reaching the ocean surface. The coloured boxes to the top-right of (a), (c), (e), (g) and (i) are associated with
 1028 ridge width. For colouring and contouring see Figure 2. The broken streamlines represent circumpolar flow and
 1029 the solid streamlines represent stationary eddies or gyre flow.



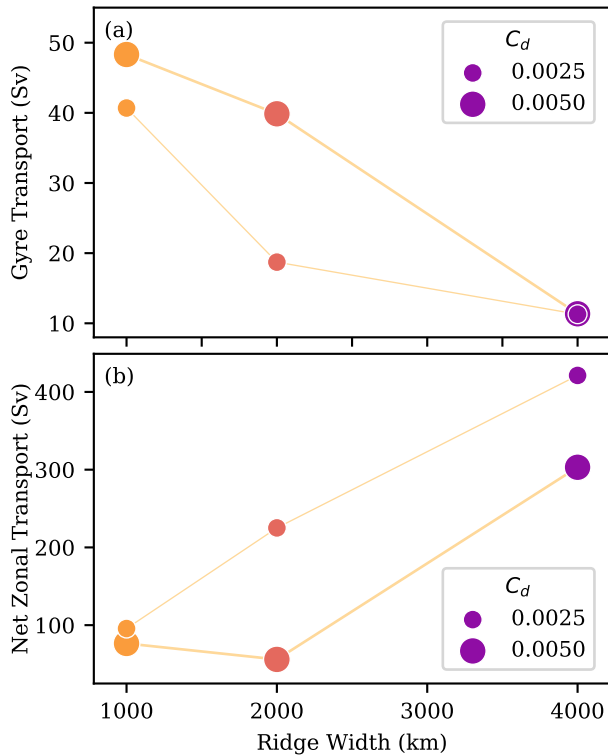
1030 FIG. 7. Plan view of two barotropic channel simulations with variation of the meridional extent. (b), (e) and
 1031 (h) show results for a 2000 m ridge height with 3600 km meridional extent (models 18, 20 and 21 respectively).
 1032 The grey section signifies land. (c), (f) and (i) show results for a 2000 m ridge height with 7200 km
 1033 meridional extent (models 22, 23 and 24 respectively). The ridge widths are: (b,c) 1000 km, (e,f) 2000 km and
 1034 (h,i) 4000 km. (Right) meridional profile of the zonal wind for each case. The coloured boxes to the top-right
 1035 of (a), (d) and (g) are associated with ridge width. For colouring and contouring see Figure 2. The broken
 1036 streamlines represent circumpolar flow and the solid streamlines represent stationary eddies or gyre flow.



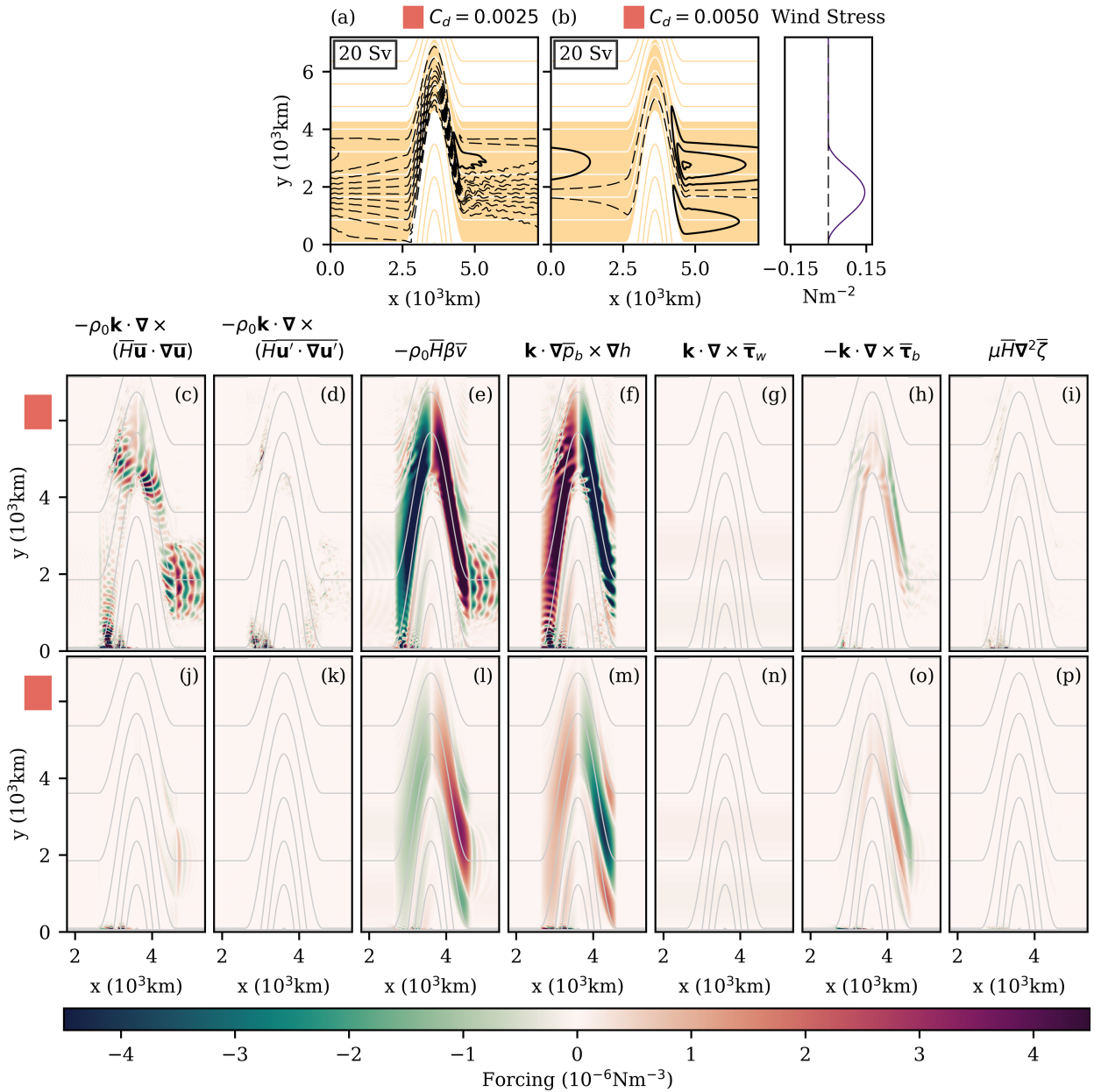
1037 FIG. 8. Terms of the barotropic vorticity equation for the extended simulations shown in Figure 7 (models
 1038 22-24). Simulations have a meridionally aligned ridge of 2000 m in height and of varying ridge widths. Rows
 1039 are associated with particular ridge widths (model 22: 1000 km, model 23: 2000 km and model 24: 4000
 1040 km). Columns represent differing barotropic vorticity terms: mean inertial term, eddy vorticity flux, advection
 1041 of planetary vorticity, bottom pressure torque, wind stress curl, bottom stress curl and viscosity. The coloured
 1042 boxes to the left of (a), (h) and (o) are associated with ridge width.



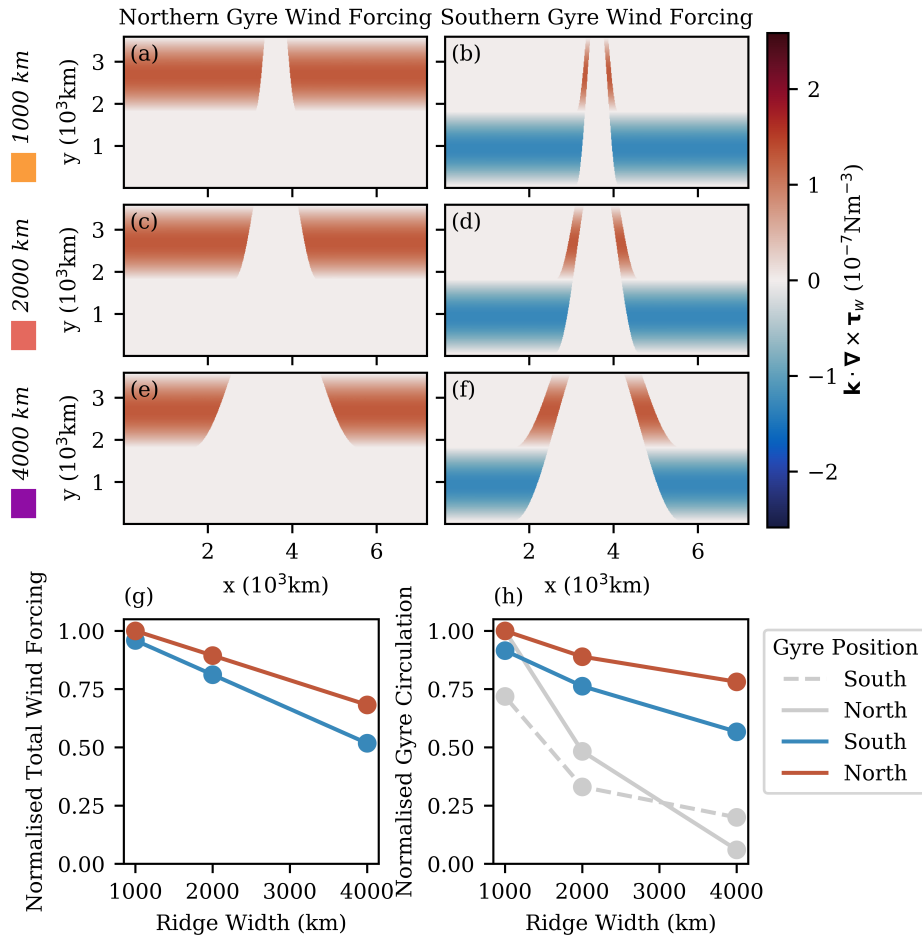
1043 FIG. 9. $\mathbf{k} \cdot \nabla \times \boldsymbol{\tau}_b$ for varying ridge width. Results are for model simulations 22 and 24 shown in Figure 8.
 1044 (a) and (b) show $\mathbf{k} \cdot \nabla \times \boldsymbol{\tau}_b$ for results with ridge width of 1000 km and 4000 km respectively. Solid grey lines
 1045 in (a) and (b) are contours of f/h . (c) shows $\mathbf{k} \cdot \nabla \times \boldsymbol{\tau}_b$ for the 4000 km ridge simulation focused on the eastern
 1046 flank of the ridge with streamlines overlaid in black. The broken black streamlines represent circumpolar flow
 1047 and the solid black streamlines represent stationary eddies or gyre flow. Broken grey lines in (c) are contours
 1048 of f/h . The box to the top-right of (c) shows the streamline spacing in Sverdrups. The coloured boxes above
 1049 (a)-(c) are associated with ridge width.



1050 FIG. 10. Volume transport versus ridge width for varying bottom stress coefficient (C_d) of 0.0025 and 0.0050
 1051 (models 22-27). The simulations with bottom stress coefficient of 0.0025 are same as presented in Figures 7c,
 1052 7f, 7i and 8. (a) Gyre strength versus ridge width for varying bottom stress coefficient. (b) Circumpolar transport
 1053 versus ridge width for varying bottom stress coefficient.



1054 FIG. 11. Barotropic streamfunction and terms of the barotropic vorticity equation for simulations with a
 1055 meridionally aligned ridge of 2000 m in height 2000 km in width. Results are for model simulations 23 and 26
 1056 shown in Figure 10 with varying bottom stress coefficient (C_d). (a) and (b) show the barotropic streamfunction of
 1057 results with bottom stress coefficient of 0.0025 and 0.0050 respectively. For colouring and contouring see Figure
 1058 2. The broken streamlines represent circumpolar flow and the solid streamlines represent stationary eddies or
 1059 gyre flow. Rows of panels (c)-(p) are associated with a particular bottom stress coefficient ((c)-(i): 0.0025 and
 1060 (j)-(p): 0.0050). Columns of panels (c)-(p) represent differing barotropic vorticity terms: mean inertial term,
 1061 eddy vorticity flux, advection of planetary vorticity, bottom pressure torque, wind stress curl, bottom stress curl
 1062 and viscosity. The coloured boxes above (a) and (b) then to the left of (c) and (j) are associated with ridge width.



1063 FIG. 12. The wind stress curl over each gyre in Figures 7b (model 18), 7e (model 20) and 7h (model 21).
 1064 (a)-(f) show a plan view of the wind forcing over each gyre with ridge width displayed in the top-right of each
 1065 plot. (g) shows an area integral of the forcing in (a)-(f) normalised to the area integral for (b). (h) shows the gyre
 1066 strength versus ridge width. The grey lines in (h) correspond to the normalised gyre strength of models 22-24
 1067 where the meridional extent is 7200 km (See Figures 7c, 7f and 7i). The coloured boxes to the left of (a), (c) and
 1068 (e) are associated with ridge width.